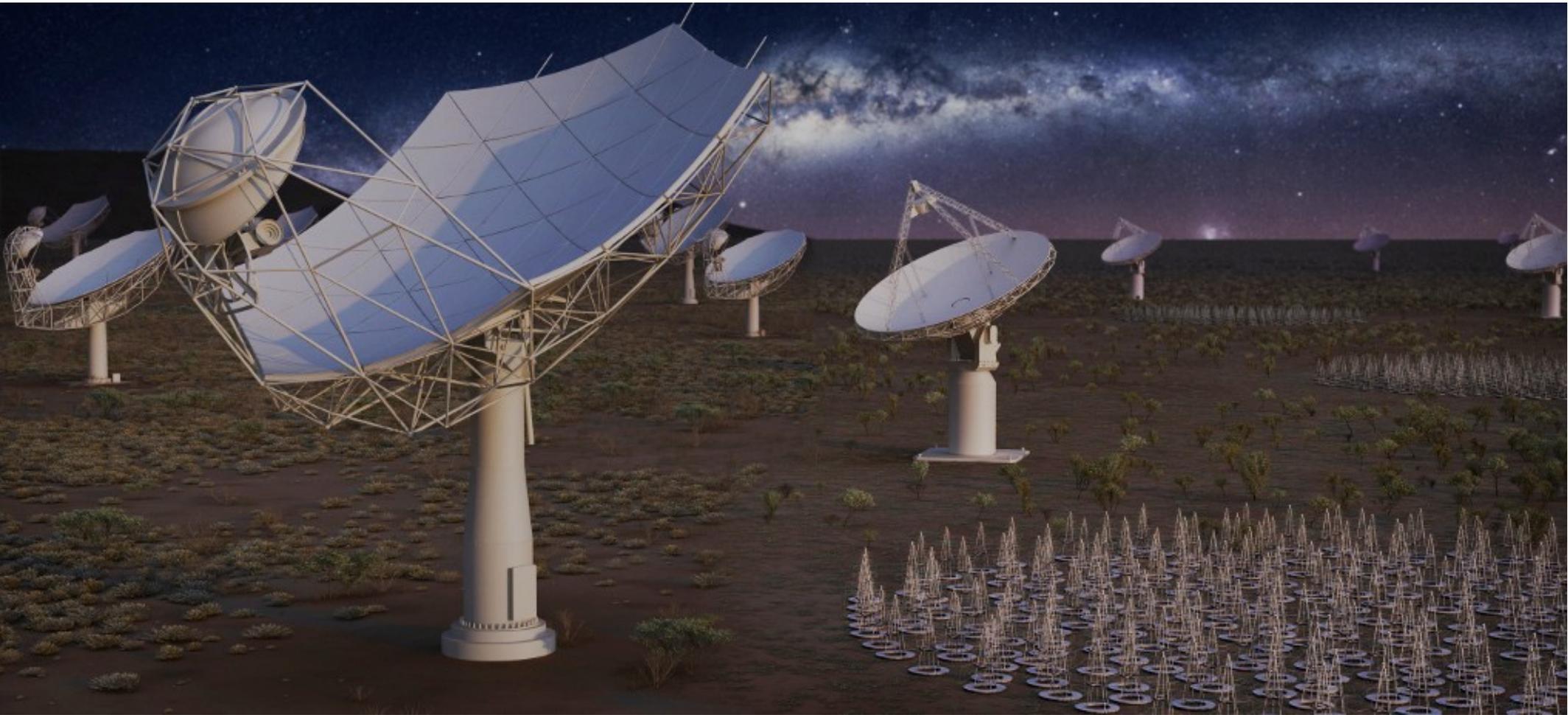


# Cosmology with the SKA



**Lucchin school 2016**  
OACN / INAF

**Phil Bull**  
JPL/Caltech  
+ SKA Cosmology SWG

# Outline

## **Lecture 1: The sky through a radio telescope**

1. Radio astronomy in the SKA era
2. Basics of radio receivers
3. Detecting radio sources
4. Fundamentals of interferometry

## **Lecture 2: Radio galaxies**

1. Physical sources of radio emission in galaxies
2. Aperture synthesis
3. Continuum surveys; 2D correlations and weak lensing
4. HI galaxy redshift surveys; peculiar velocities

## **Lecture 3: Intensity mapping**

1. Intensity mapping
2. Designing an intensity mapping experiment
3. Foreground contamination
4. Open questions and the future of radio cosmology

# The era of big surveys

The way we do astronomy is changing!

***Big science:*** Big surveys, big datasets, big teams, big questions, big budgets...

**(Big headaches)**

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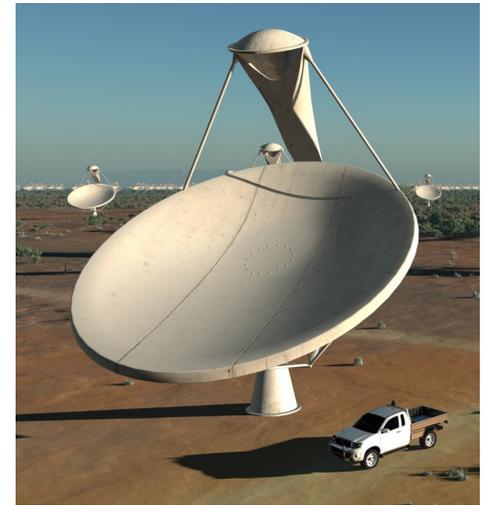
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**(Big headaches)**



**Euclid**  
(ESA/Astrium)

**New science!**

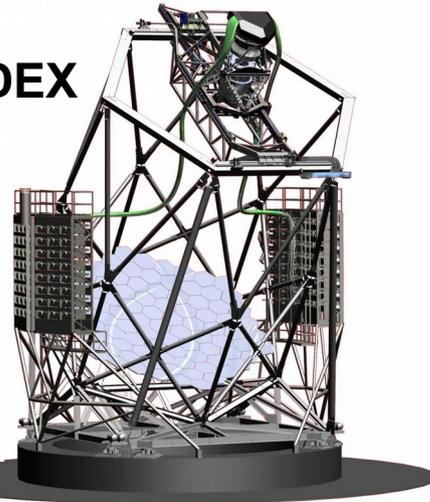


**SKA (SKAO)**

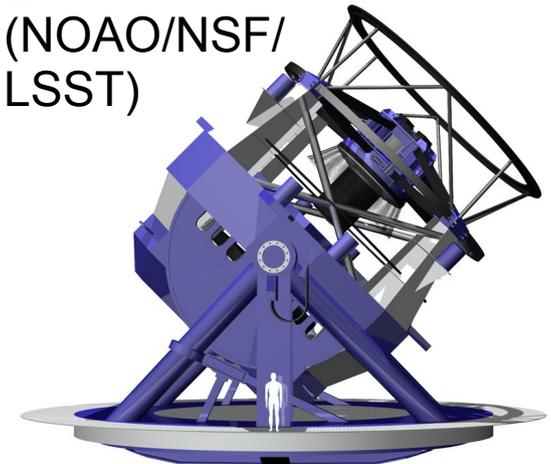


**WFIRST (NASA)**

**HETDEX**



**LSST**  
(NOAO/NSF/  
LSST)



# What we want...

## ***Understanding!***

- What is dark energy?
- Is inflation real?
- Where does General Relativity break down?
- Are there other particles? Forces? (e.g. dark matter)

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# What we need...

## *Data!*

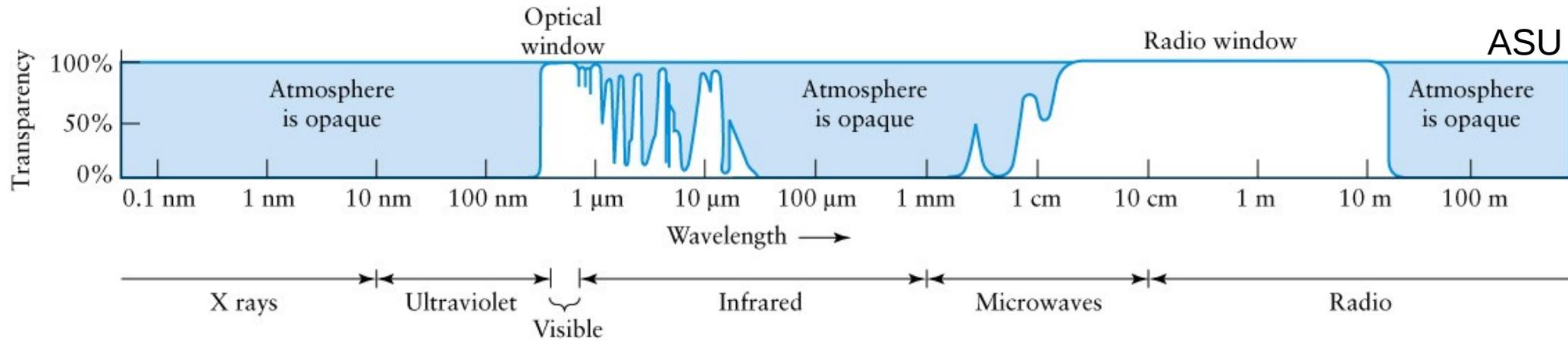
- Map of how matter is distributed throughout space-time
- Information on how structures grow
- **Observe billions(!) of galaxies across cosmic time**

## *Theory!*

- New ideas on how to explain these phenomena
- (See [arXiv:1512.05356](https://arxiv.org/abs/1512.05356) for a review...)

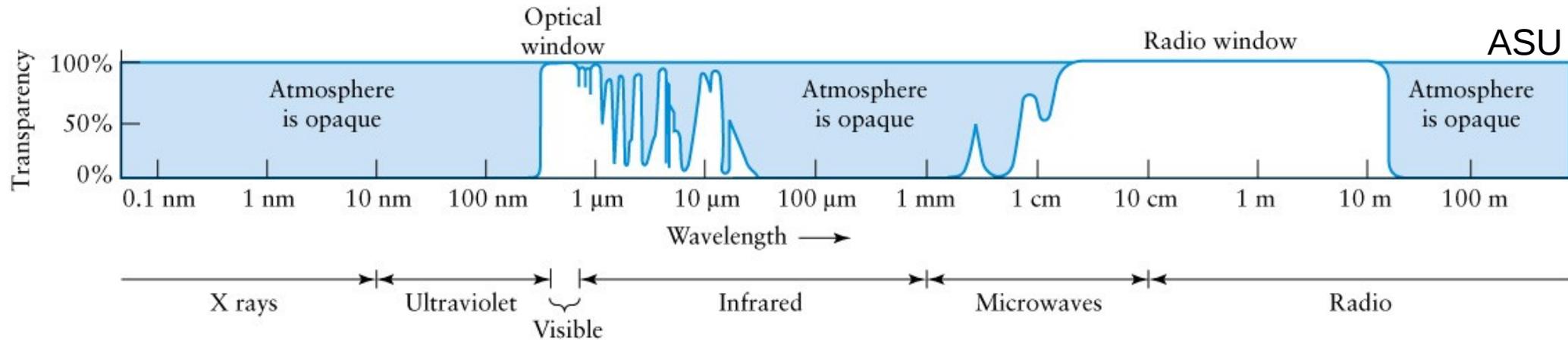
# Radio cosmology

The radio sky is very different to other wavelengths



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The radio sky is very different to other wavelengths



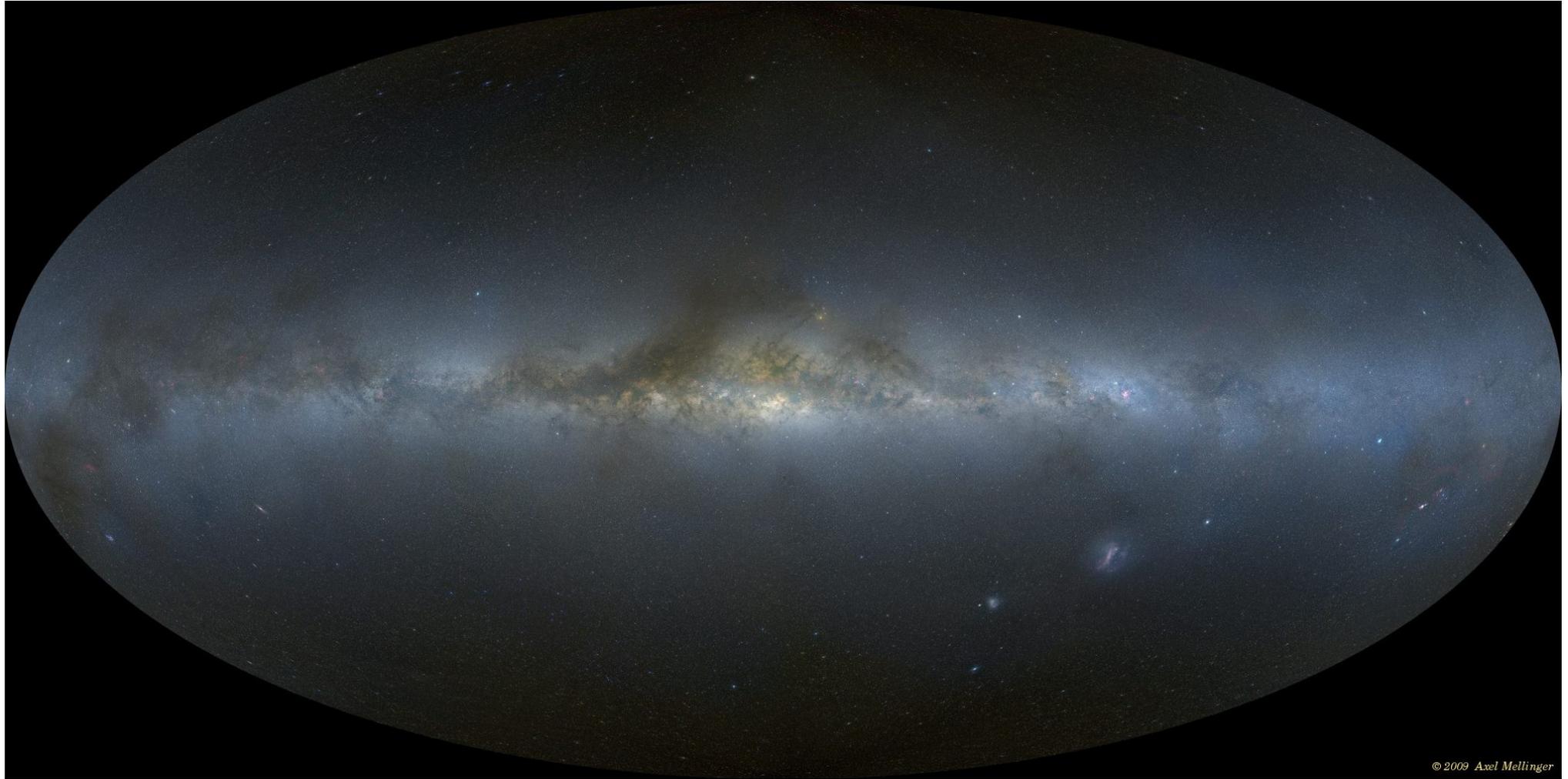
**Lots of high-energy physics:** Black holes, neutron stars, pulsars, supernovae... Many bright objects to look for

**Radio doesn't get absorbed easily:** Radio waves emitted by neutral hydrogen pass through dust/gas

**Efficient way of seeing 100's of millions of galaxies that trace the large-scale structure of space-time**

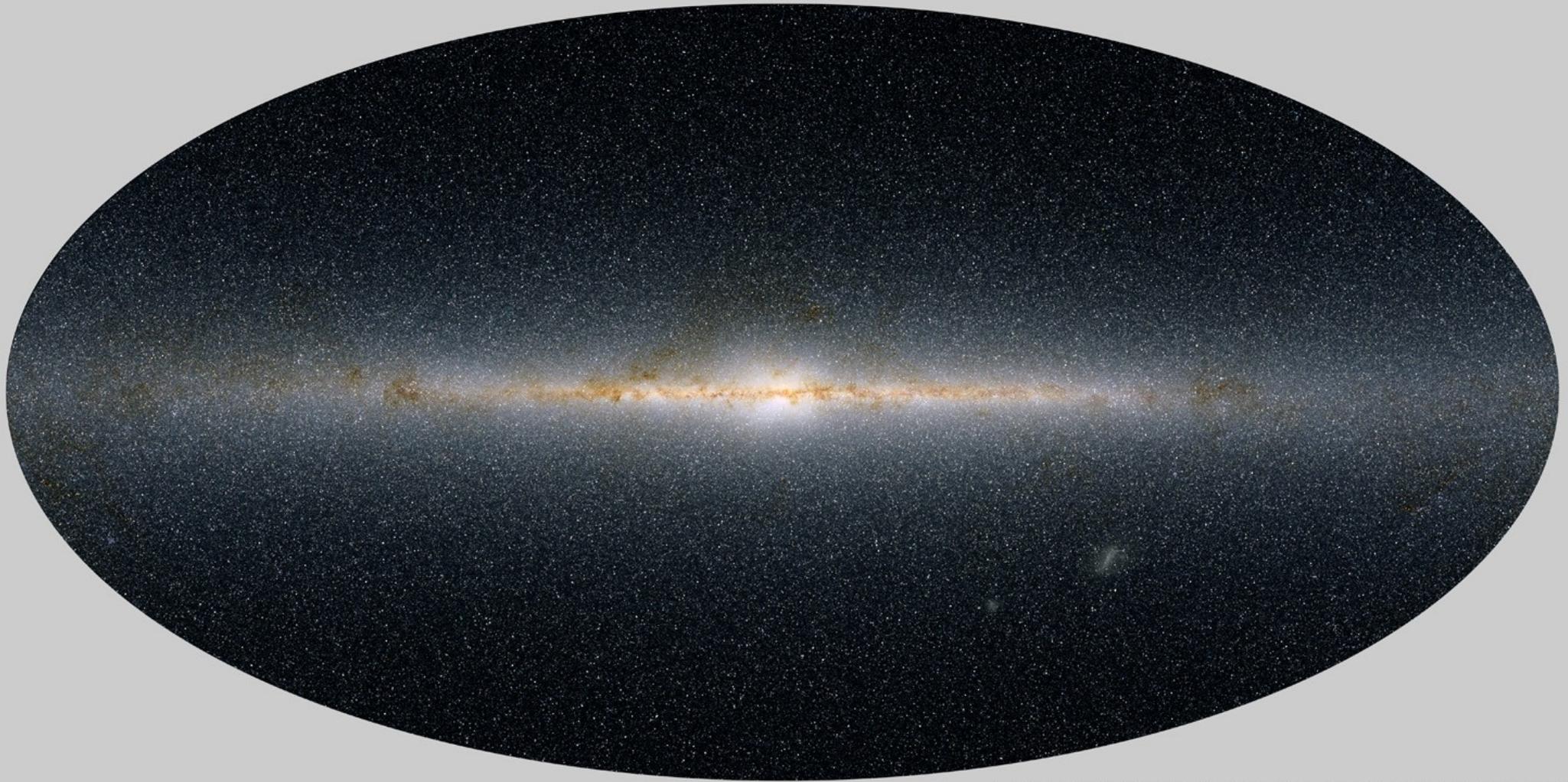
# Radio astronomy in the SKA era

# The sky



**Optical**

# The sky

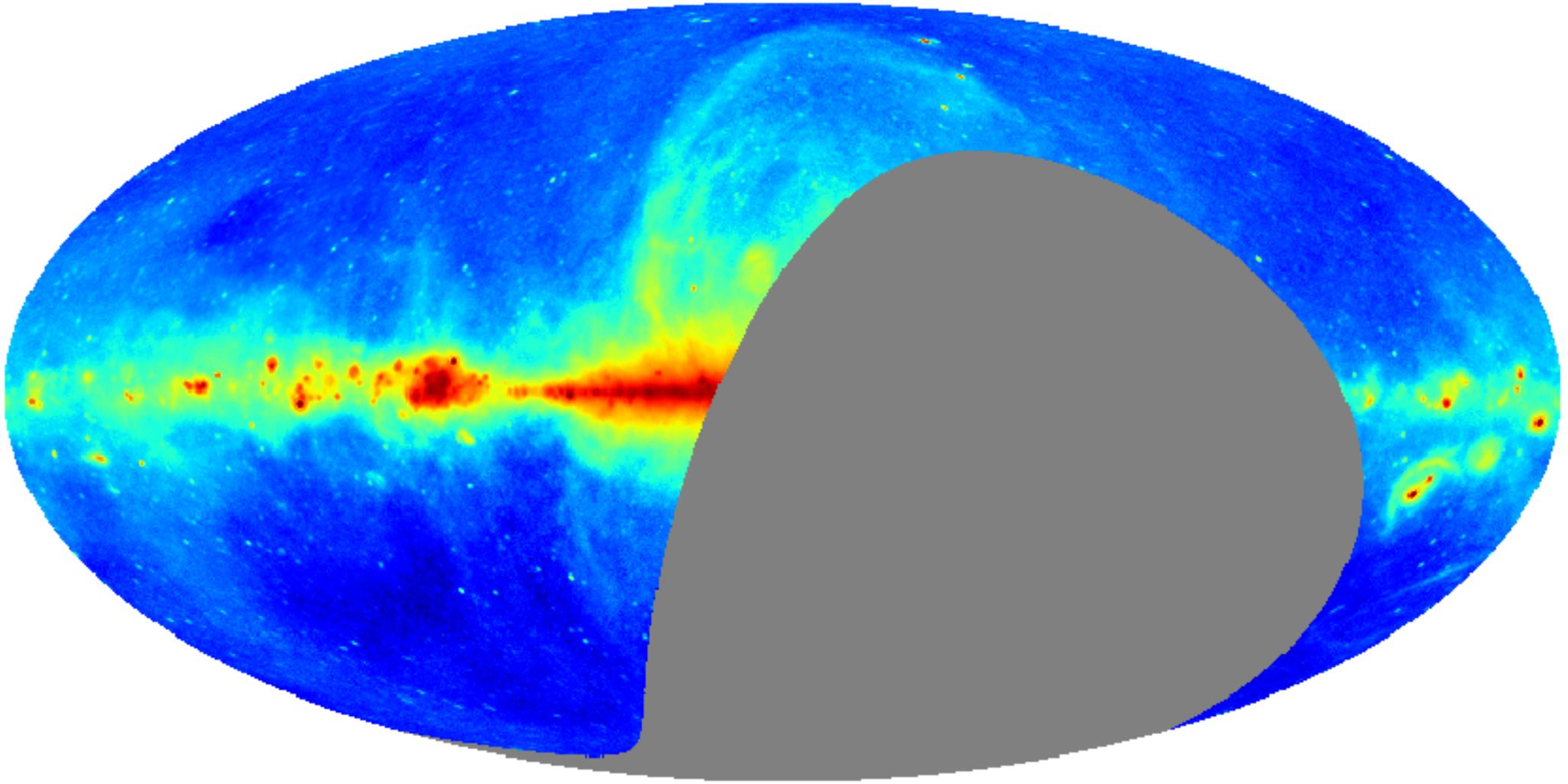


Two Micron All Sky Survey Image Mosaic: Infrared Processing and Analysis Center/Caltech & University of Massachusetts

# Infrared

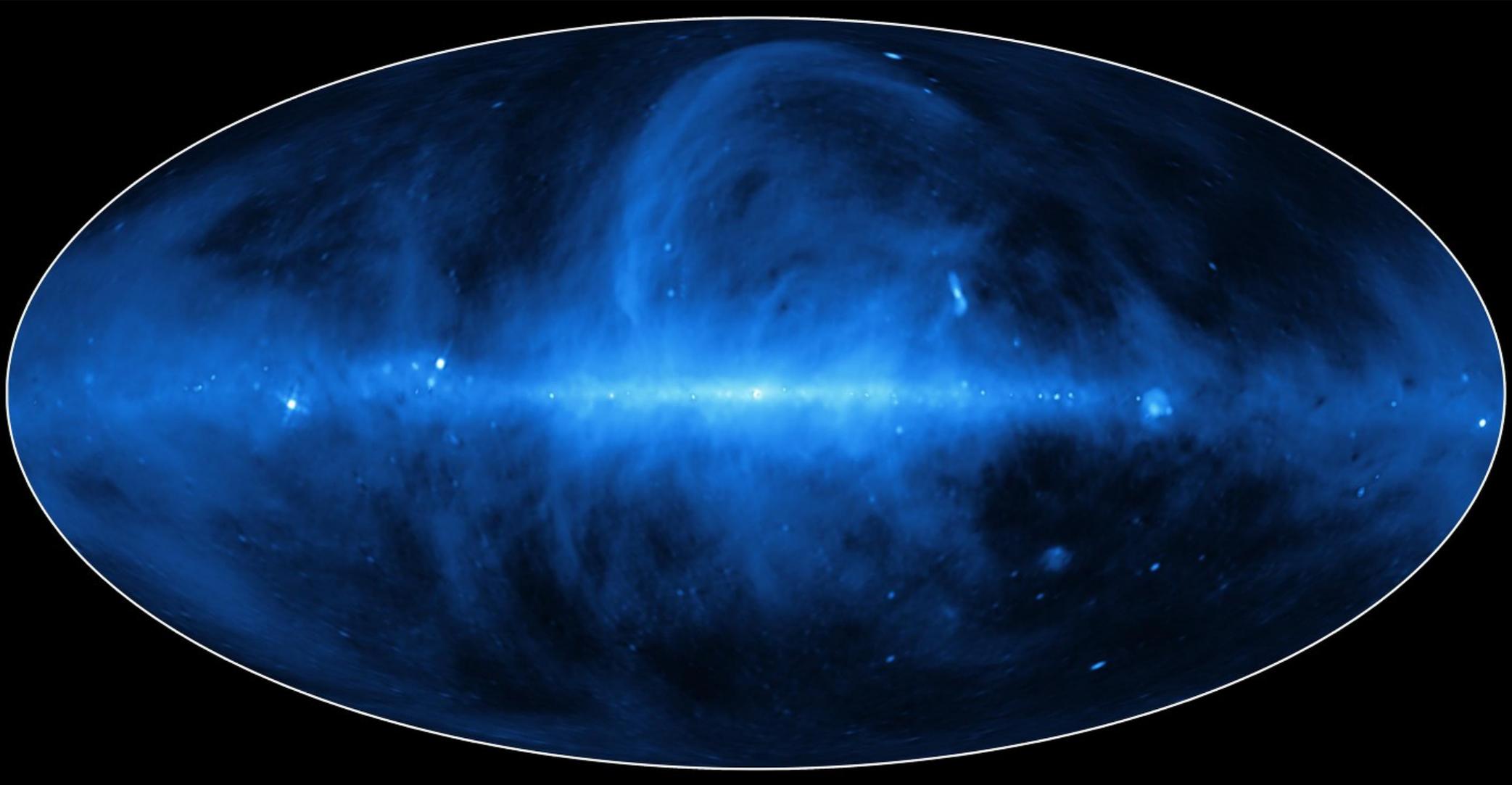
2MASS

# The sky



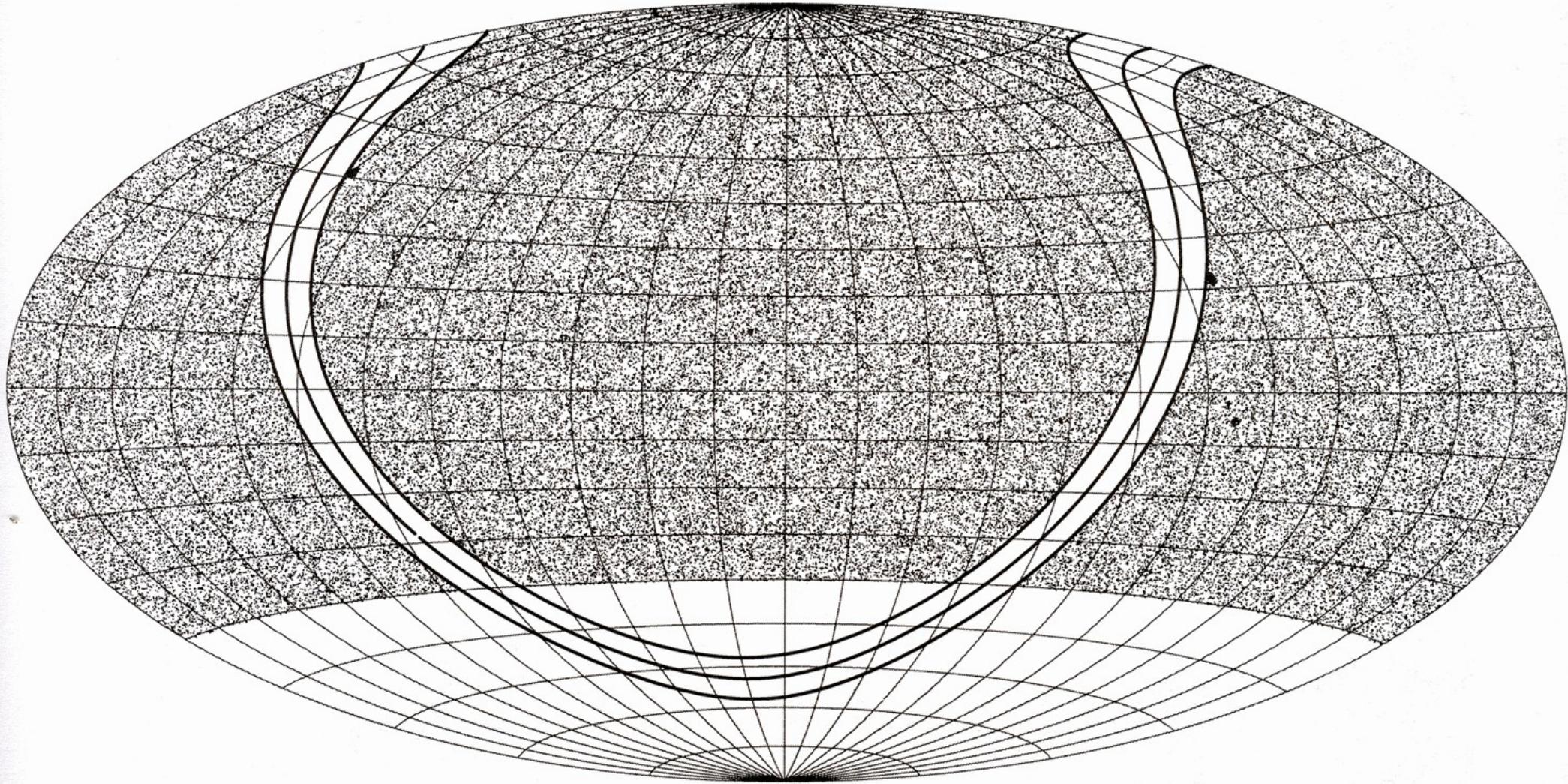
**Radio (5 GHz)**

# The sky



**Radio (1.4 GHz)** (rescaled)

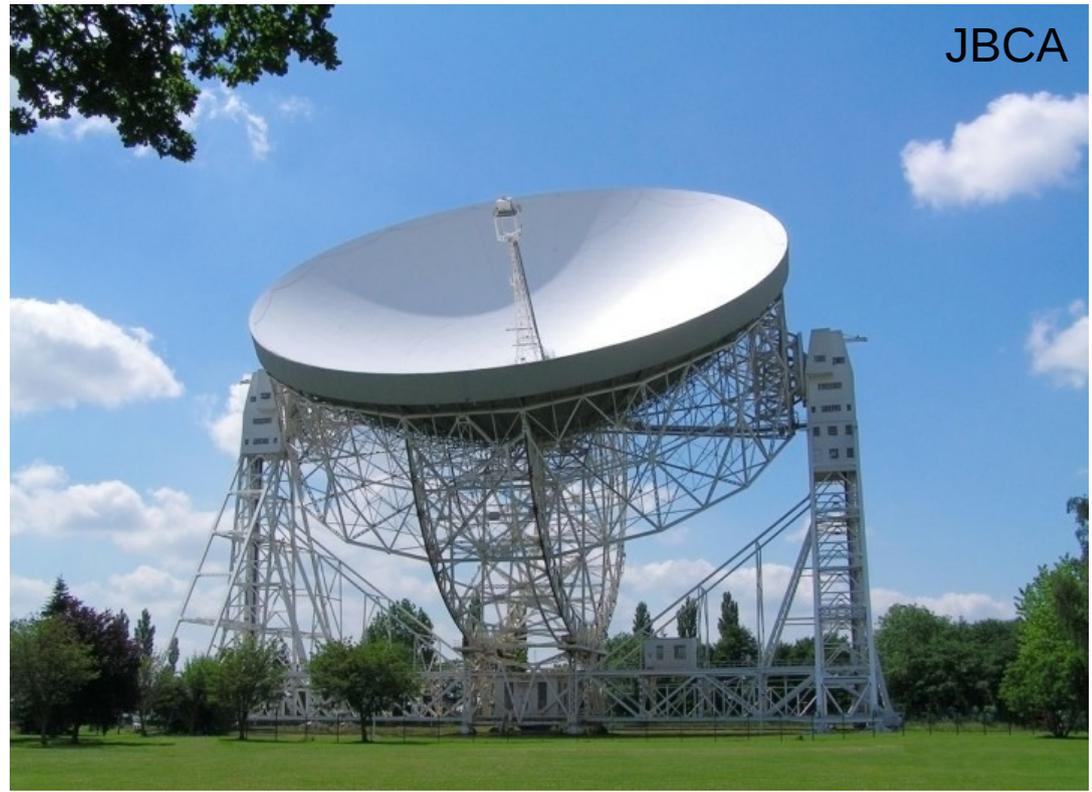
# The sky



**Radio (1.4 GHz)** (just galaxies)

# Single-dishes

“Classic” single-dish radio telescopes



Arecibo

# Radio arrays



VLA /  
NRAO



LOFAR / ASTRON

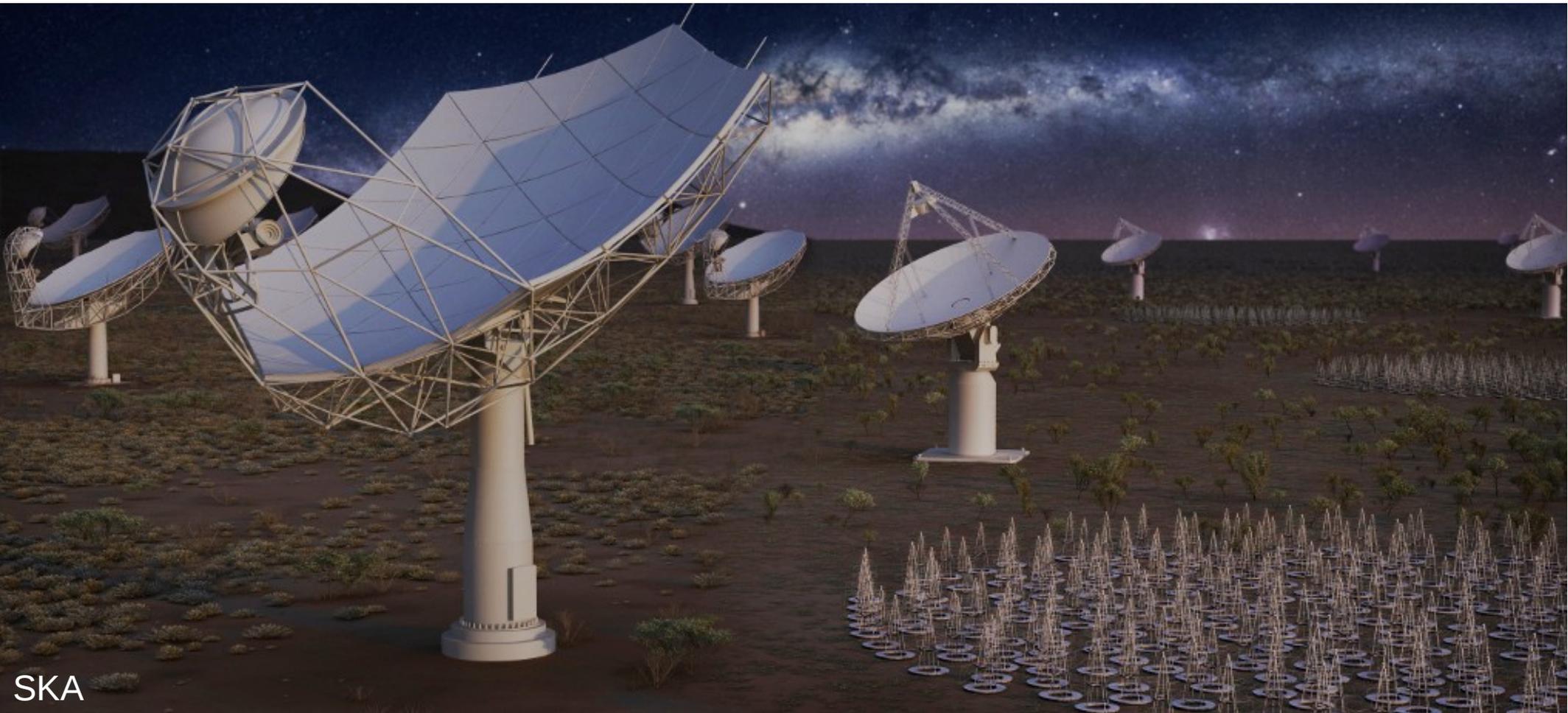


ATCA

# Square Kilometre Array

**SKA1-MID**  
(South Africa)

**Mid-frequency dish array**  
350 MHz – 14 GHz (5 bands), 190 dishes

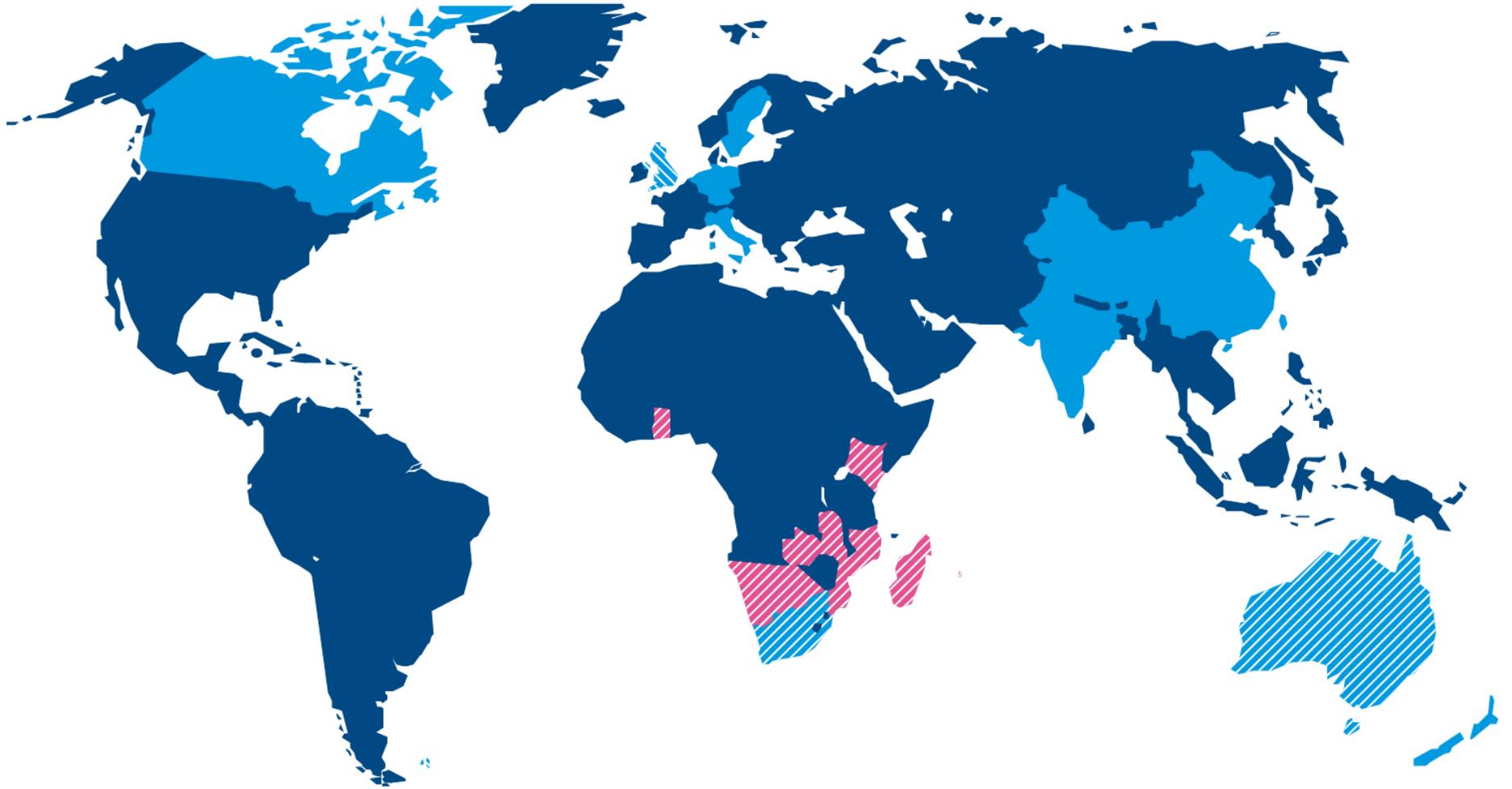


SKA

**Low-frequency aperture array**  
50 – 350 MHz, ~500 stations x 90 dipoles

**SKA1-LOW**  
(Australia)

# Square Kilometre Array



- Full members
- ▨ SKA Headquarters host country
- ▨ SKA Phase 1 and Phase 2 host countries



- ▨ African partner countries  
(non-member SKA Phase 2 host countries)

This map is intended for reference only and is not meant to represent legal borders

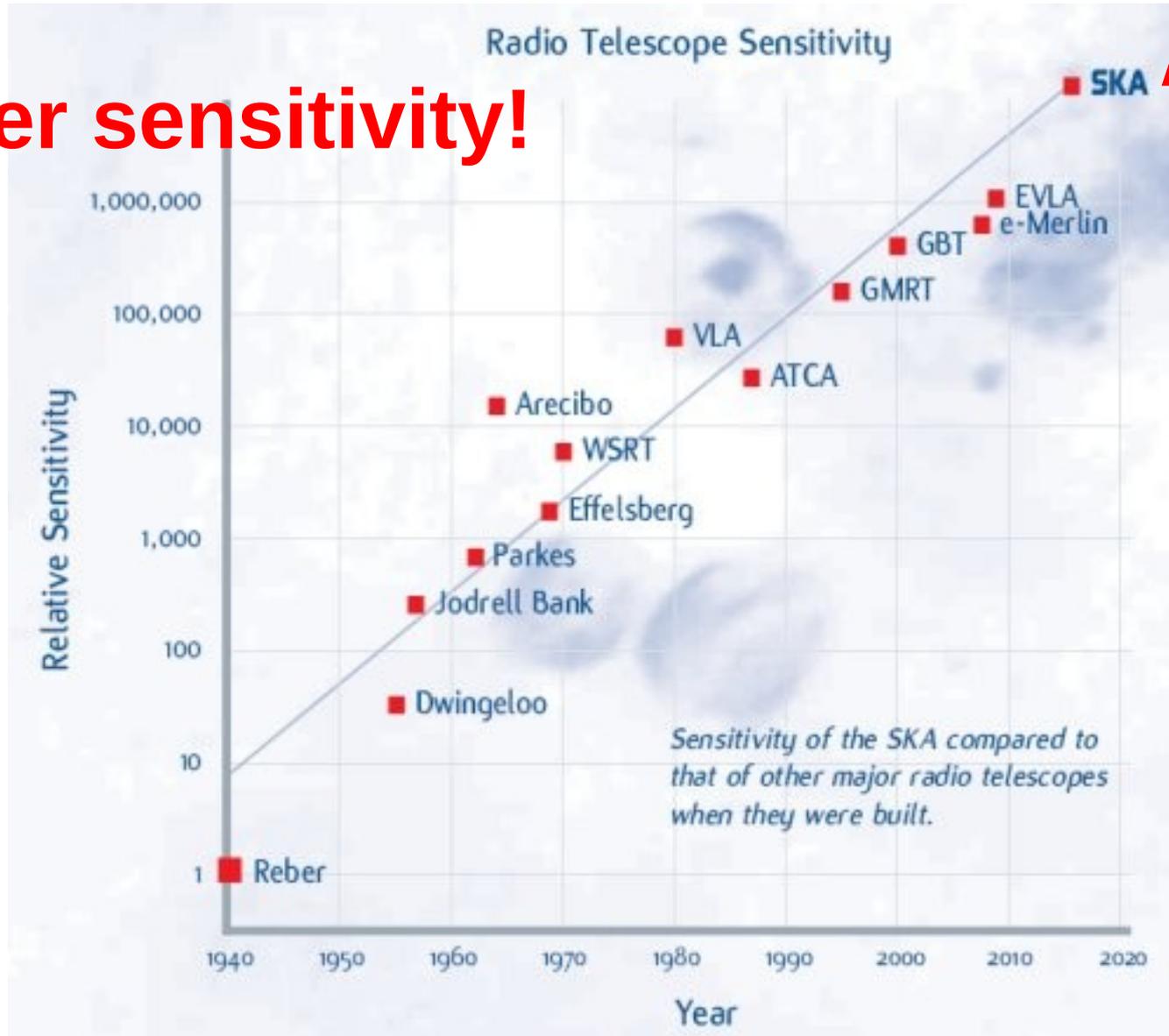
# The SKA in context

What does the SKA do that older radio telescopes don't?

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What does the SKA do that older radio telescopes don't?

**Higher sensitivity!**



**Better!**



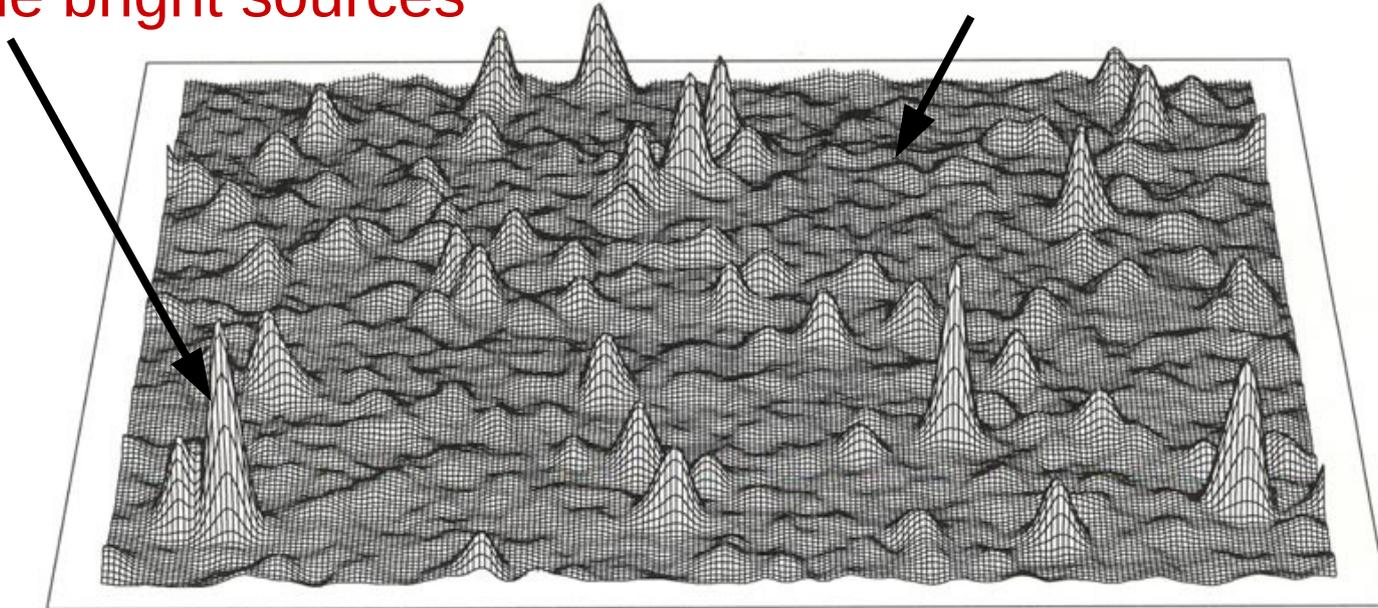
# How to improve radio telescopes

## Better sensitivity:

- Low-noise receivers (cryogenics, better amplifiers)
- Better location (less radio interference, better weather)
- Bigger dish / more dishes (interferometer)
- Wider bandwidth (collect more photons!)

**Low sensitivity = high noise**  
Only see the bright sources

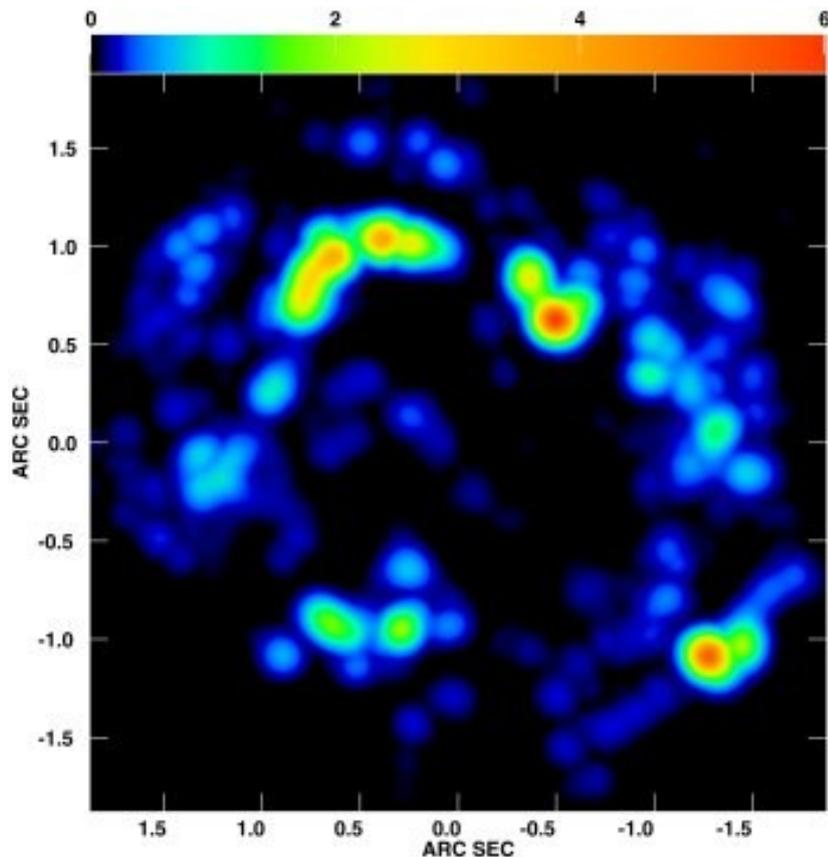
**High sensitivity = low noise**  
Can also see fainter sources



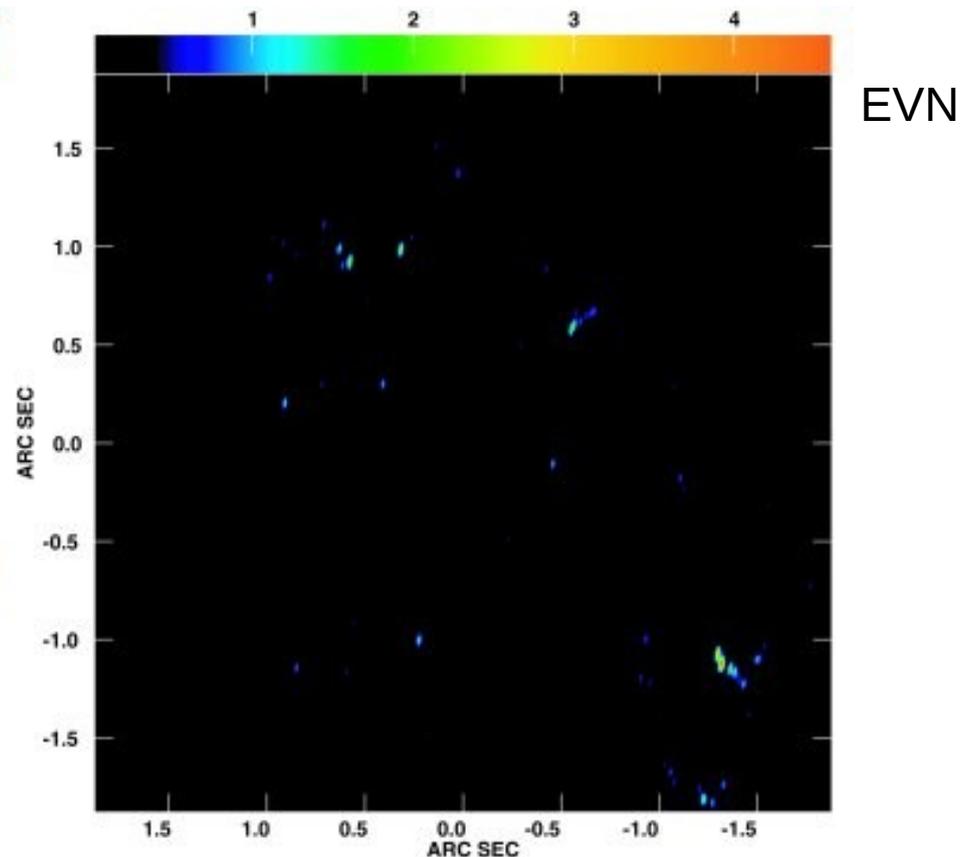
# How to improve radio telescopes

## Better resolution:

- Bigger dish (single-dish)
- More dishes, longer baselines (interferometer)



Short baselines (low resolution)



Long baselines (high resolution)

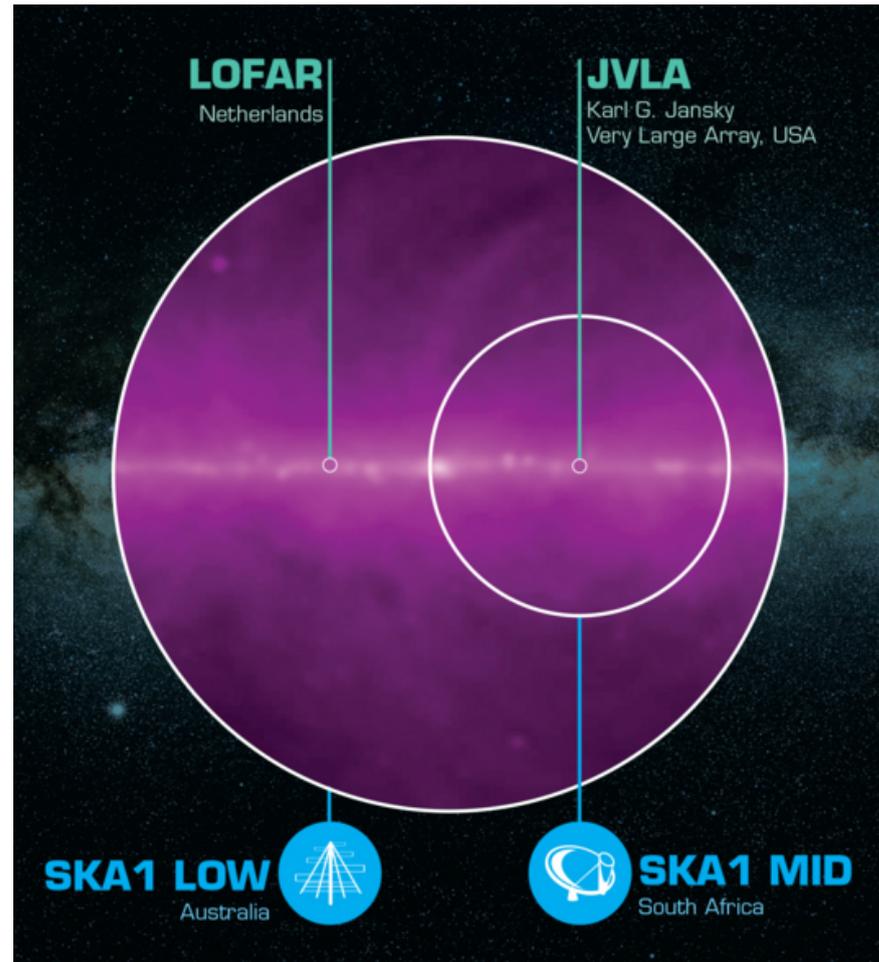
# How to improve radio telescopes

## Faster surveys:

- Lower noise
- Bigger field of view
- Multi-beam receivers

## New science:

- Cover different wavelengths
- Narrow frequency channels
- Faster sampling / processing



# The SKA does all these things...

- Better sensitivity (more dishes, low-noise receivers)
- Better resolution (more dishes, more baselines)
- Big bandwidth, many bands, many frequency channels
- Excellent sites (South African and Australian deserts, low RFI)
- Huge field of view (fast surveys)

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## Remember what cosmologists need...

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SKA intensity mapping survey: reconstruct the large-scale matter distribution from  $0 < z < 12$

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### **Observe billions of galaxies across cosmic time**

SKA continuum galaxy survey: detect millions of galaxies out to  $z \sim 5$ ; measure lensing and 2D clustering

# The SKA does all these things...

**Welcome to the era of  
radio cosmology!**

- Better sensitivity (more dishes, low-noise receivers)
- Better resolution (more dishes, more baselines)
- Big bandwidth, many bands, many frequency channels
- Excellent frequency coverage (wide bandwidths, low RFI)
- Huge field of view (fast surveys)

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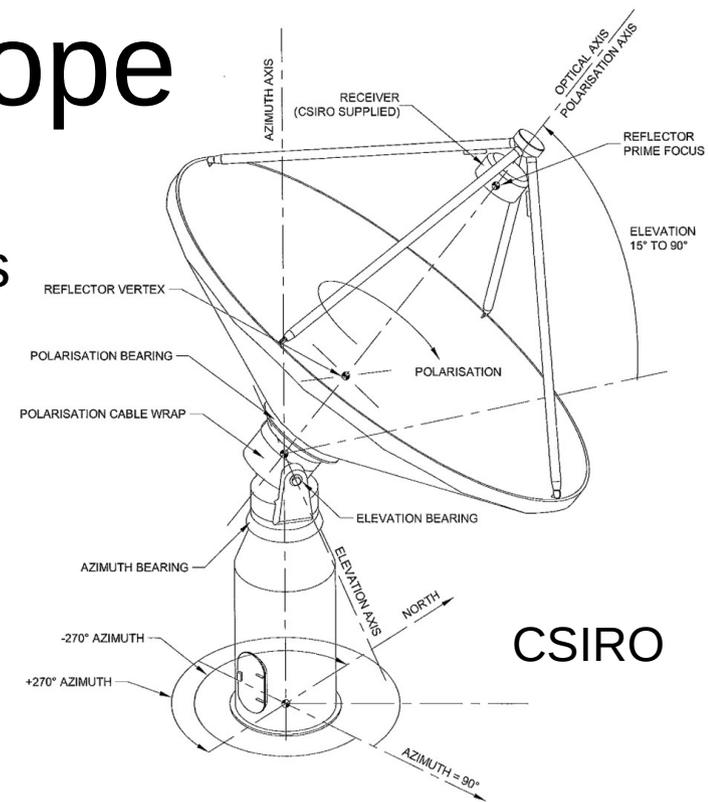
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# Basics of radio receivers

# Anatomy of a radio telescope

Reflector/  
antenna

Focuses and collects radio waves  
and feeds them into electronics



# Anatomy of a radio telescope

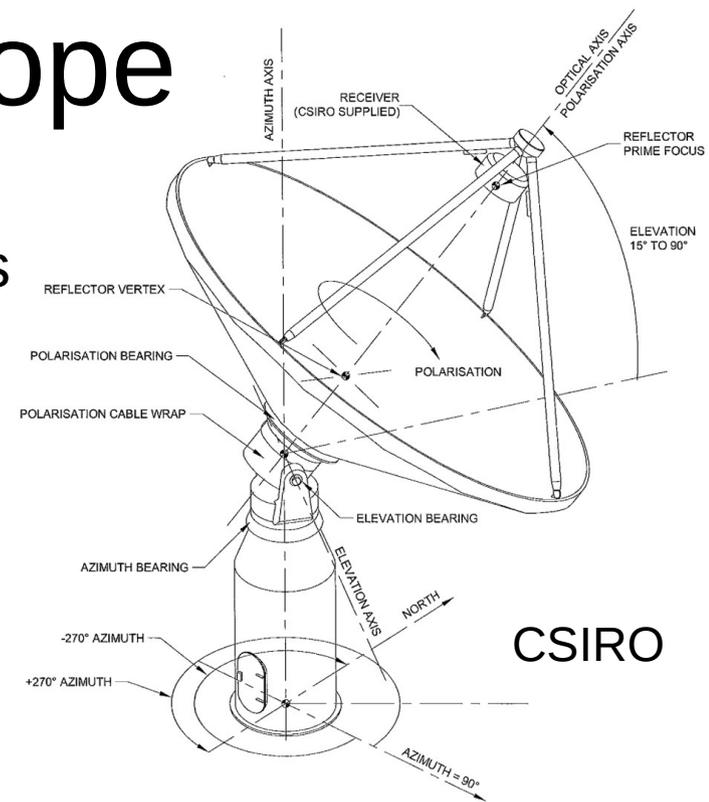
Reflector/  
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Mixers /  
filters

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Converts waves into lower-  
frequency signal and filters out  
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# Anatomy of a radio telescope

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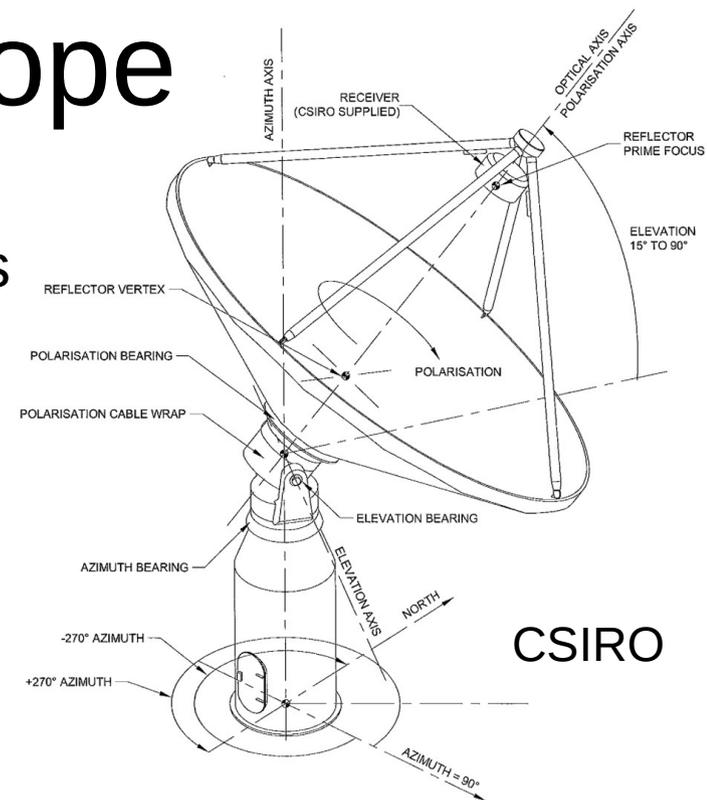
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Amplifiers

Boost the amplitude of input signals  
(without adding too much extra noise!)



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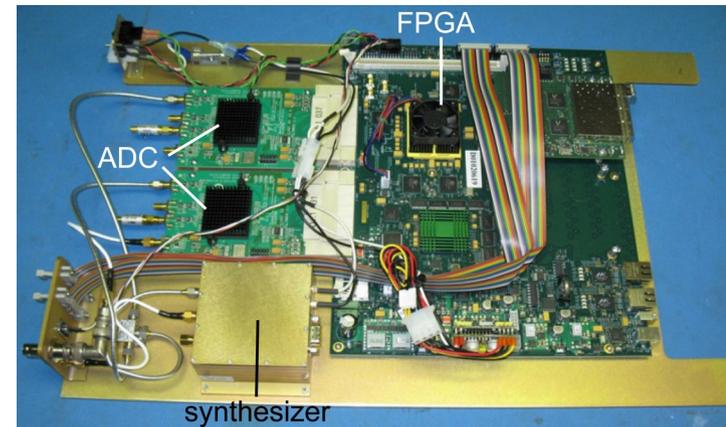
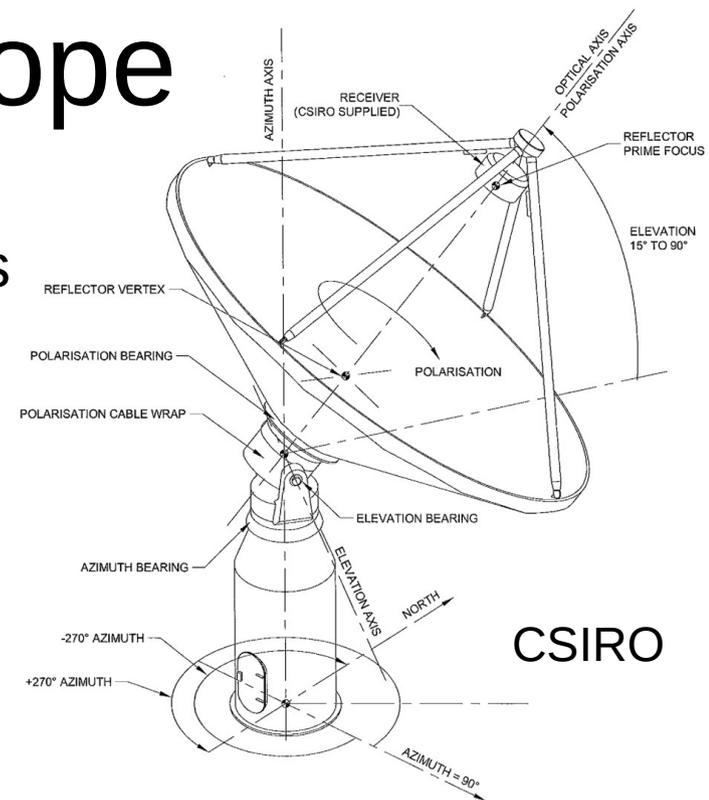
Amplifiers

Boost the amplitude of input signals (without adding too much extra noise!)

Backend

“Detects” and digitises input signals, splits into frequency channels, sends data to PC

Real systems can be **much** more complicated!



# Resolution and collecting area

ICRAR

## Antenna

- Collects and focuses radio waves
- All you need is a conductive material!
- Dishes focus waves from one direction
- Dipoles collect waves from most of the sky



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## Diffraction / optics

- Shape of antenna and optical path determine how much radiation enters the telescope from each direction → sets the **resolution**
- Area (*aperture*) of antenna sets the total amount of radiation entering the telescope

$$\theta \approx \mathcal{O}(1) \times (\lambda/D_{\text{dish}})$$

$$A_{\text{eff}} \approx 0.7\pi(D_{\text{dish}}/2)^2$$

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## Diffraction / optics

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- Area (*aperture*) of antenna sets the total amount of radiation entering the telescope
- Trade-off between sensitivity and resolution? → **Interferometry**



# Noise and sensitivity

## Receiver noise

- Radio receivers measure signal + **thermal noise**
- Noise comes from electronics, the sky, the ground...
- Total noise temperature is the **system temperature**

## Reducing noise

- Lower system temperature = less noise
- Can **average the signal** over time – noise averages down
- Can also average the signal over **frequency**;  
*wider bandwidth* = more photons = lower noise

## Radiometer equation

$$\sigma_T \approx \frac{T_{\text{sys}}}{\sqrt{\delta\nu t_{\text{obs}}}} \approx \frac{\text{Thermal noise temperature}}{\text{Number of "samples"}}$$

# Typical numbers: SKA1-MID dish (band 1)

<b>Dish diameter:</b>	15 m
<b>System temperature:</b>	23 K
<b>Total bandwidth:</b>	700 MHz
<b>Observing frequency:</b>	350 – 1050 MHz
<b>Frequency channels:</b>	Can choose! (~10 kHz typical)
<b>Observing time:</b>	Can choose! (Let's try 1 hour)

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$$\theta \approx \mathcal{O}(1) \times (\lambda/D_{\text{dish}})$$

~1.1 degrees @ 1000 MHz

$$A_{\text{eff}} \approx 0.7\pi(D_{\text{dish}}/2)^2$$

~124 m<sup>2</sup>

$$\sigma_{\text{T}} \approx \frac{T_{\text{sys}}}{\sqrt{\delta\nu t_{\text{obs}}}}$$

~3.8 mK (10 kHz channel)

# Detecting radio sources

# Detecting galaxies

What determines whether we can “see” a galaxy with a radio telescope?

(1) How bright is the galaxy?

**Flux density:** how much power is received from the source?

$$S_\nu = \int_{\text{source}} I_\nu(\theta, \phi) d\Omega \qquad S = \frac{L}{4\pi d_L^2}$$

$$1\text{Jy} = 10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1}$$

- Galaxy flux densities are usually ~mJy or  $\mu\text{Jy}$
- A mobile phone at 1km has  $S \sim 1 \text{ MJy}$ !

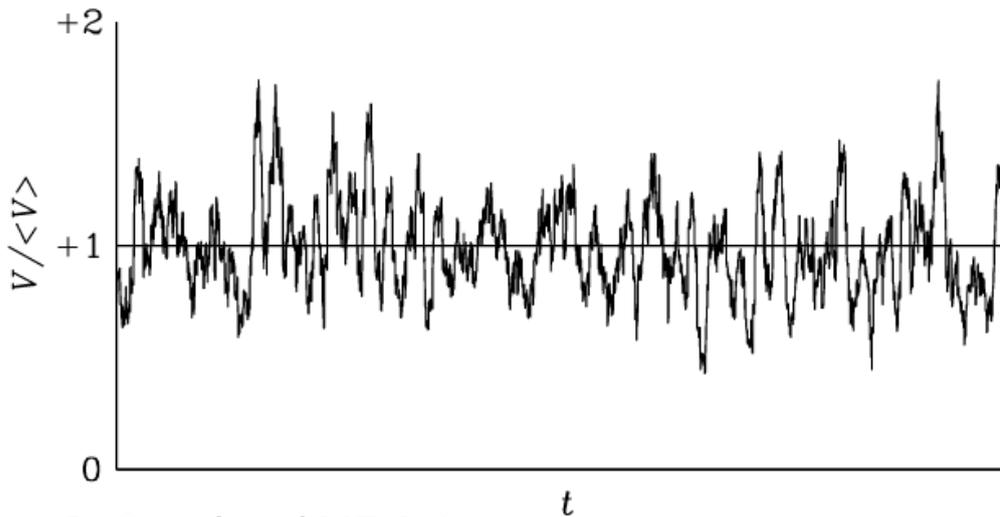
# Detecting galaxies

What determines whether we can “see” a galaxy with a radio telescope?

(2) How sensitive is the radio telescope?

- Radio waves cause *voltages* in the receiver electronics
- The voltages are *amplified* to make them measurable

**Thermal noise** from the sky and inside the receiver electronics gets added to the voltage signal of the source



J. Condon / NRAO

$$\sigma_S \approx \frac{2k_B T_{\text{sys}}}{A_{\text{eff}} \sqrt{\delta\nu t_{\text{obs}}}}$$

**Radiometer equation**  
(flux sensitivity)

# Detecting galaxies

What determines whether we can “see” a galaxy with a radio telescope?

(3) Are other things contaminating the signal?

The telescope measures the **total amount of radiation** coming from the direction it is pointing in

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- What if we're actually seeing  $>1$  galaxies close together?
- Or emission from our own galaxy?
- Or emission from Earth/satellites/mobile phones?
- Or just a random noise fluctuation?

# Detecting galaxies

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- What if we're actually seeing  $>1$  galaxies close together?

## **Confusion**

- Or emission from our own galaxy?

## **Foregrounds**

- Or emission from Earth/satellites/mobile phones?

## **Interference / RFI**

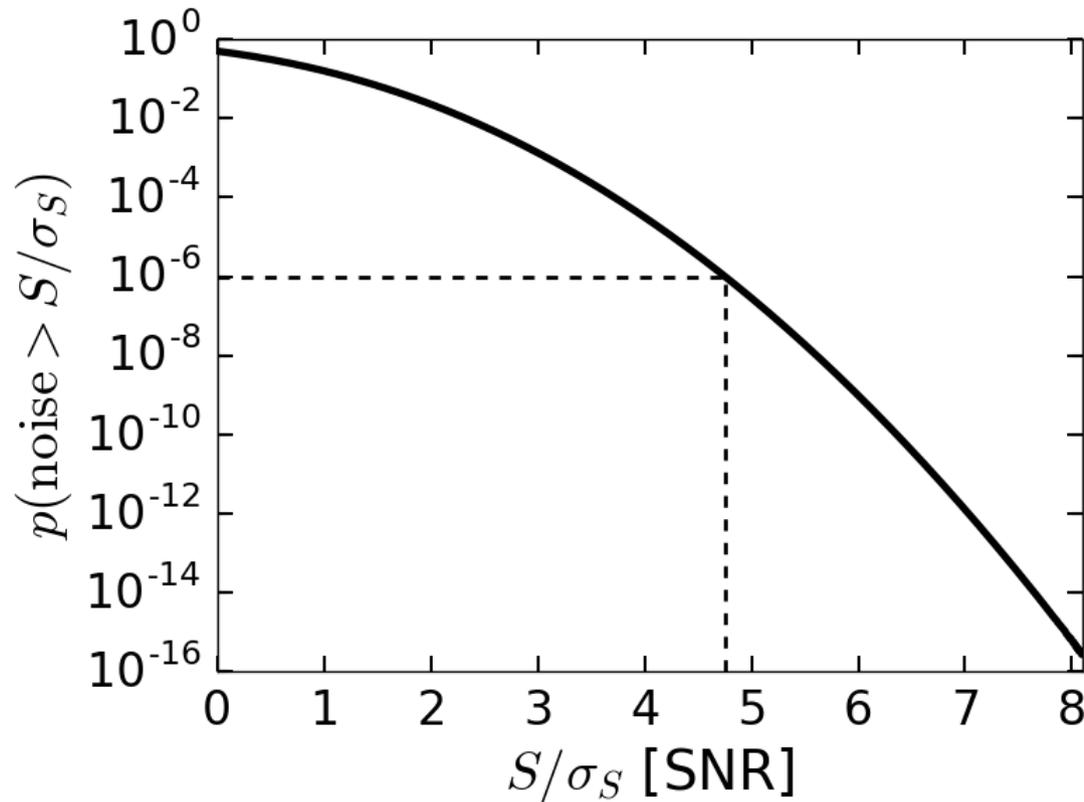
- Or just a random noise fluctuation?

## **Statistical fluctuations**

# Thresholding

How often will we mistake a noise fluctuation for a galaxy?

→ Can only “keep” candidate galaxies that are several times brighter than the noise level



In a sample of  $10^6$  galaxies with  $S > 4.75 \sigma_S$ :

~1 will be a noise fluctuation!

(assumes Gaussian noise)

**Thresholding** throws away random fluctuations **and** real galaxies that are too faint

# Confusion

ESA / Herschel

Objects that appear close together on the sky:

*Can the telescope tell if they are separate objects?*

If not, the sources are said to be **confused** with each other

There are typically many more faint sources than bright ones

→ image can be crowded with faint objects

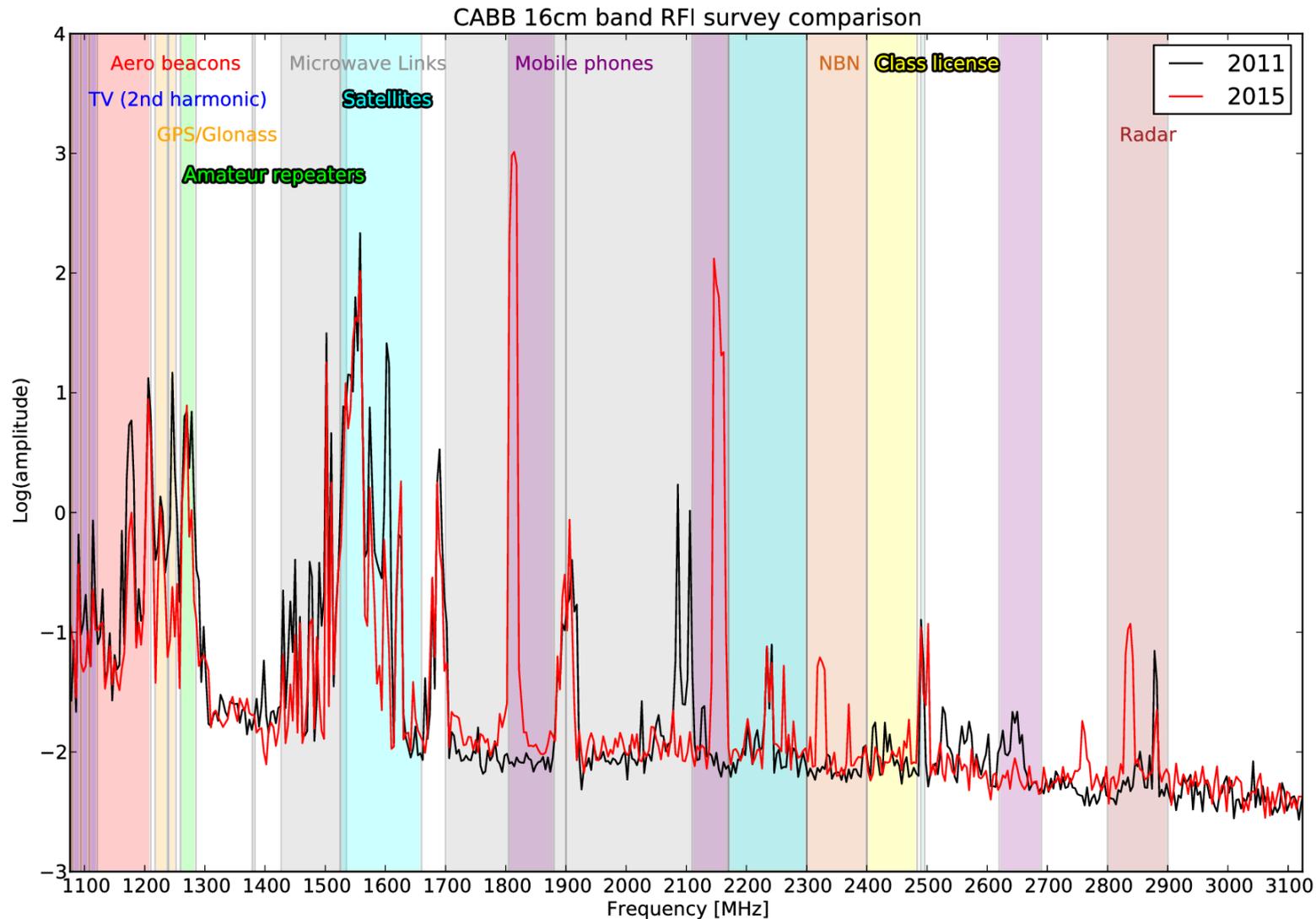


Very sensitive telescopes are limited by confusion rather than noise → need **better resolution**

# Radio Frequency Interference (RFI)

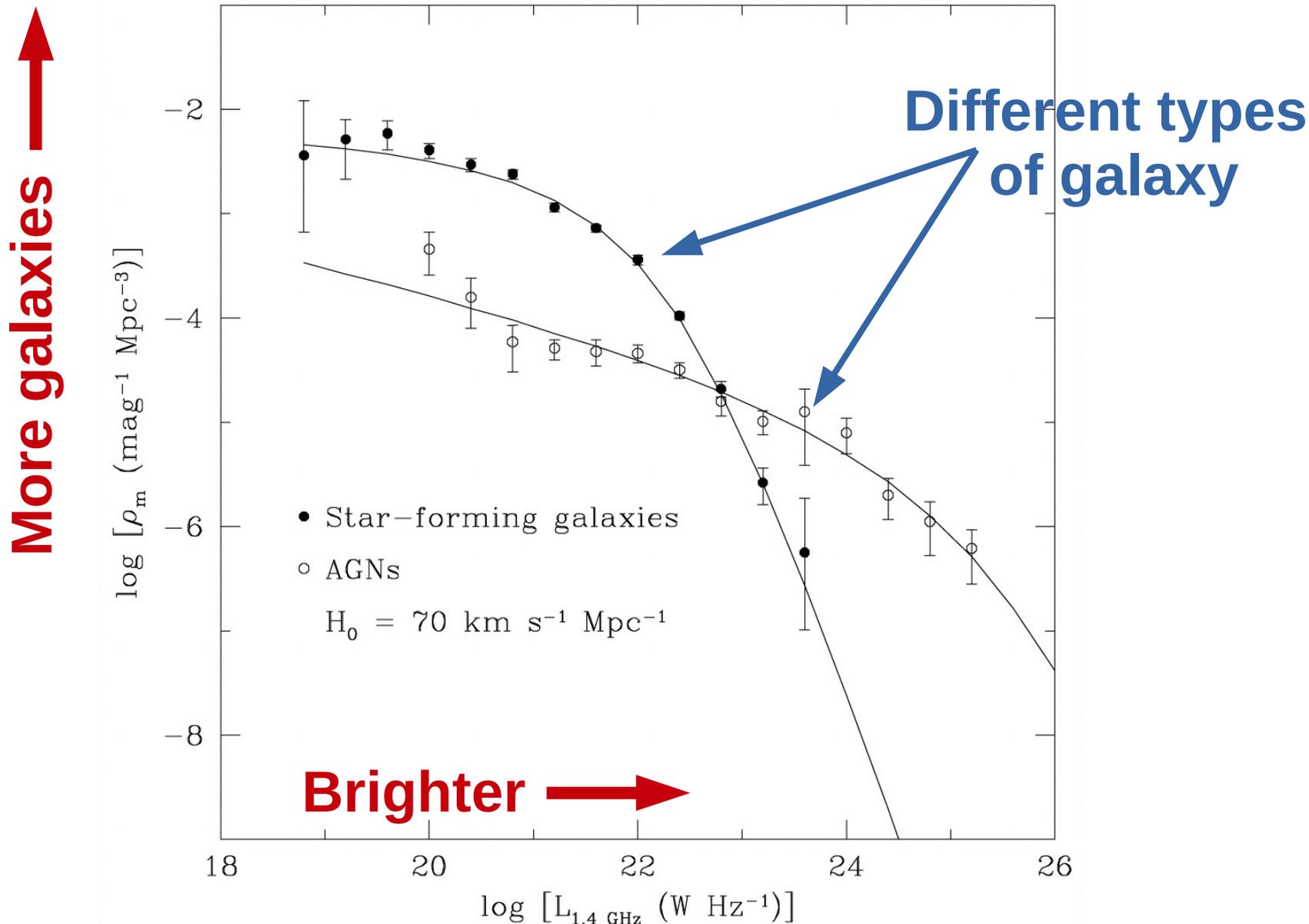
Humans cause a lot of pollution at radio frequencies!

→ Move to a “radio-quiet” site to reduce the RFI



# Galaxy number counts

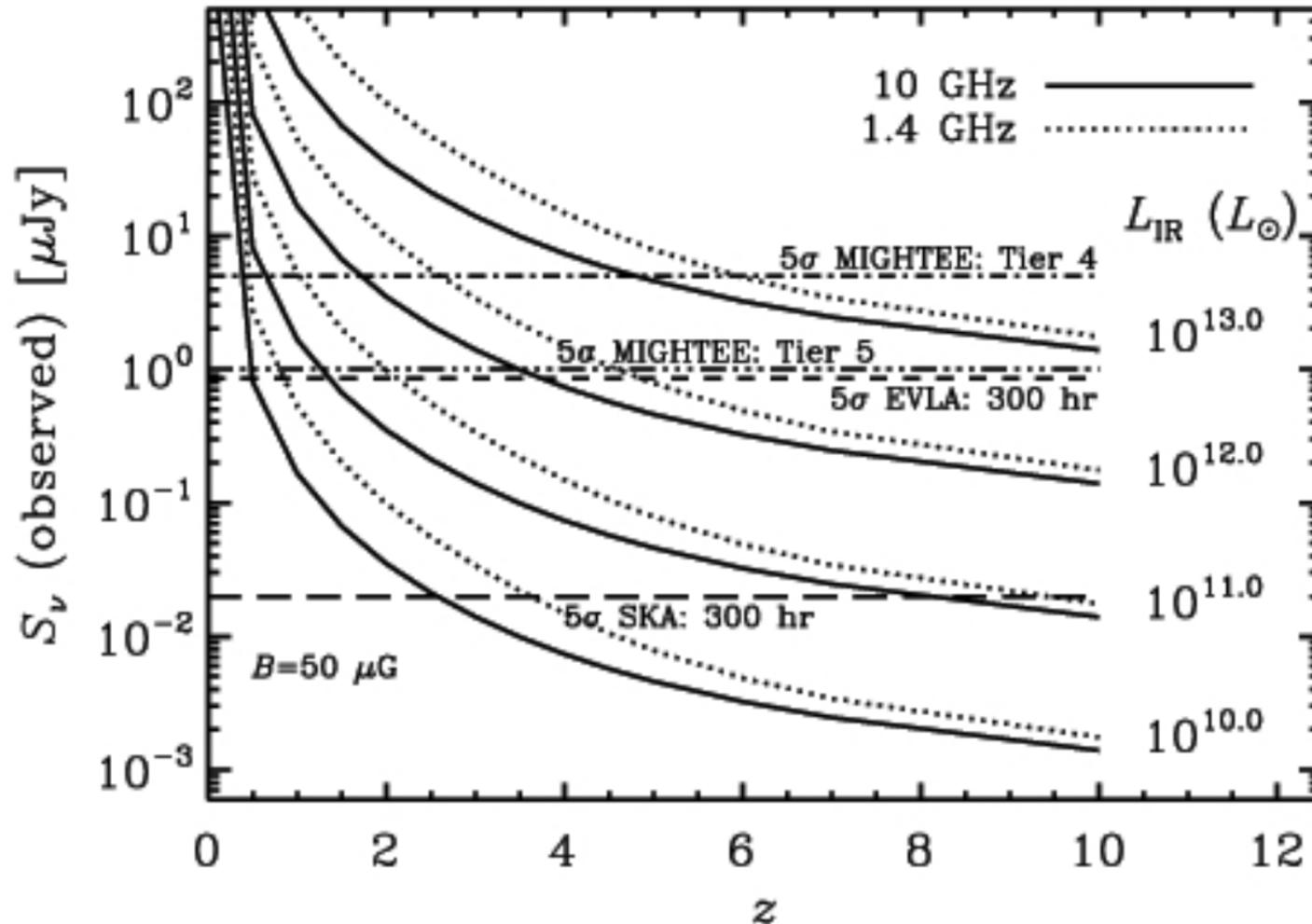
Number of galaxies vs. their intrinsic luminosity



# Number counts vs. redshift

- Distant sources are fainter
- Source populations evolve with redshift
- Luminosity depends on frequency (redshifted!)

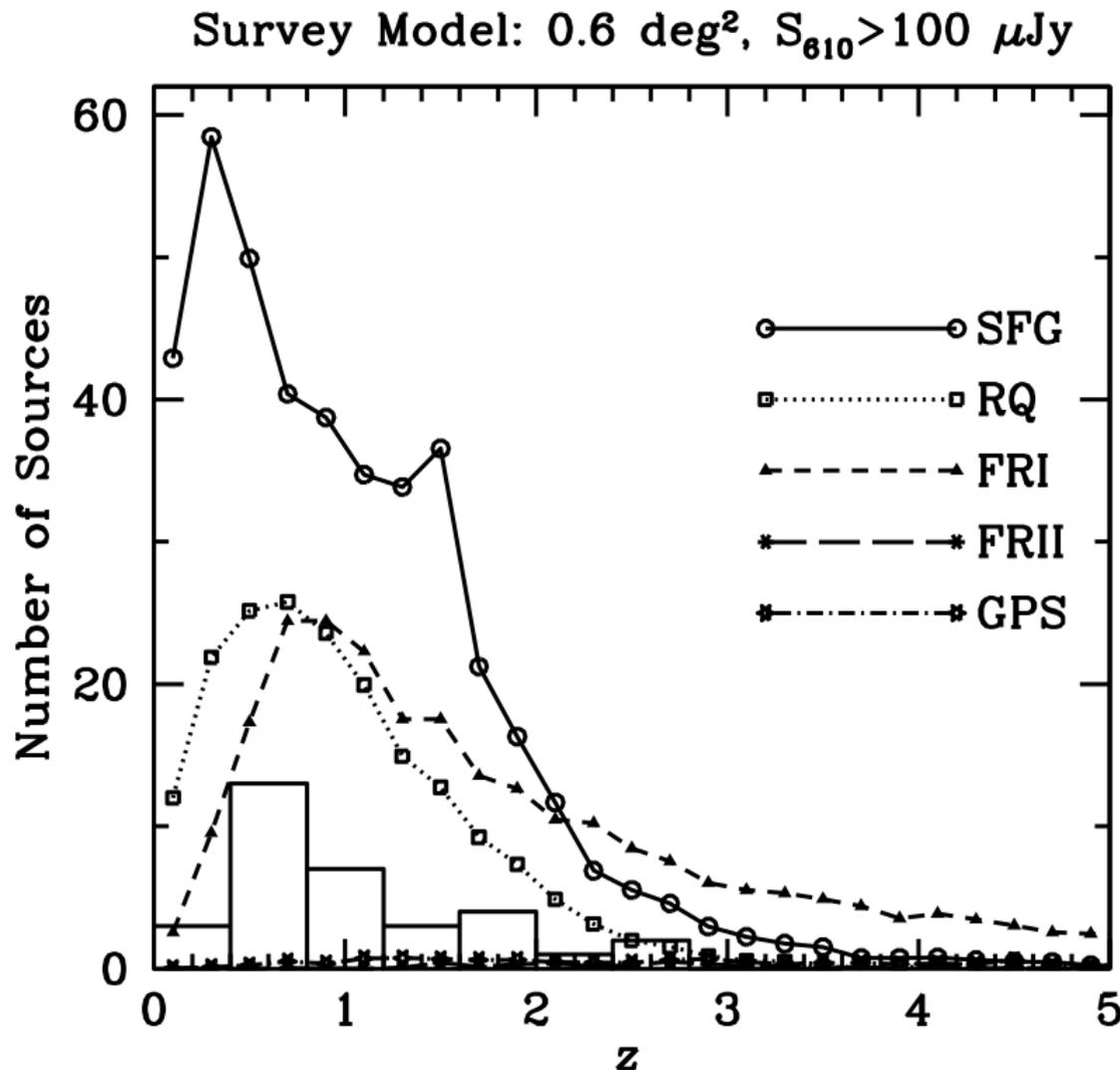
$$S = \frac{L}{4\pi d_L^2}$$



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# Radio interferometry: Basics

# Two-element interferometer

Plane wave enters each receiver *with a phase/delay* that depends on their separation:

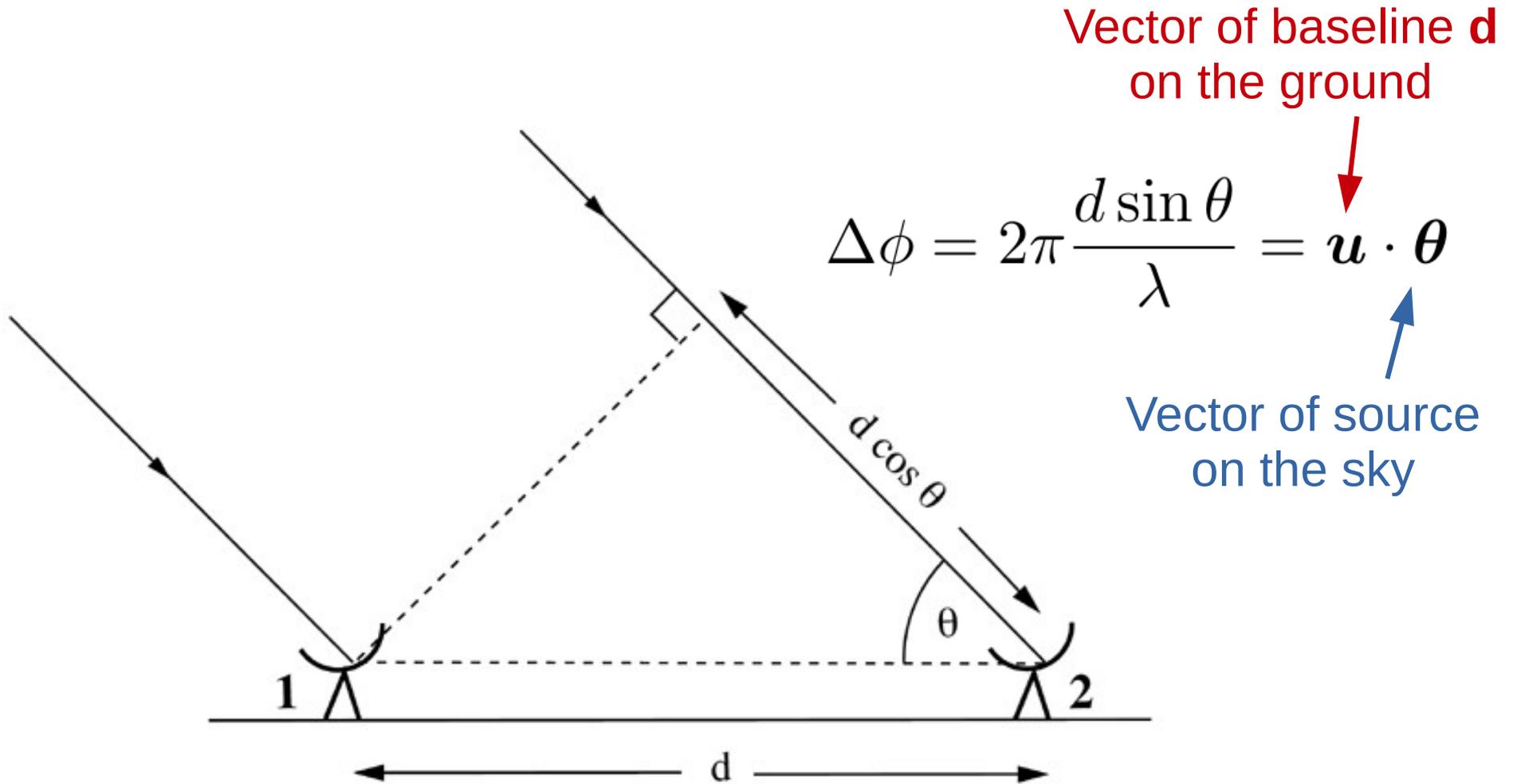


Fig 5.11 'Galaxies in the Universe' Sparke/Gallagher CUP 2007

The electric field of the wave,  $E$ , induces a voltage in the receivers:

$$v_2(t) = \int_{-\pi}^{+\pi} A(\theta) E(\theta) e^{i\omega t} d\theta$$

$$v_1(t) = \int_{-\pi}^{+\pi} A(\theta) E(\theta) e^{i(\omega t + \Delta\phi)} d\theta$$

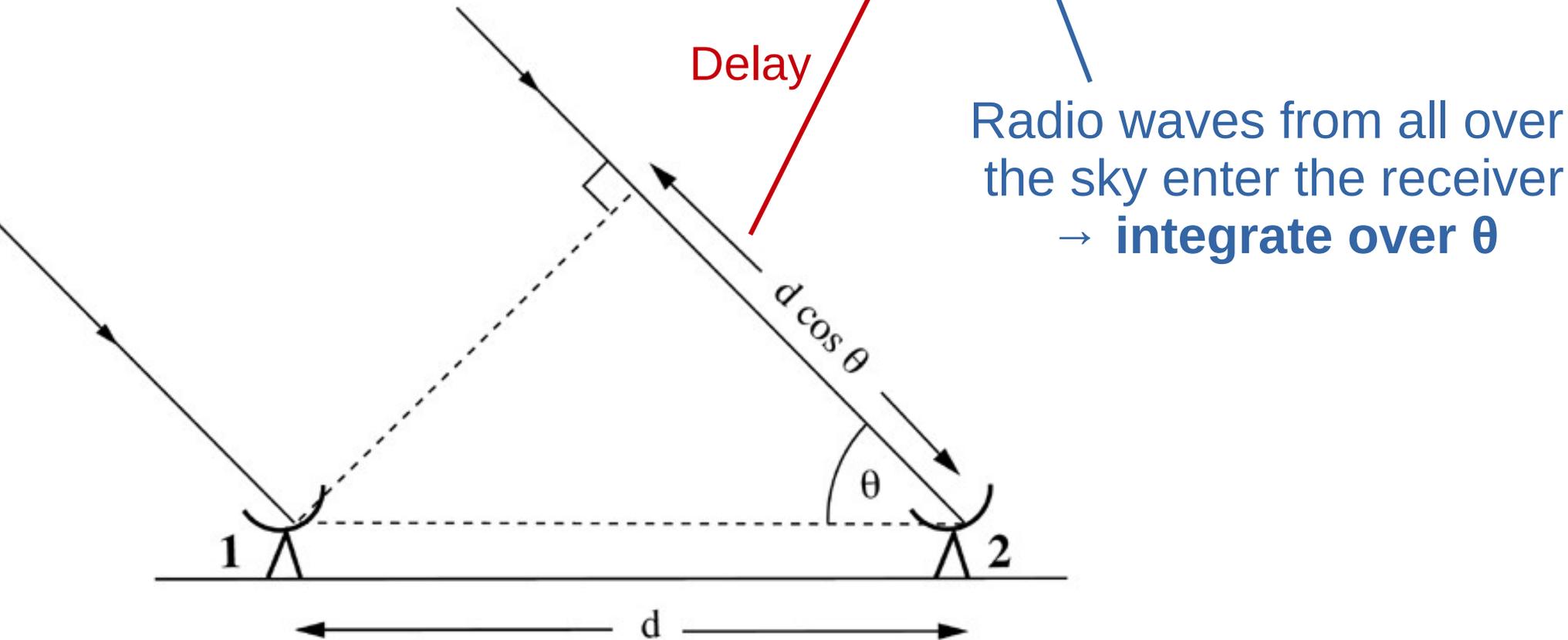


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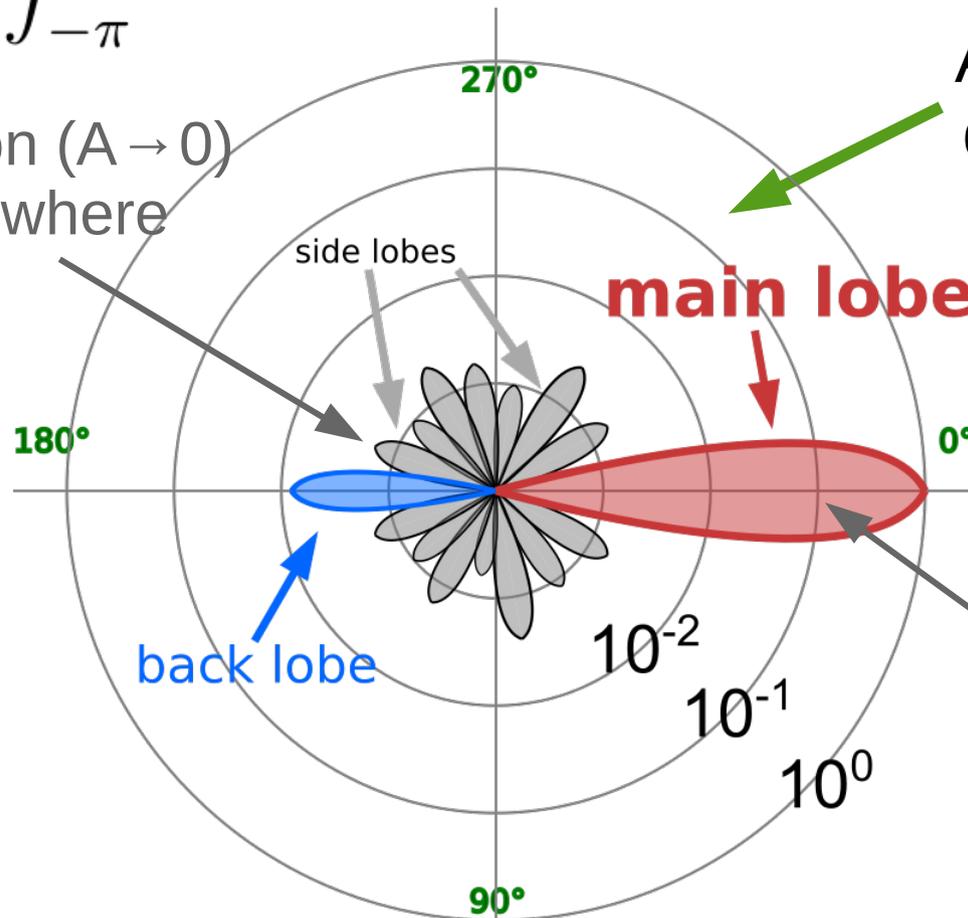
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The antenna pattern of each receiver,  $A(\theta)$ , *attenuates* the signal

Amount of attenuation depends on direction of the source

More attenuation ( $A \rightarrow 0$ ) if source is elsewhere



Less attenuation ( $A \sim 1$ ) if source is near the centre of the beam

Now multiply (*correlate*) the voltages from the two receivers and measure (*detect*) the resulting signal:

Correlation **multiplies** voltages and **averages** signal over time

<Averaging> – only **coherent** signals do not average-out

$$\langle v_1(t) \cdot v_2^*(t) \rangle = \left\langle \int_{-\pi}^{+\pi} A(\theta) E(\theta) e^{i\omega t} e^{i\mathbf{u} \cdot \boldsymbol{\theta}} d\theta \cdot \int_{-\pi}^{+\pi} A^*(\theta') E^*(\theta') e^{-i\omega t} d\theta' \right\rangle$$

Emission from different sources ( $\theta \neq \theta'$ ) is incoherent, so **averages to zero**

(Why doesn't the emission from a single incoherent source average out? – *van Cittert-Zernike theorem*)

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Define the **intensity distribution** on the sky and **primary beam**:

$$\begin{aligned}I(\theta) &= |E(\theta)|^2; & B(\theta) &= |A(\theta)|^2 \\ \tilde{I}(\theta) &\equiv B(\theta)I(\theta) = \int_{-\infty}^{+\infty} \tilde{I}(\mathbf{k}) e^{i\mathbf{k} \cdot \boldsymbol{\theta}} d\mathbf{k}\end{aligned}$$

Now multiply (*correlate*) the voltages from the two receivers and measure (*detect*) the resulting signal:

Correlation **multiplies** voltages and **averages** signal over time

**<Averaging>** – only **coherent** signals do not average-out

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→ Interferometers measure Fourier modes on the sky

Measured mode depends on baseline length and wavelength,  
 $\mathbf{u} = \mathbf{d} / \lambda$

# Key points: Interferometers

Interferometers measure the *averaged product* of voltages from 2 receivers with *different phase delays*

→ **Phase delay depends on array geometry (baseline length)**

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Interferometers measure the *averaged product* of voltages from 2 receivers with *different phase delays*

→ **Phase delay depends on array geometry (baseline length)**

The voltages are a function of the *intensity over the whole sky*, attenuated by an *antenna pattern*

→ **Interferometers see the whole sky** (weighted by a beam)

*Fourier modes* of the intensity distribution with wavenumber  $u = d / \lambda$  (matching the phase delay) interfere *constructively*

→ **Each baseline measures a single Fourier mode** of the (antenna-weighted) intensity on the whole sky

# Complications...

## Phase delay depends on wavelength

$$\Delta\phi = 2\pi \frac{d \sin \theta}{\lambda}$$

- Interferometer response is *chromatic*
- Measure *different Fourier modes* at different frequencies!
- Averaging over frequency (bandwidth) therefore averages over Fourier modes
- Signal is *smearred out* by averaging

# Complications...

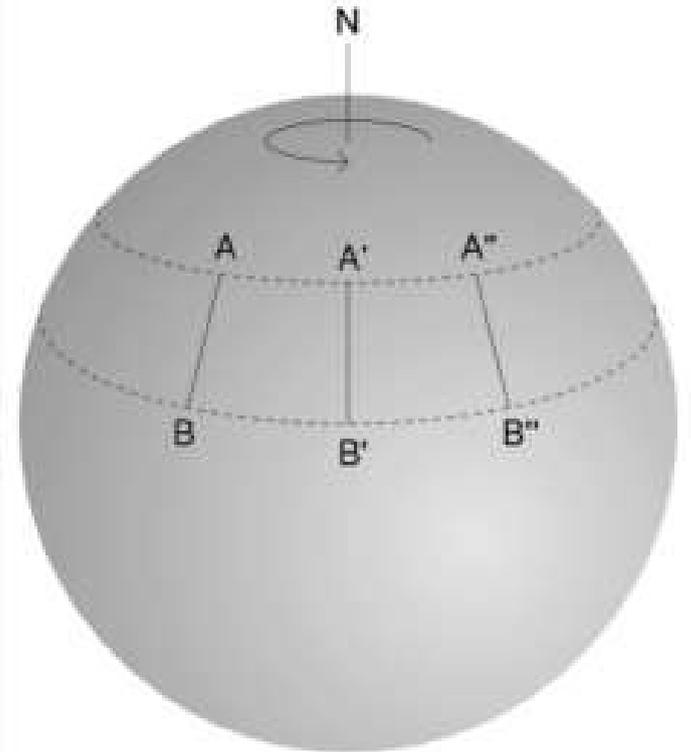
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## Earth rotation

- Baselines are aligned with different directions on the sky at different times of day
- Measure *different Fourier modes* as the Earth rotates



# Complications...

## **Mode-mixing due to the primary beam**

- Interferometers see intensity *modulated by primary beam*
- Primary beam breaks orthogonality → *mixing* of Fourier modes on the sky

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- The sky is curved; we should use **spherical harmonic** basis (Fourier basis is not orthonormal on the sky)
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## Further reading (advanced):

- T. Bastian, *Radio interferometry notes* [<https://is.gd/PmsBR8>]
- Parsons et al. 2012, *Delay transform* [arXiv:1204.4749]
- Shaw et al. 2014, *m-mode analysis* [1401.2095]
- Cornwell, Holdaway & Uson 1993, *Radio interferometric imaging of very large objects*

# Aperture synthesis

# Two receivers → many receivers

2 receivers = 1 baseline = 1 Fourier mode

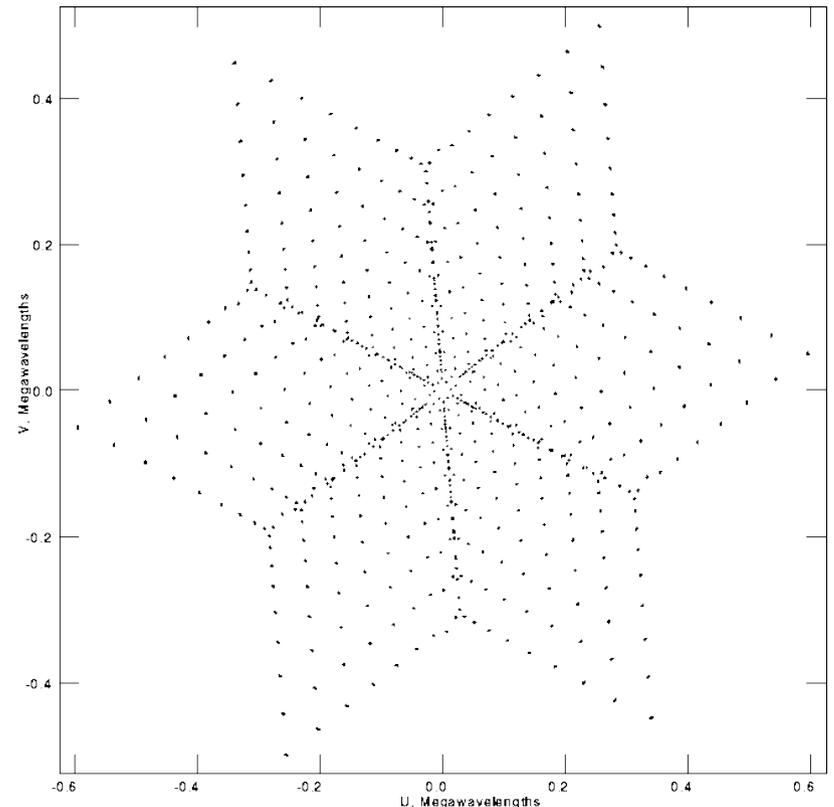
$N$  receivers =  $N(N-1)/2$  baselines

Correlate all the receivers → get more Fourier modes  
in one “snapshot”

Baselines can point in different directions → **2D** Fourier plane



VLA / NRAO



# Array layout: placing the receivers

**Recall:** Length of baseline,  $d \propto$  Fourier wavenumber,  $\mathbf{u}$

- Short baselines = small  $\mathbf{u}$  = large scales
- Long baselines = high resolution

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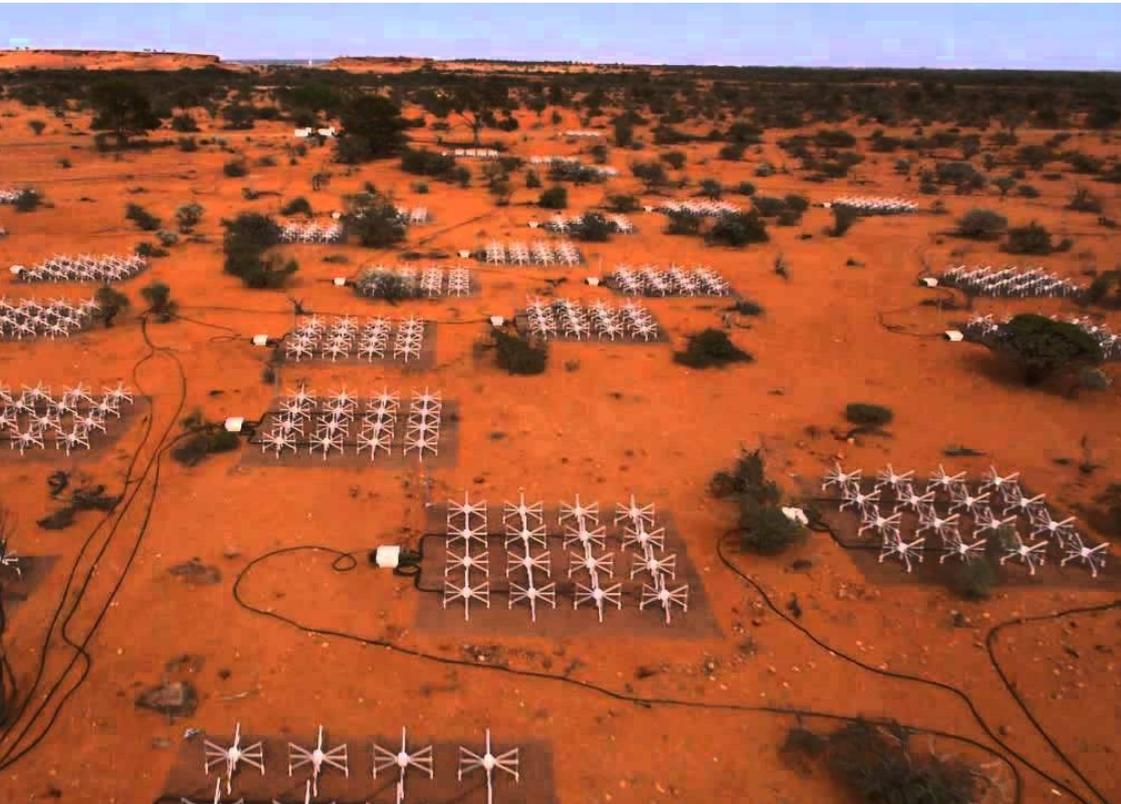
**Optimise:** Where do you need most sensitivity?

- Small objects (e.g. jets)  $\rightarrow$  more long baselines (sparse array)
- Large scales  $\rightarrow$  more short baselines (dense array)
- Detect galaxies  $\rightarrow$  balanced baseline distribution

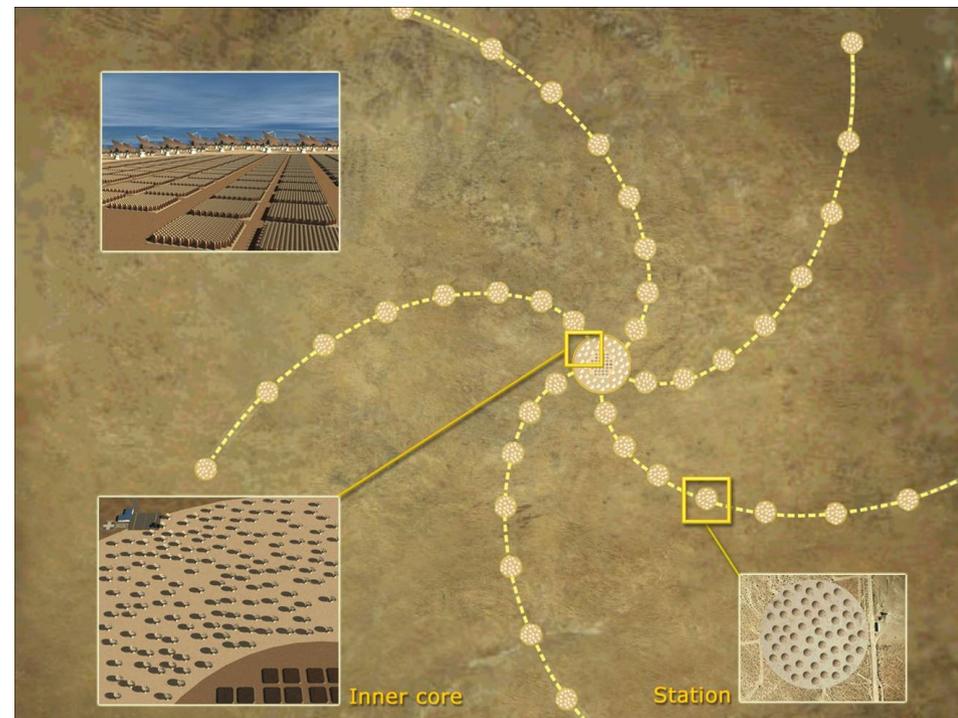
**Sparse array**  
e.g. JIVE/EVN



**Dense array**  
e.g. MWA



**Balanced array**  
e.g. SKA-MID



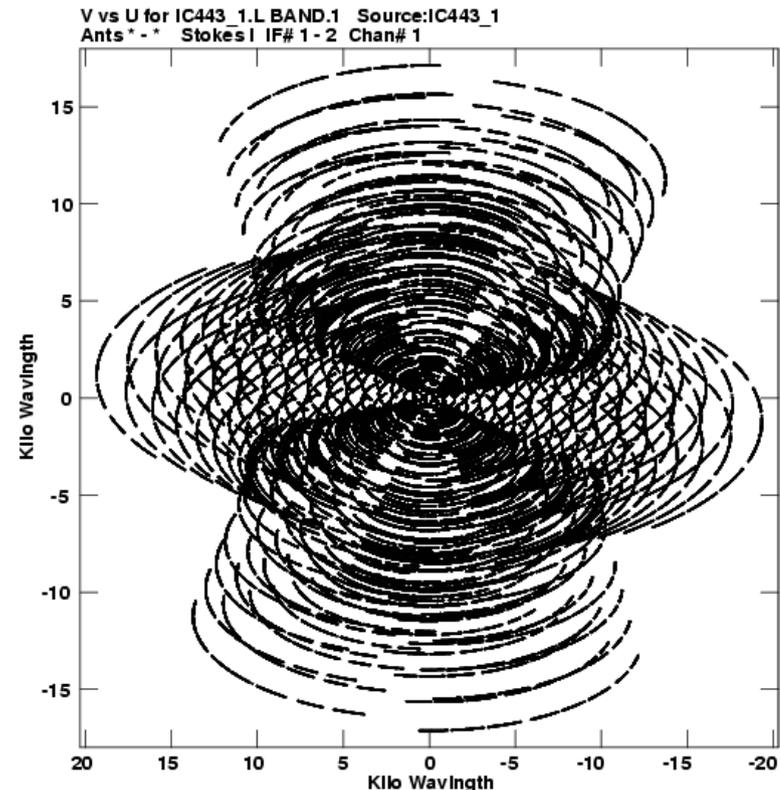
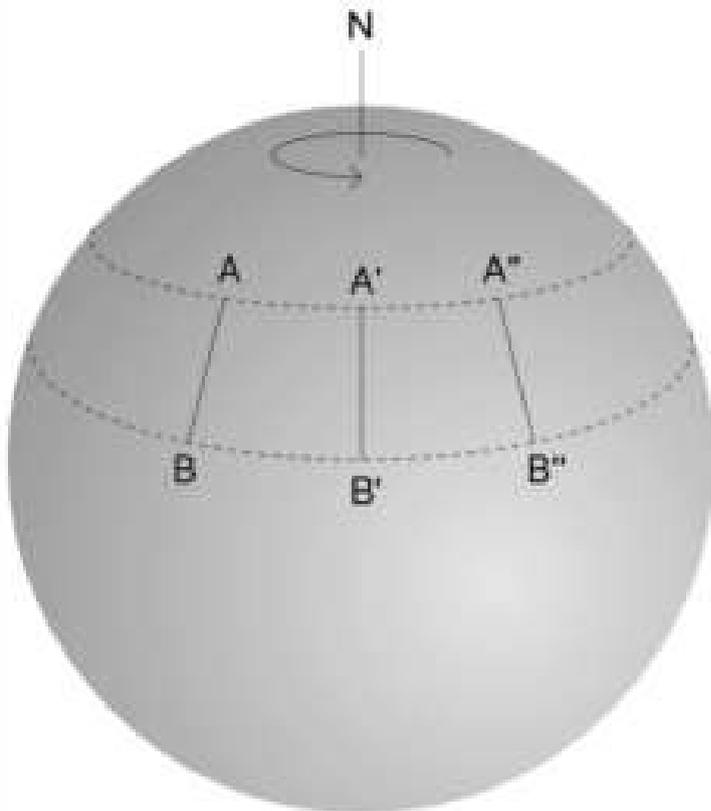
# Earth rotation

As the Earth rotates, the baseline vectors **rotate** with respect to the sky → sample different Fourier modes at different times

Represent baselines in the **uv** (Fourier) plane

→ Each baseline traces a curve in the uv plane over time

Get more Fourier modes just by waiting...



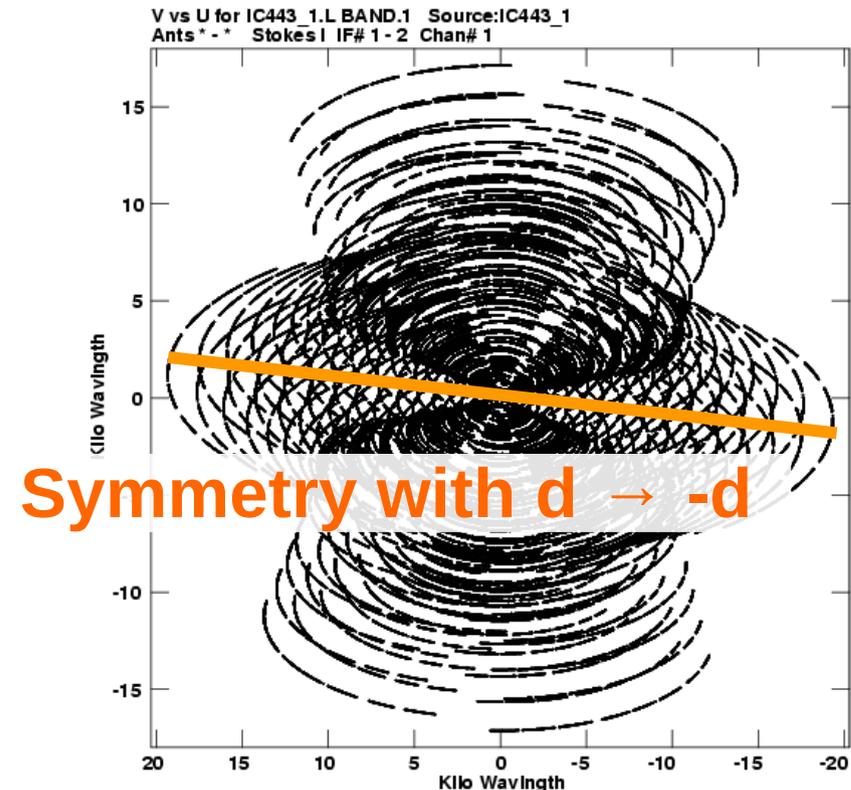
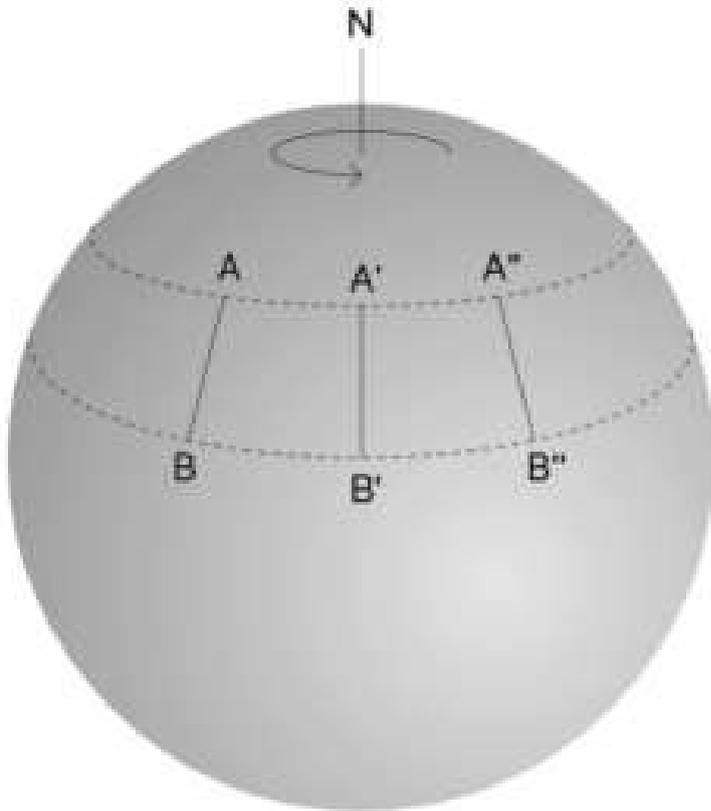
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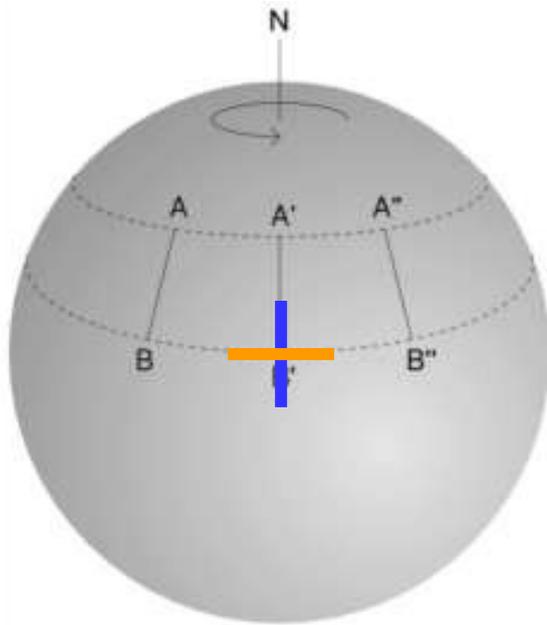


Symmetry with  $d \rightarrow -d$

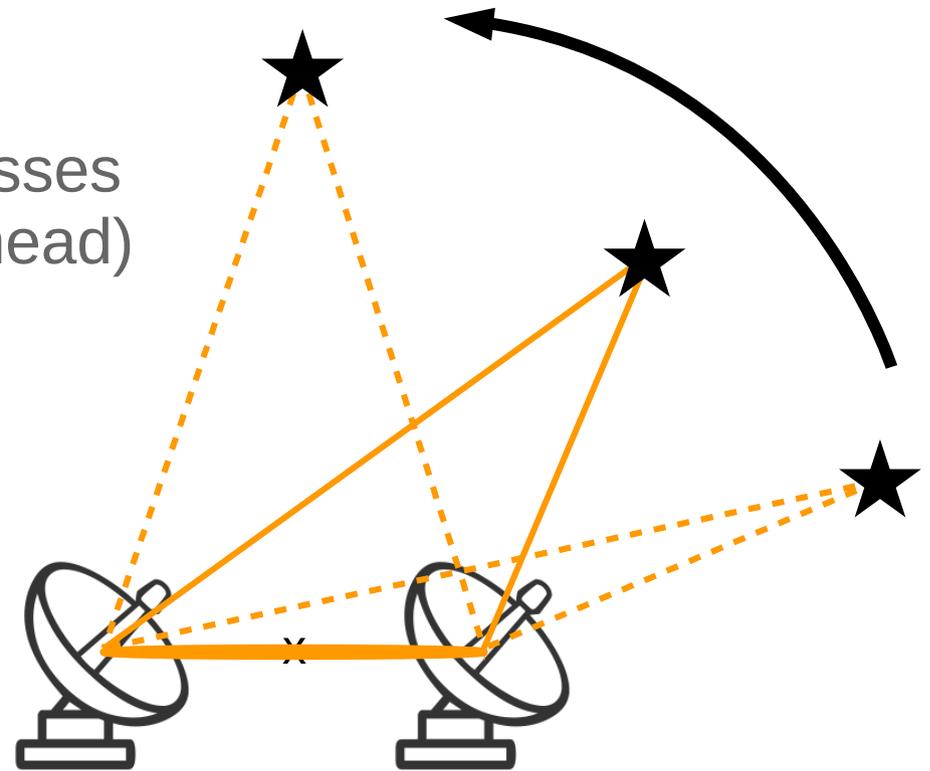
# Earth rotation

Also depends on **latitude** of array and angle of source

Baseline along the equator (east-west):  
 $|u|$  varies but  $v=0 \rightarrow$  **line** in the  $uv$  plane



(if source passes directly overhead)



Baseline across the equator (north-south):  
 $\rightarrow$  delay is always the same:  $u = \text{const.}$

# Earth rotation

Also depends on **latitude** of array and angle of source



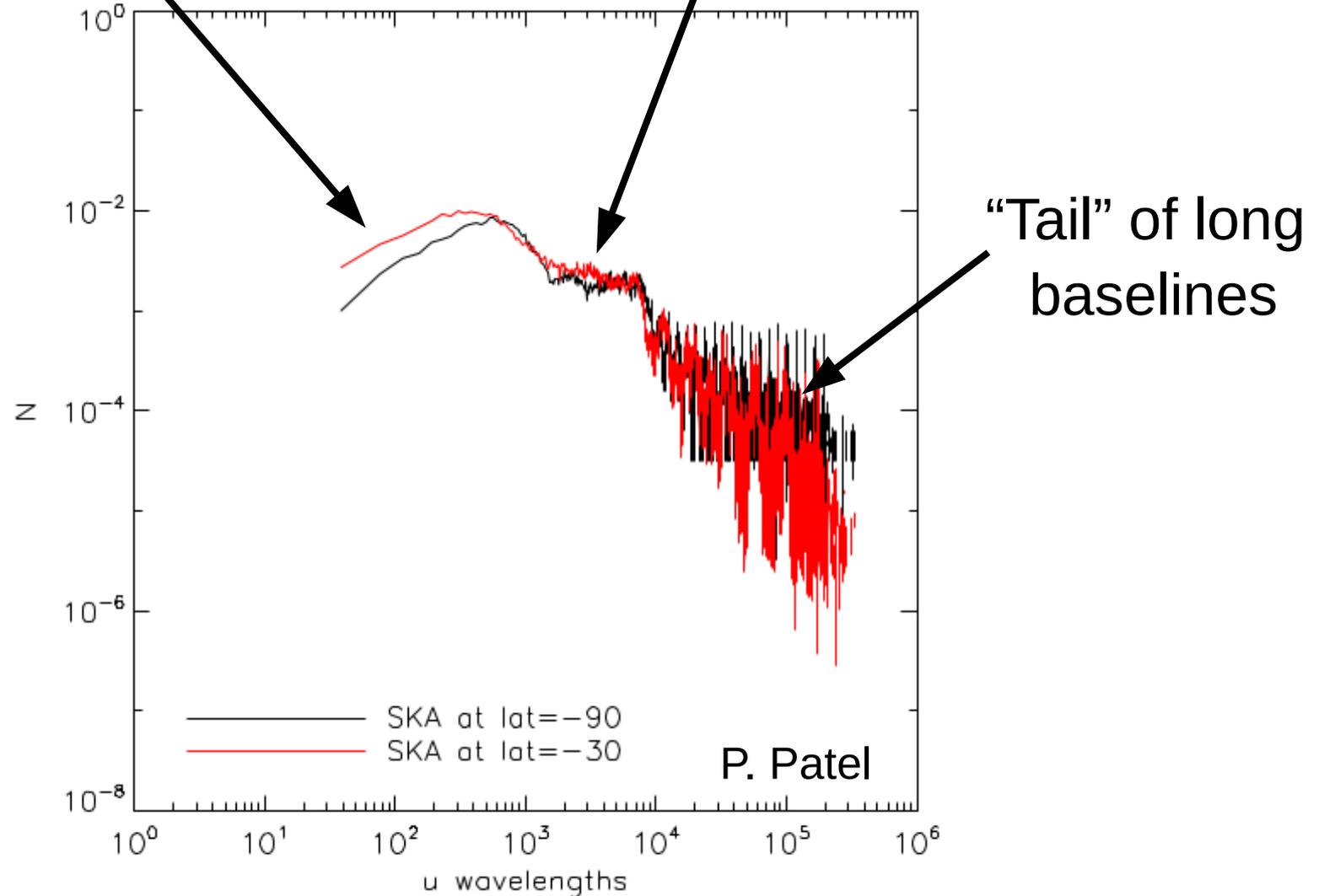
Teide Observatory (IAC)  
J.C. Casado

Tenerife ( $28.3^\circ$  N)

# SKA1-MID *average* baseline density

Many short baselines  
(dense core)

Plateau of intermediate  
baselines (“spiral arms”)

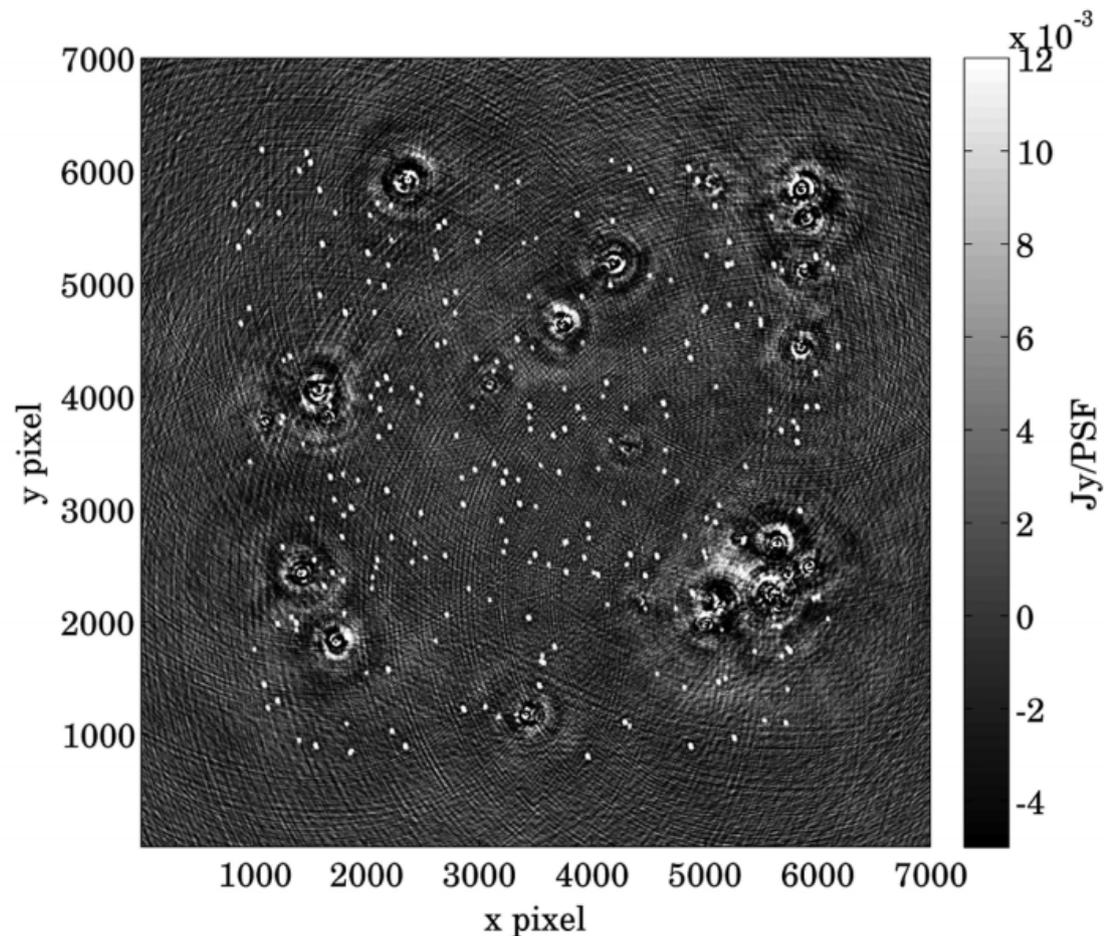


**Averaged** over rings in  $uv$ ,  $|u| = \text{const.}$

# Missing baselines and weighting

Measured visibilities = Fourier coefficients

- Inverse FT to reconstruct the intensity distribution,  $I(\theta)$
- But some baselines are always missing...



# Missing baselines and weighting

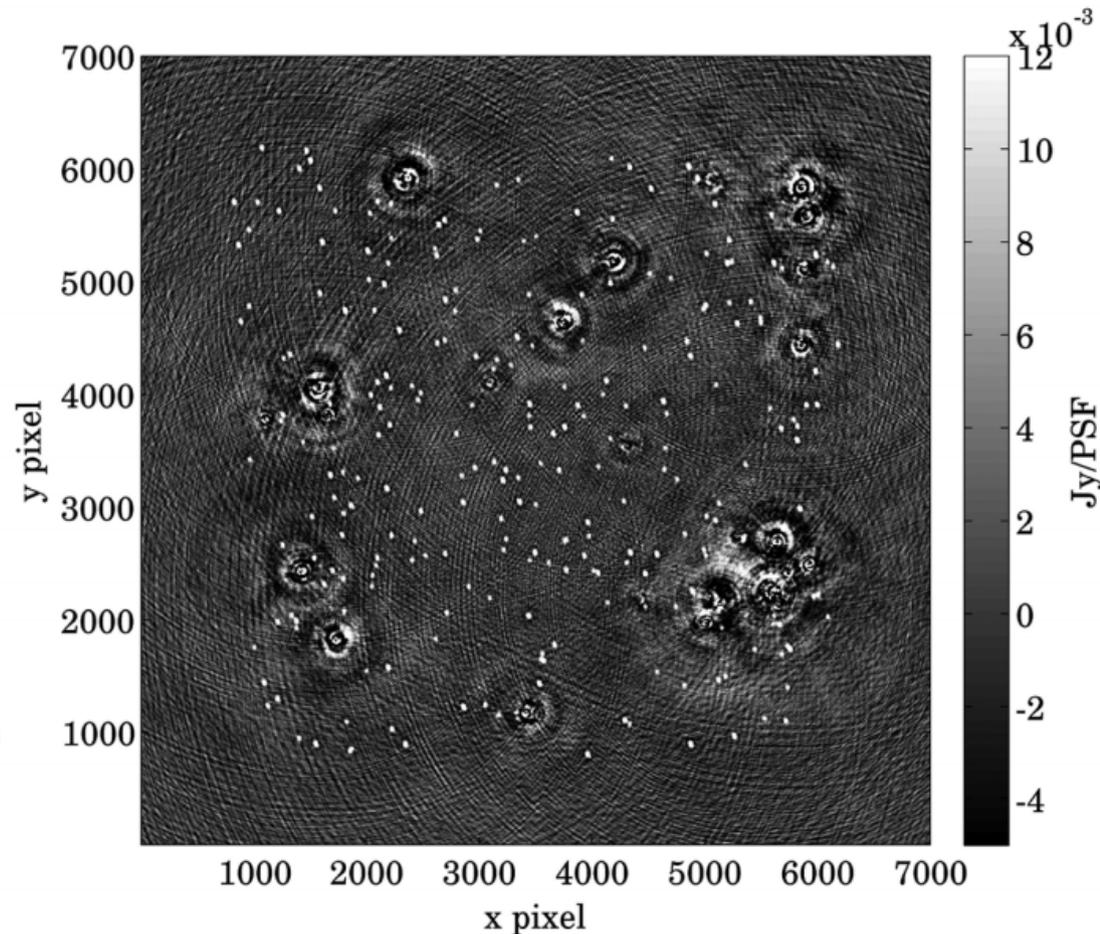
Measured visibilities = Fourier coefficients

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Problem when measuring **flux**: when baselines are missing, some flux is not counted!

Some baselines are poorly sampled: high noise

Primary beam sidelobes also add extra structure to image



# Deconvolution

Remove the primary beam by “dividing it out”

$$\langle v_1(t) \cdot v_2^*(t) \rangle = \int_{-\pi}^{+\pi} |A(\theta)|^2 |E(\theta)|^2 e^{i\mathbf{u} \cdot \boldsymbol{\theta}} d\theta$$

Simple “CLEAN” method: for every peak in the image, divide by (scaled) primary beam, then multiply by delta-fn

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Simple “CLEAN” method: for every peak in the image, divide by (scaled) primary beam, then multiply by delta-fn

Bad for diffuse emission! Poorly modelled by delta-fns

(More advanced methods exist to properly weight by the noise etc.)

**Do you even need to make an image?**

Can do source detection, measure galaxy properties etc. directly, in Fourier (visibility) space

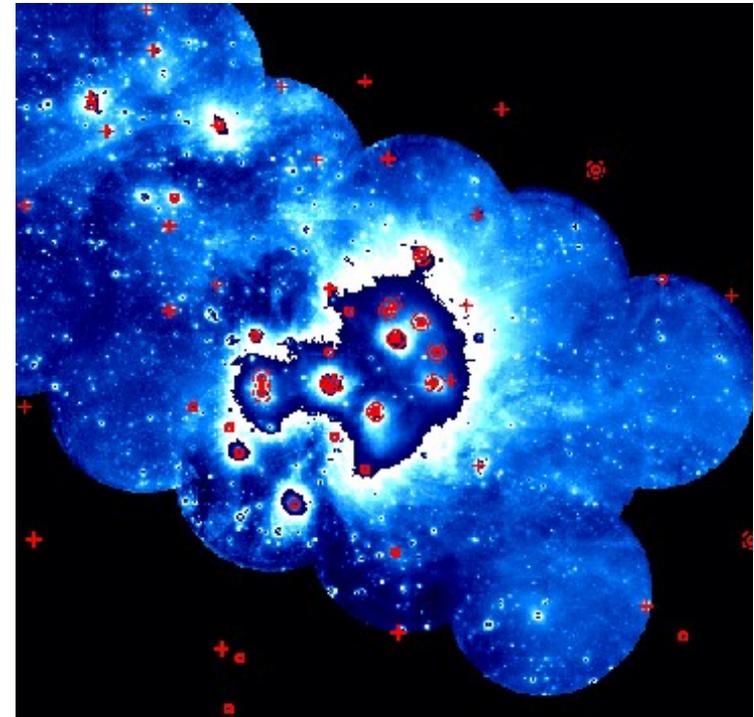
# Mosaicing

Each image is restricted to the primary beam field of view  
i.e. a single “pointing”

To make a map, many pointings must be stitched together

**Recall:** interferometers can't measure Fourier modes  
corresponding to scales larger than the **shortest** baseline  
(and we normally have  $\text{FOV} = \lambda/D_{\text{dish}} > \lambda/D_{\text{min}}$ )

S. Gibson



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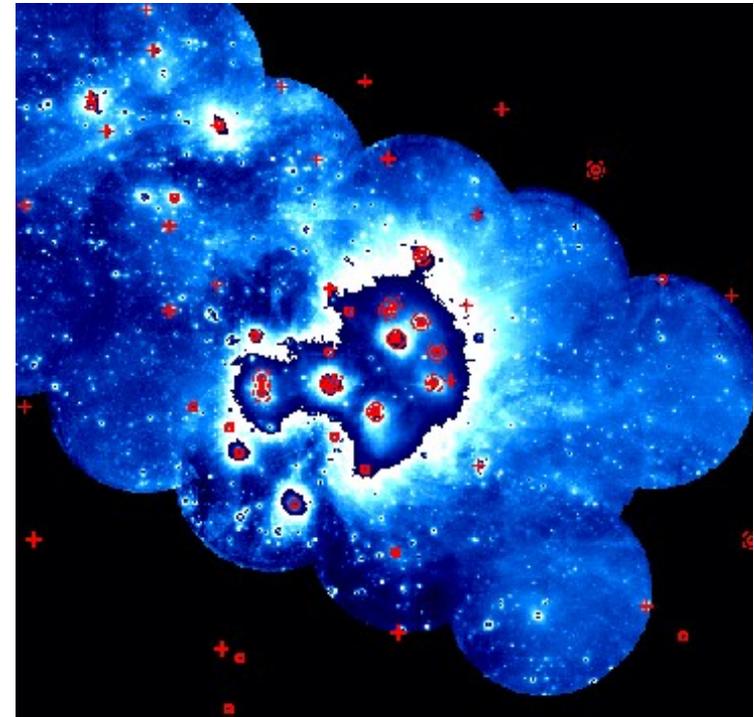
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S. Gibson

“Maps” are essentially “high-pass” filtered  
i.e. large scales are removed

Not a “true” image – **missing information**

- Can add autocorrelation info from single dishes to “fill in” large scales
- Not necessary for galaxy surveys (only care about counting objects)



# Physical sources of radio emission in galaxies

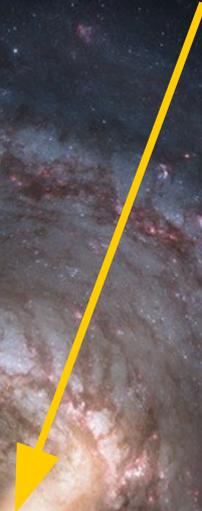


Nick Risinger / NASA (artistic impression)

**Star-forming  
regions**



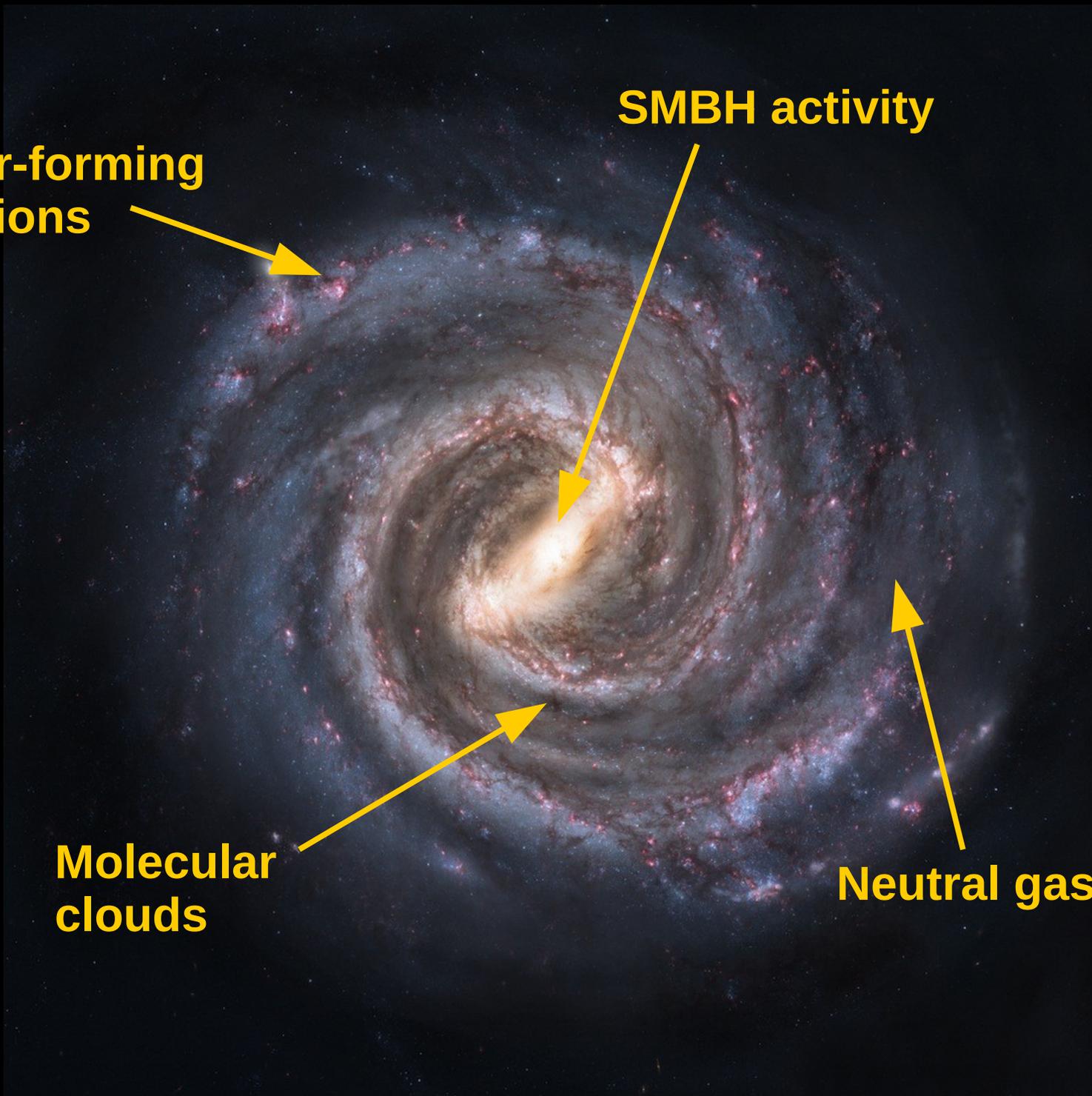
**SMBH activity**



**Molecular  
clouds**



**Neutral gas**



# Active Galactic Nuclei

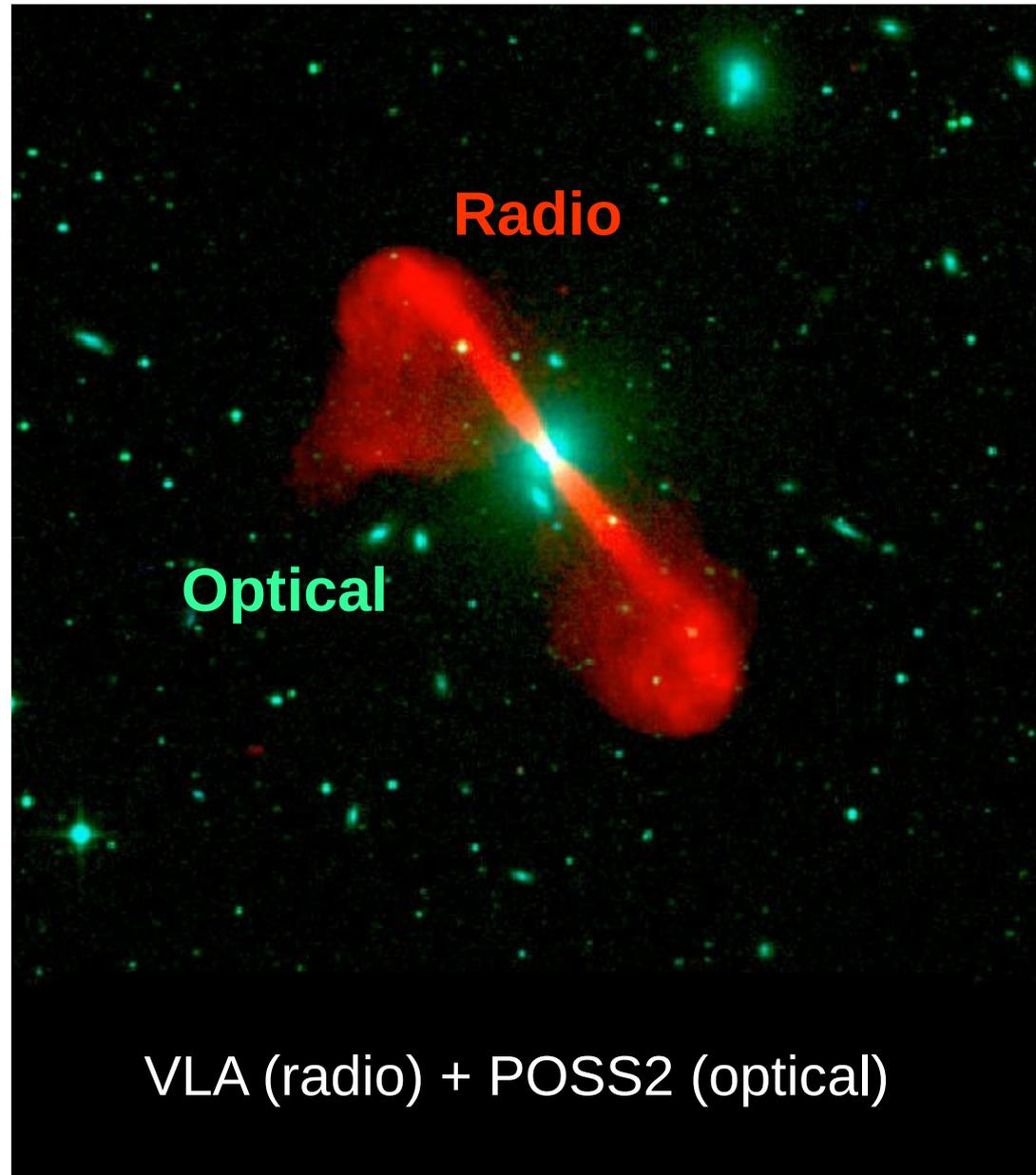
NRAO / AUI

Almost all galaxies have a **super-massive black hole** (SMBH) at the centre

Matter falls into SMBH → **accretion disk** forms outside

Friction releases extreme amounts of energy

Strong magnetic fields form



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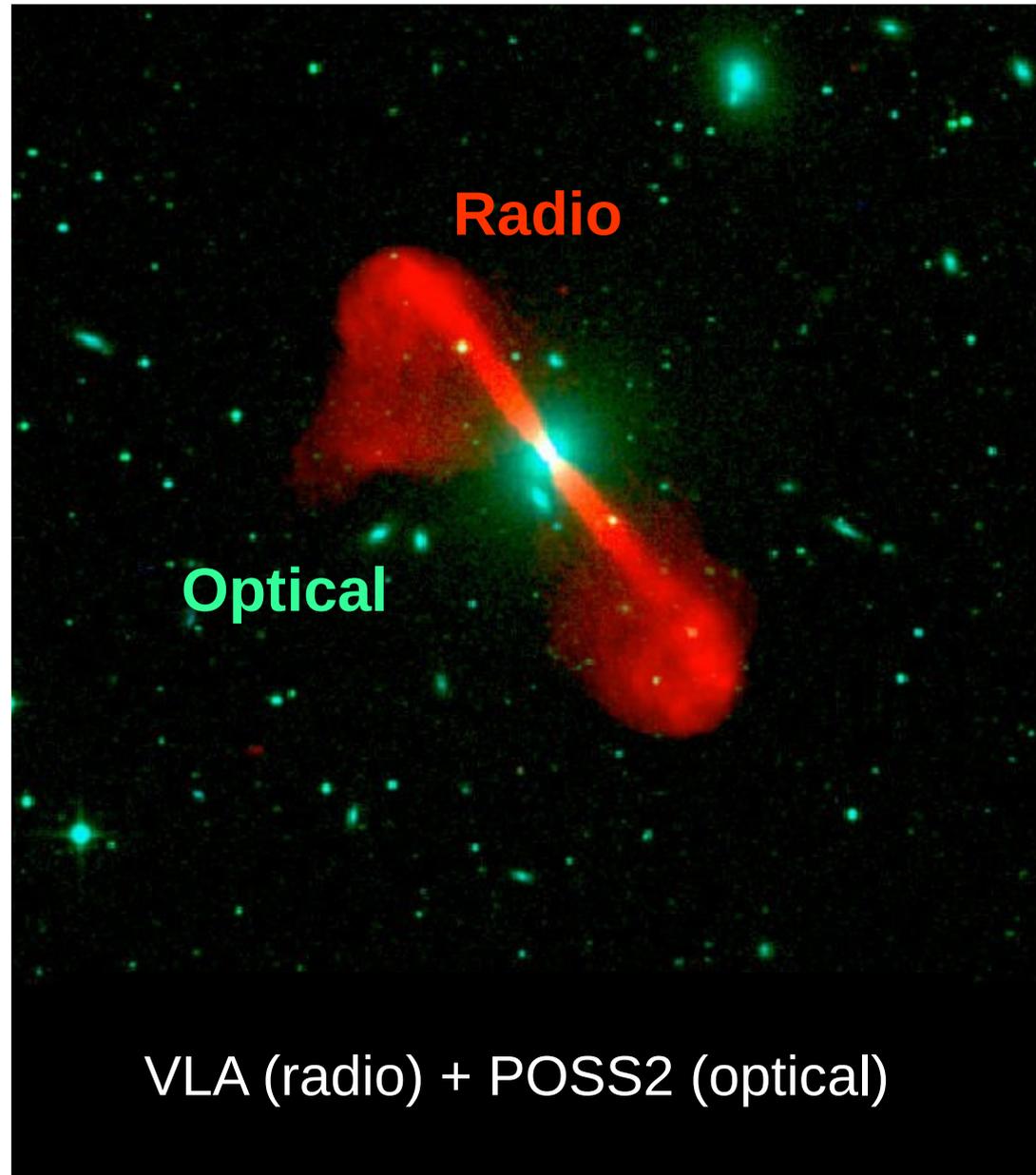
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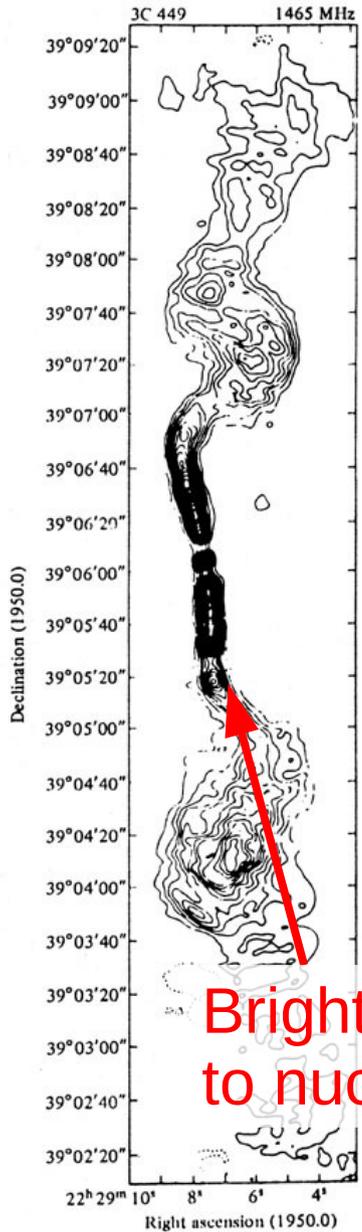
**Jet** of highly-accelerated charged particles is emitted along the SMBH spin axis

Very bright **synchrotron** emission from the jet



VLA (radio) + POSS2 (optical)

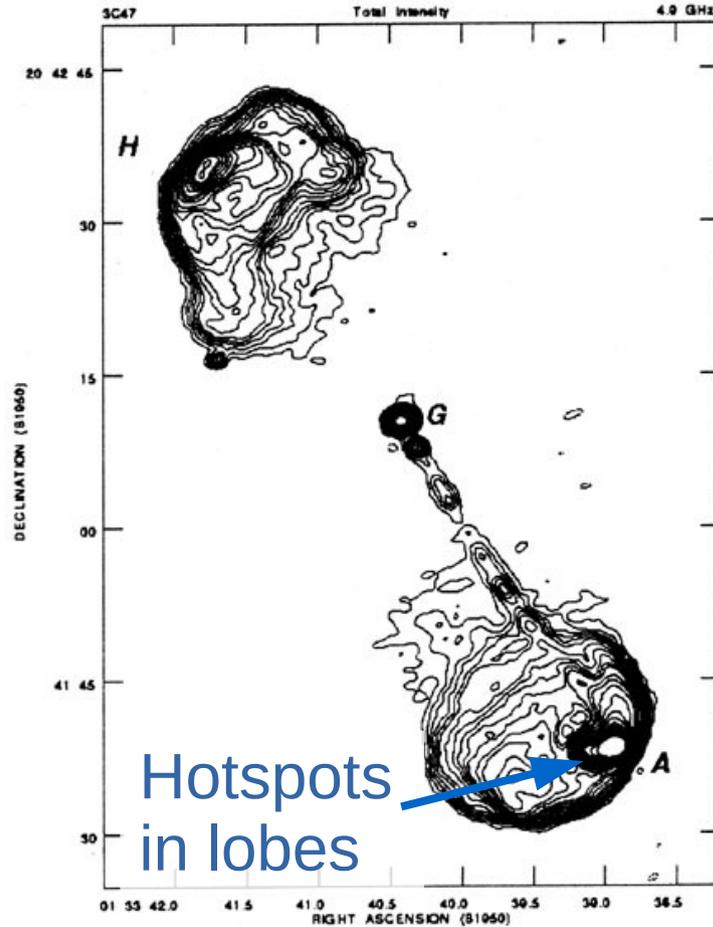
# FR-I



Brighter close to nucleus

Perley et al. 1979

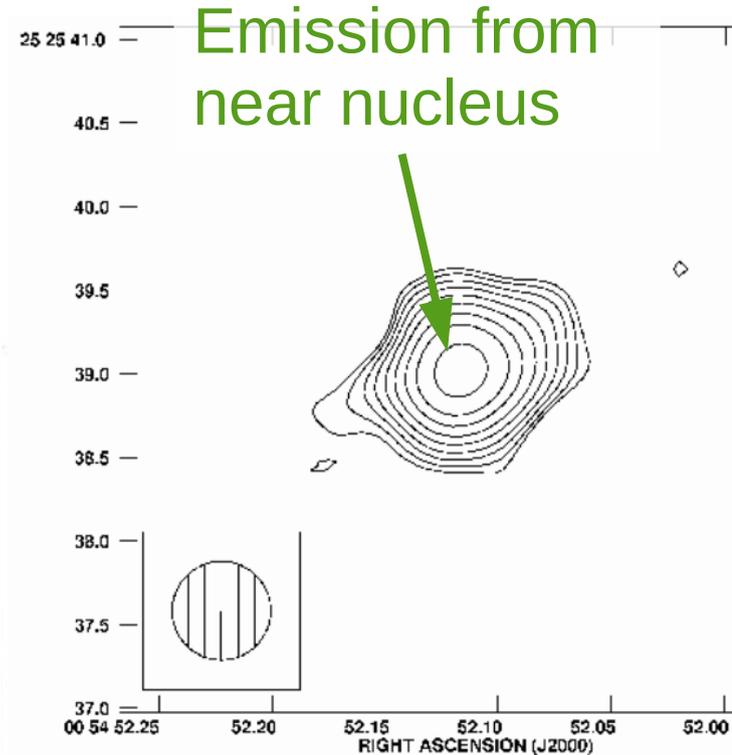
# FR-II



Hotspots in lobes

Bridle et al. 1994

# RQQ



Emission from near nucleus

Leipski et al. 2006

Most AGN are “radio-quiet”  
(but still emit in the radio)

# Star formation

Stars form when cold gas clouds **collapse** under gravity and heat up

Some fraction of **high-mass** (O,B) stars is formed

These burn fast and bright, ionising surrounding gas



# Star formation

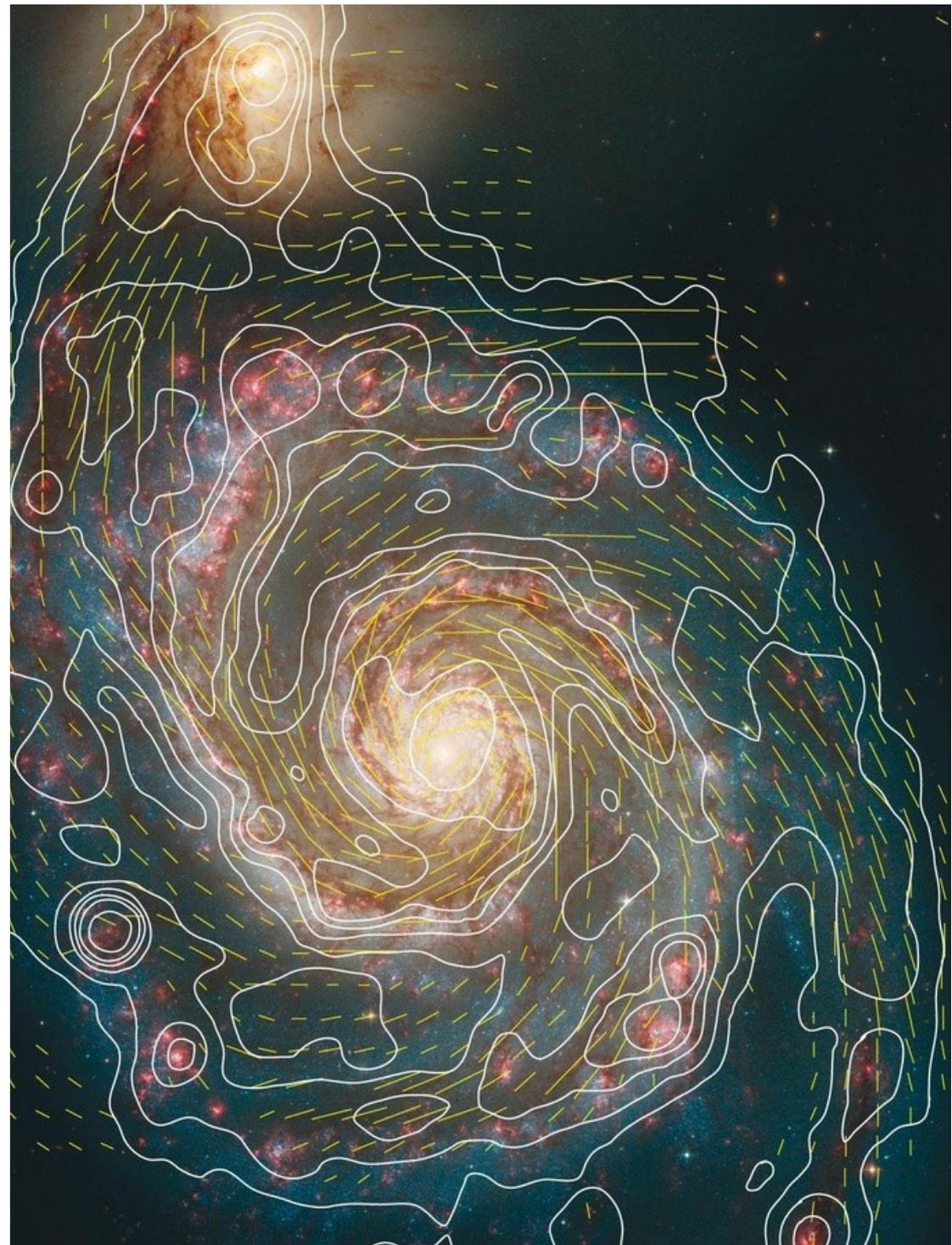
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They soon run out of fuel and explode → **supernova**

Supernova remnants: free electrons + magnetic fields → *synchrotron radiation*



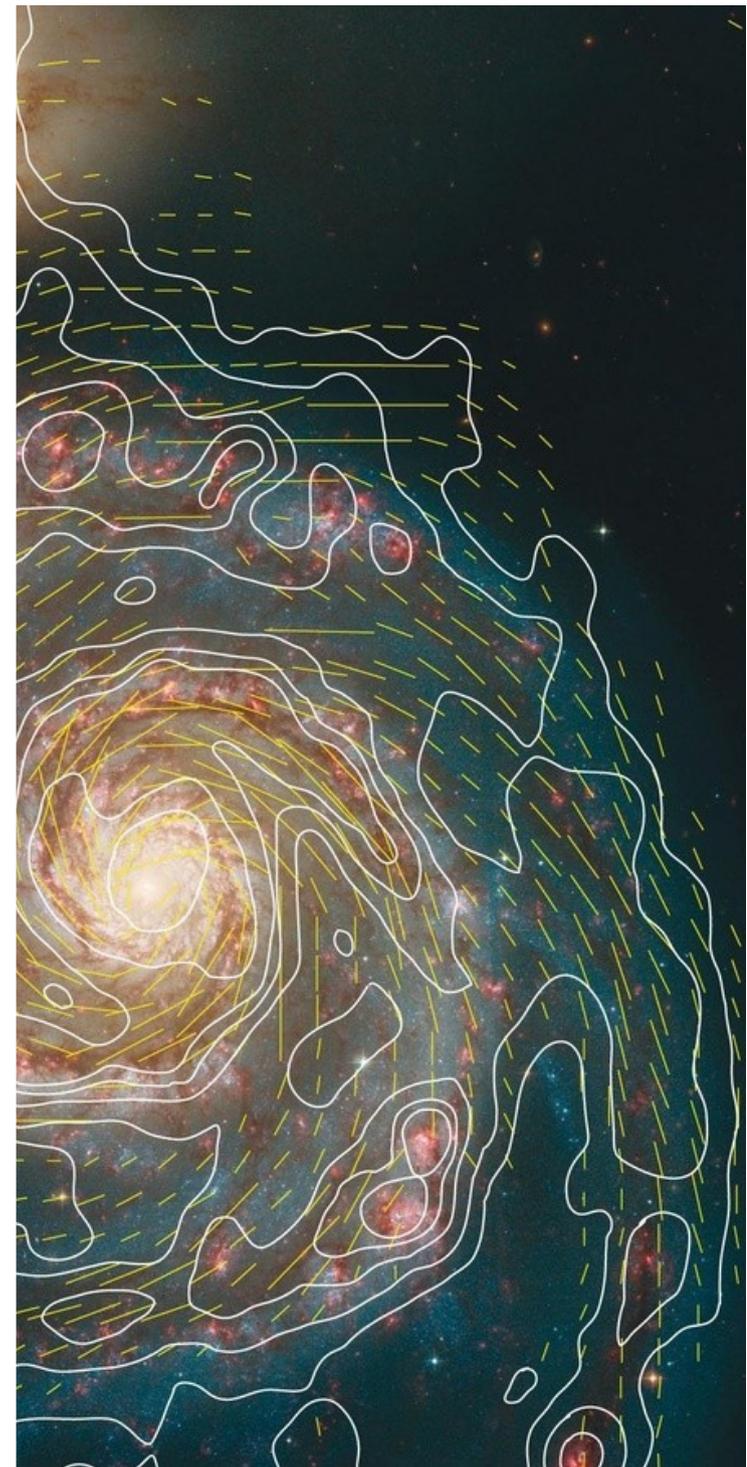
# Star formation

A strong correlation between radio and IR luminosity is observed

→ both are **tracers of star formation**

$$L_{1.4\text{ GHz}} = 4.324 \times 10^{29} \text{ erg/s} \frac{\psi_{\text{SFR}}}{M_{\odot} \text{ yr}^{-1}}$$

Rieke et al. 2009



VLA / HST / STScI

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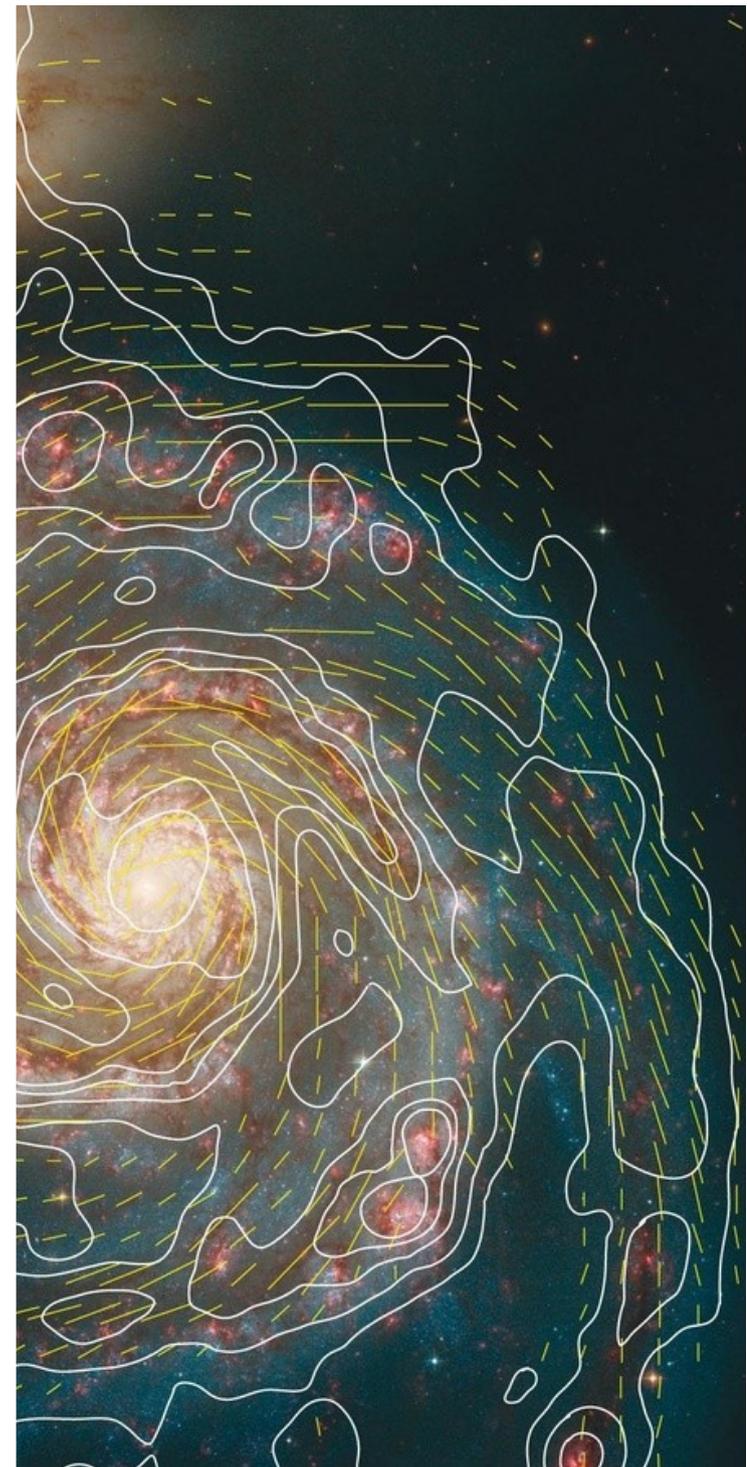
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Rieke et al. 2009

**Dust obscuration** is a big problem for other SFR indicators – but not radio

(N.B. Small fraction of free-free emission is also present – not pure synchrotron)

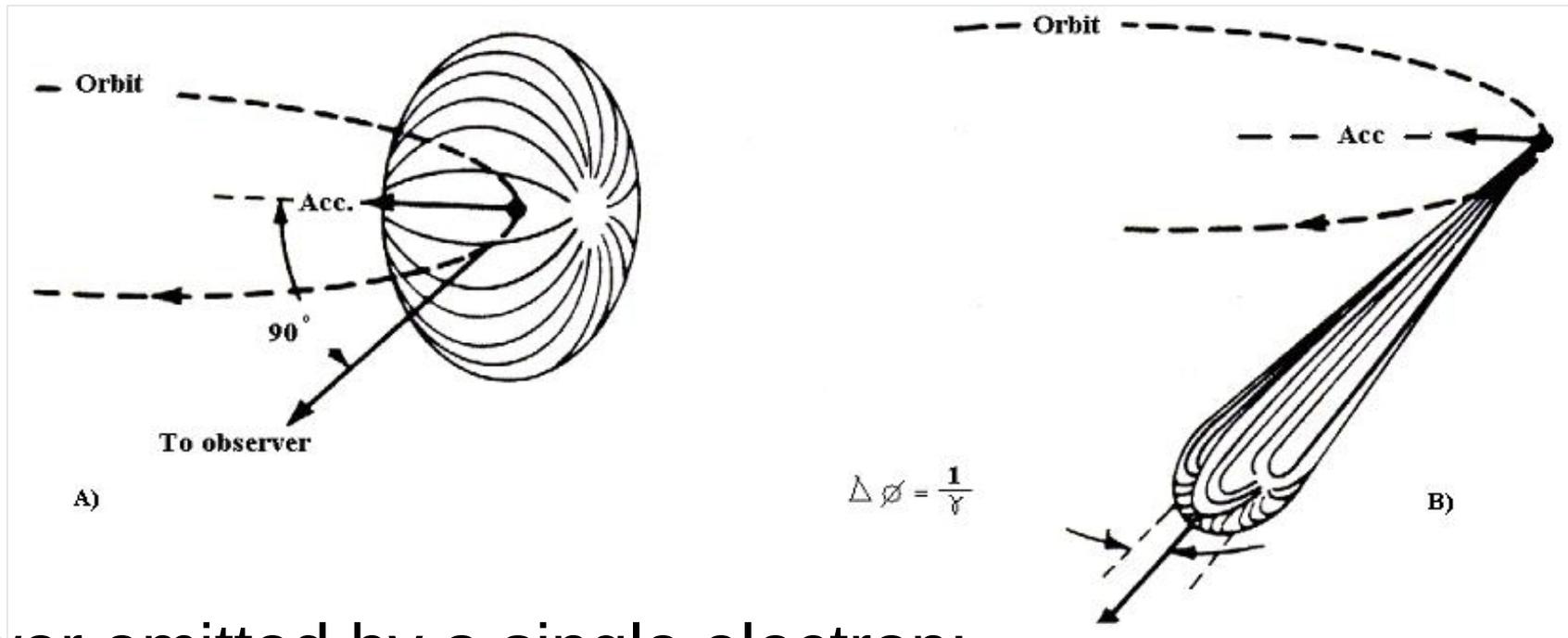


# Synchrotron radiation

Charged particles emit radiation when accelerated

Magnetic fields accelerate electrons → *cyclotron* radiation

Emission is **relativistically beamed** for high-energy electrons



Power emitted by a single electron:

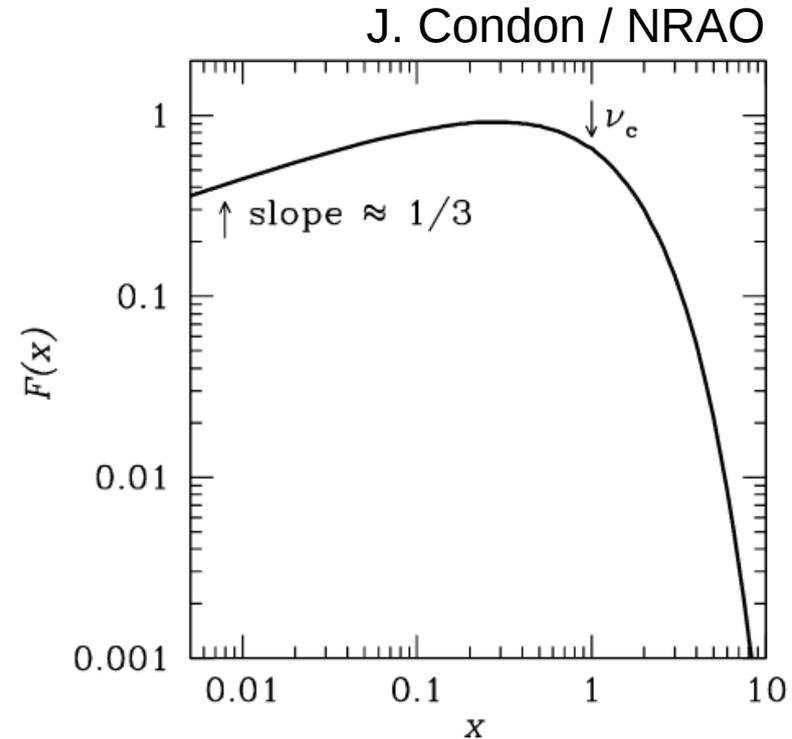
$$P = \left\langle \frac{dE}{dt} \right\rangle = \frac{4}{3} \sigma_T \beta^2 \gamma^2 \frac{cB^2}{8\pi}$$

# Synchrotron radiation

Emission frequency depends on the *boosted* gyro frequency

For a single electron:

$$\begin{aligned}\nu_{\text{crit}} &\simeq \gamma^2 \nu_g = \frac{\gamma^2}{2\pi} \frac{eB}{m_e c} \\ &\approx 17.6 \text{ GHz} \left( \frac{\gamma}{10^4} \right)^2 \left( \frac{B}{1 \text{ nT}} \right)\end{aligned}$$

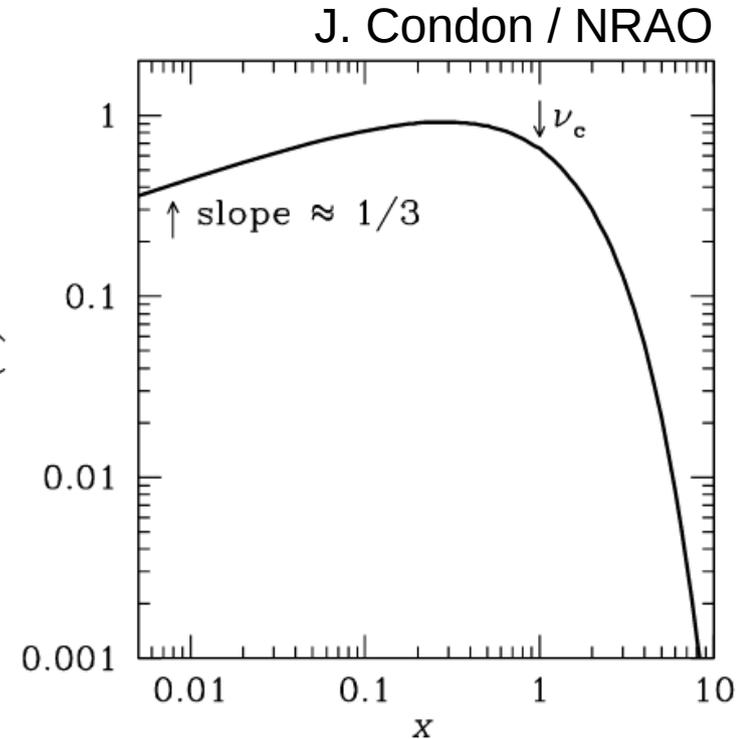


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## Electron energy distribution

Cosmic rays in the ISM have a power-law energy distribution

$$\frac{dN_e(E)}{dE dV} \propto E^{-\delta} \quad \delta \approx 2.4$$

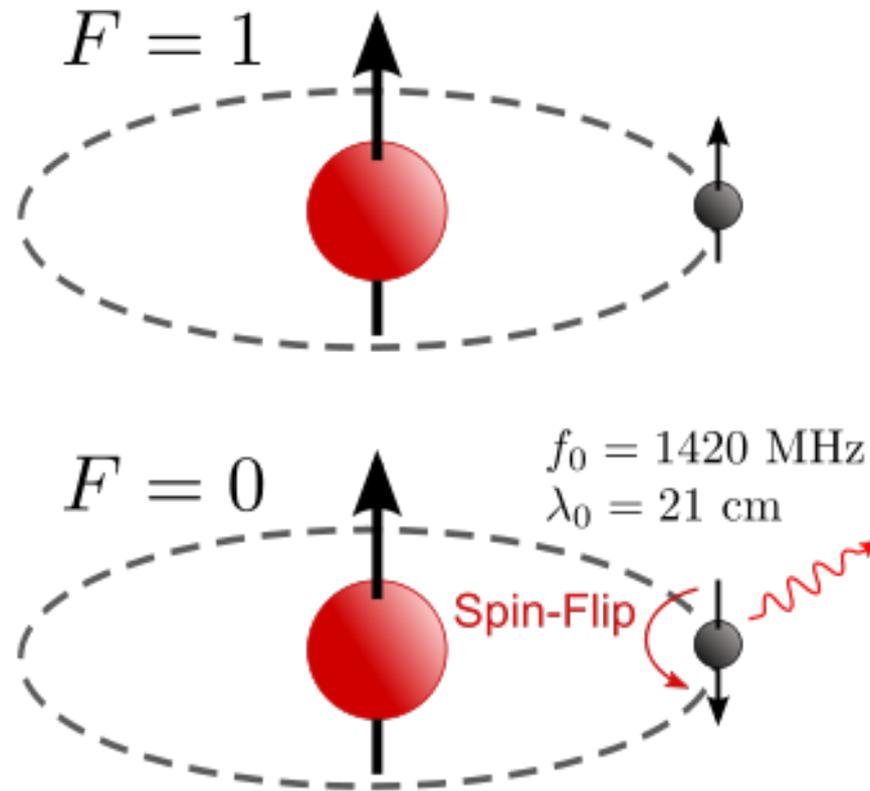
Final emission power is a product of power-laws, to give:

$$\epsilon_\nu \sim \nu^{-0.7}$$

# Neutral Hydrogen

Proton-electron spin alignment in Hydrogen ground state

Rare “spin-flip” transition ( $\sim 10^{-7} \text{ yr}^{-1}$ ) emits  $\lambda=21.1\text{cm}$  line



$6 \mu\text{eV!}$   
 $(\sim 10^{-24} \text{ J})$

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Neutral Hydrogen (“HI”) is common in the Universe! Can be used to see regions that don’t emit any other light

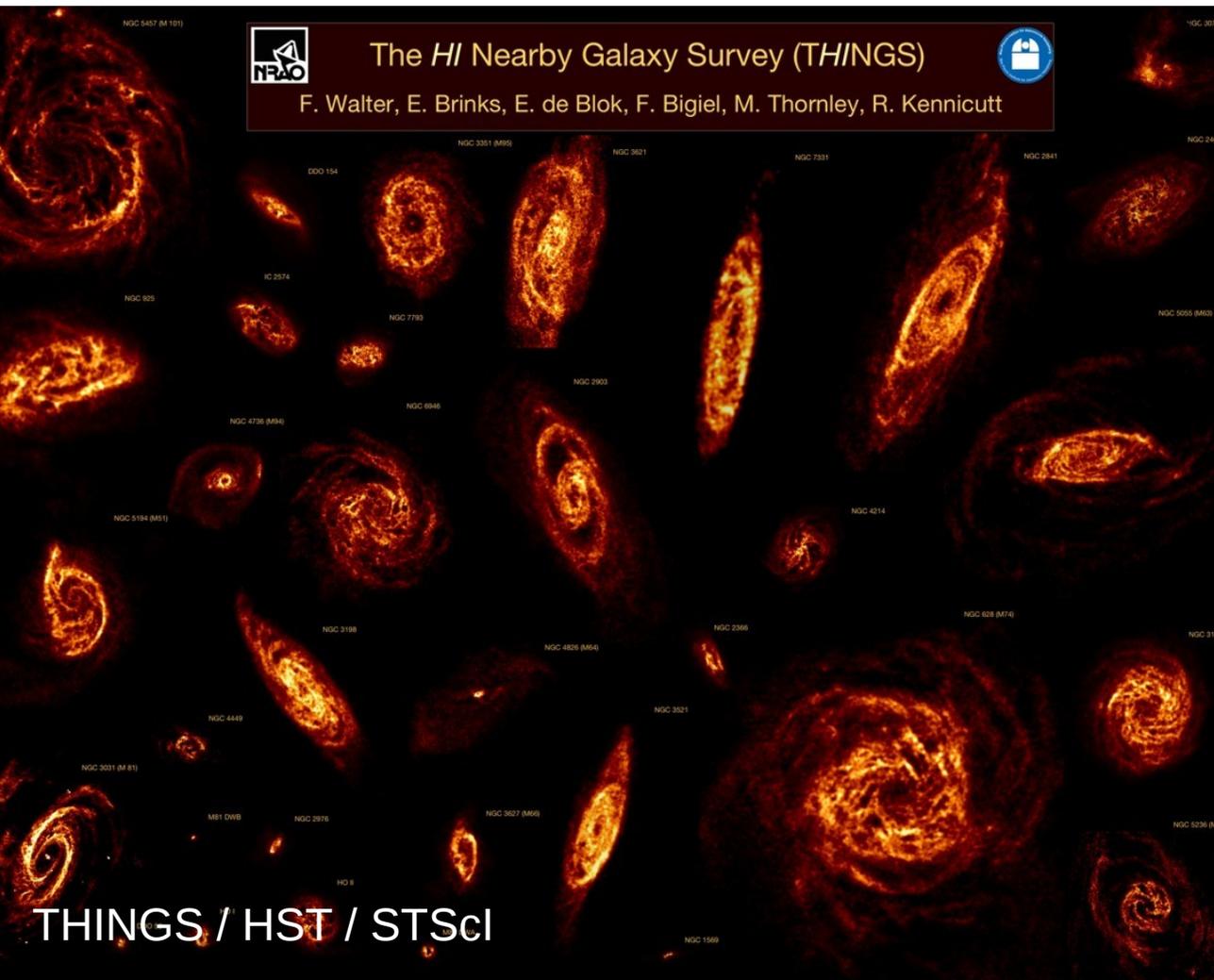
21cm line is redshifted  $\rightarrow$  observed at  $\lambda = 21\text{cm} \times (1 + z)$



# Neutral Hydrogen

It's easy to destroy HI...

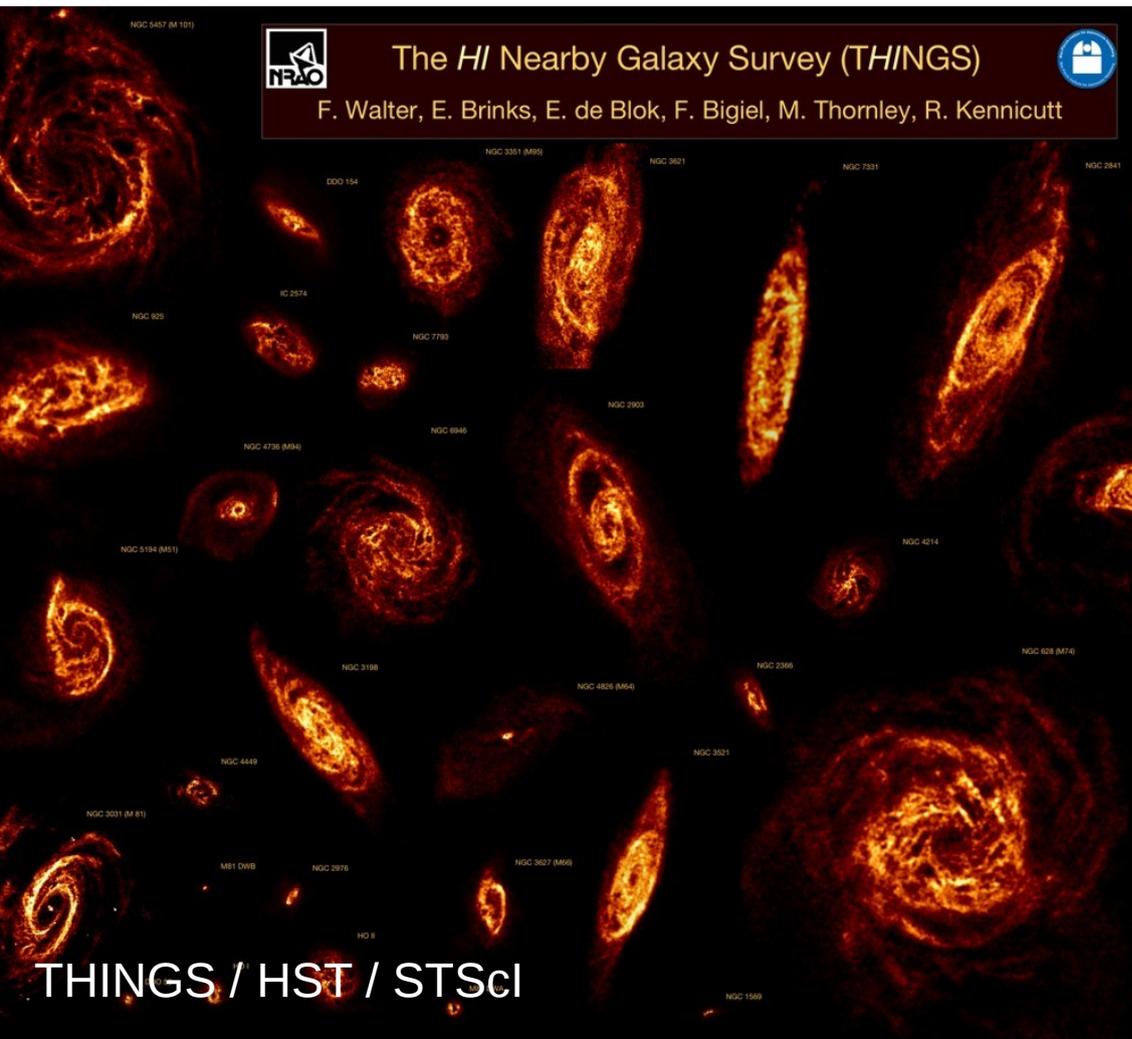
- Photo-ionisation by UV background from stars/galaxies
- Processing of neutral gas into stars (star formation)



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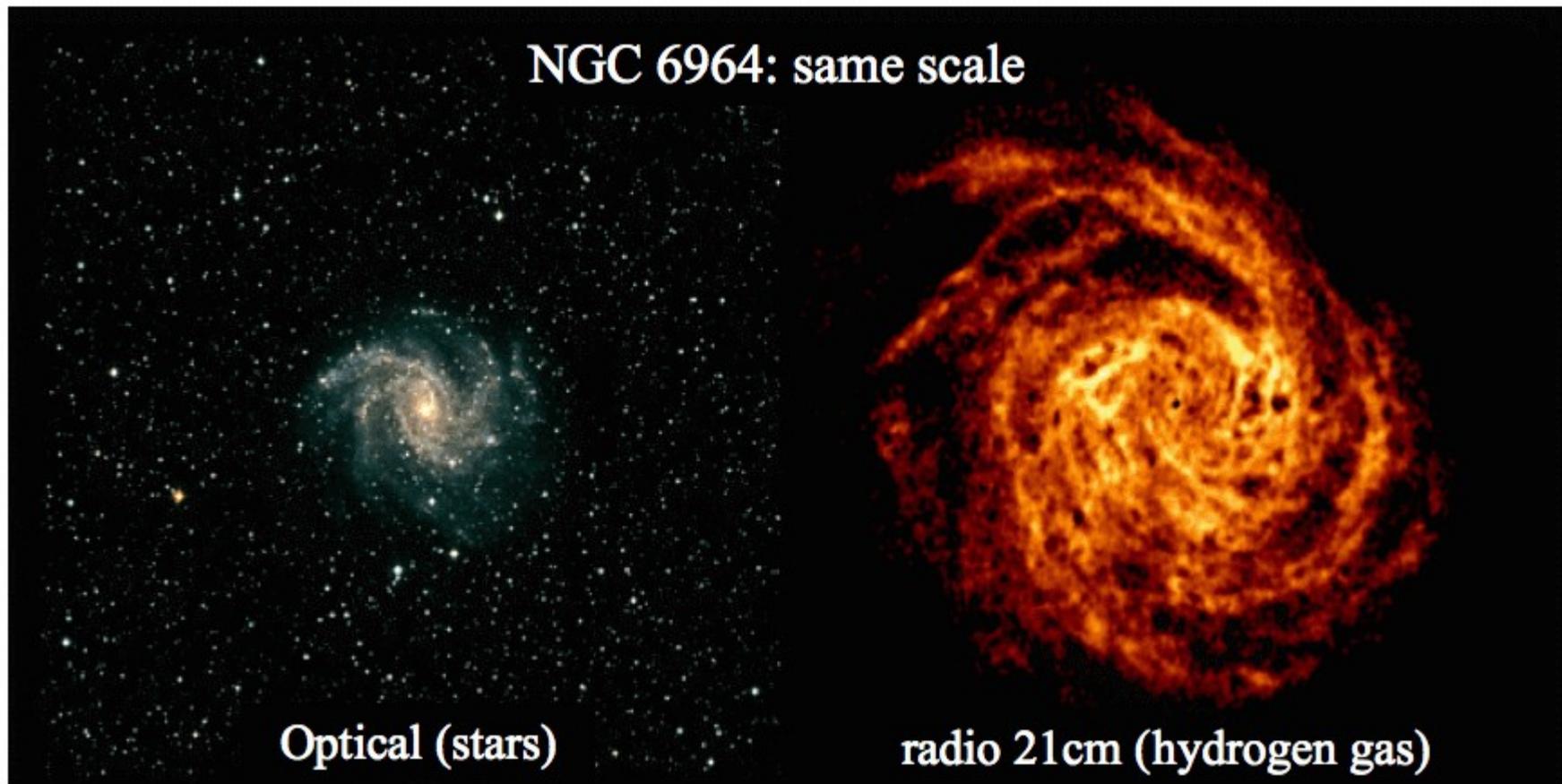
HI gas cycles through *reservoirs* in galaxies

- Ionised gas falls in from IGM and cools → **new HI**
- Gas inside reservoir is **shielded** from UV
- HI falls into galaxy and eventually **forms stars**

# Neutral Hydrogen

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# Continuum galaxy surveys

# Detection

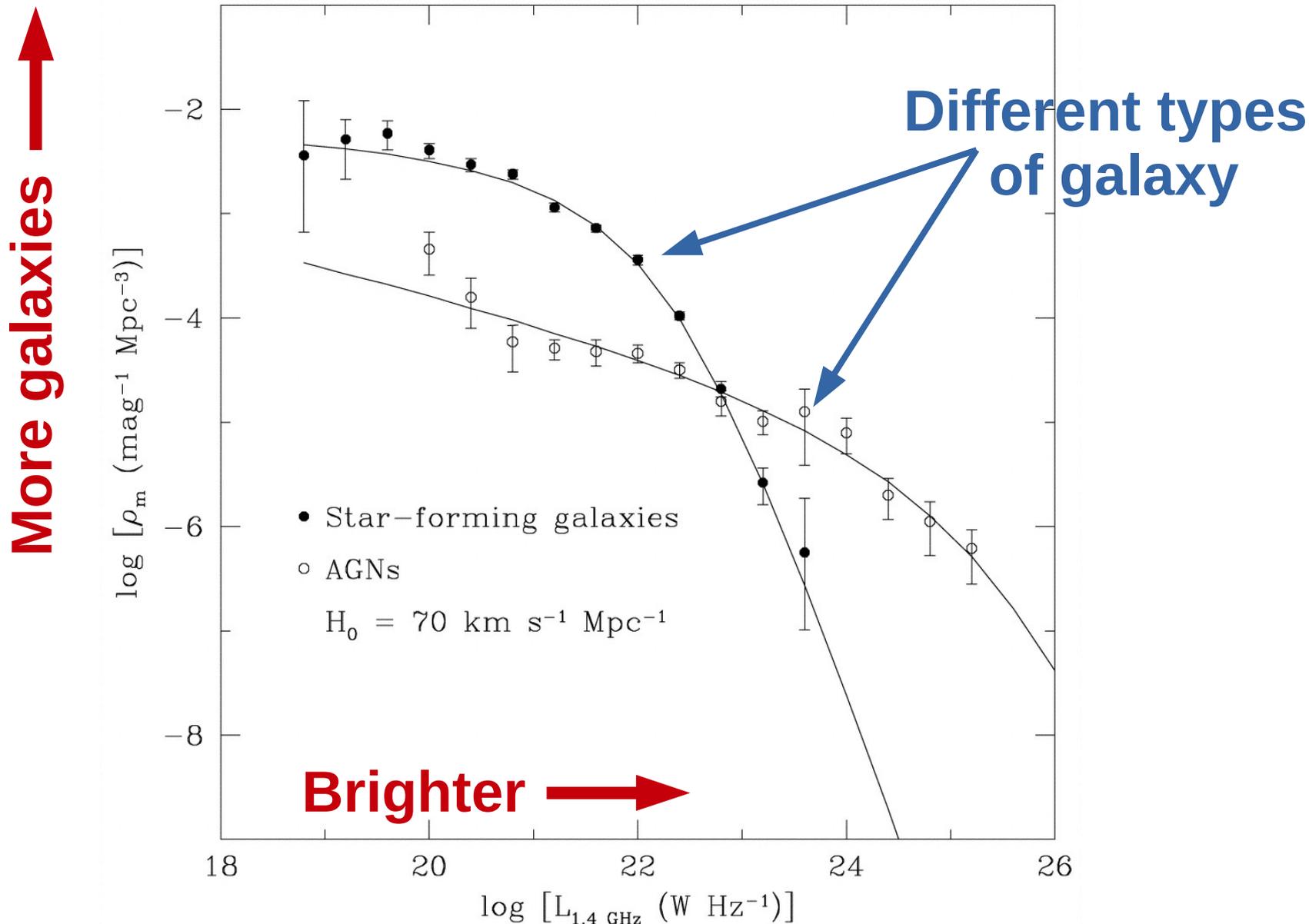
- (1) Stare at the sky (integrate) until some noise level is reached...
- (2) Integrate over full bandwidth to **improve sensitivity**

$$\sigma_S \approx \frac{2k_B T_{\text{sys}}}{A_{\text{eff}} \sqrt{\delta\nu t_{\text{obs}}}}$$

- (3) Make image from interferometer snapshots
  - (4) Keep point sources that are brighter than some threshold above the noise level
- (Recall the issues of confusion, thresholding etc.)

# Galaxy number counts

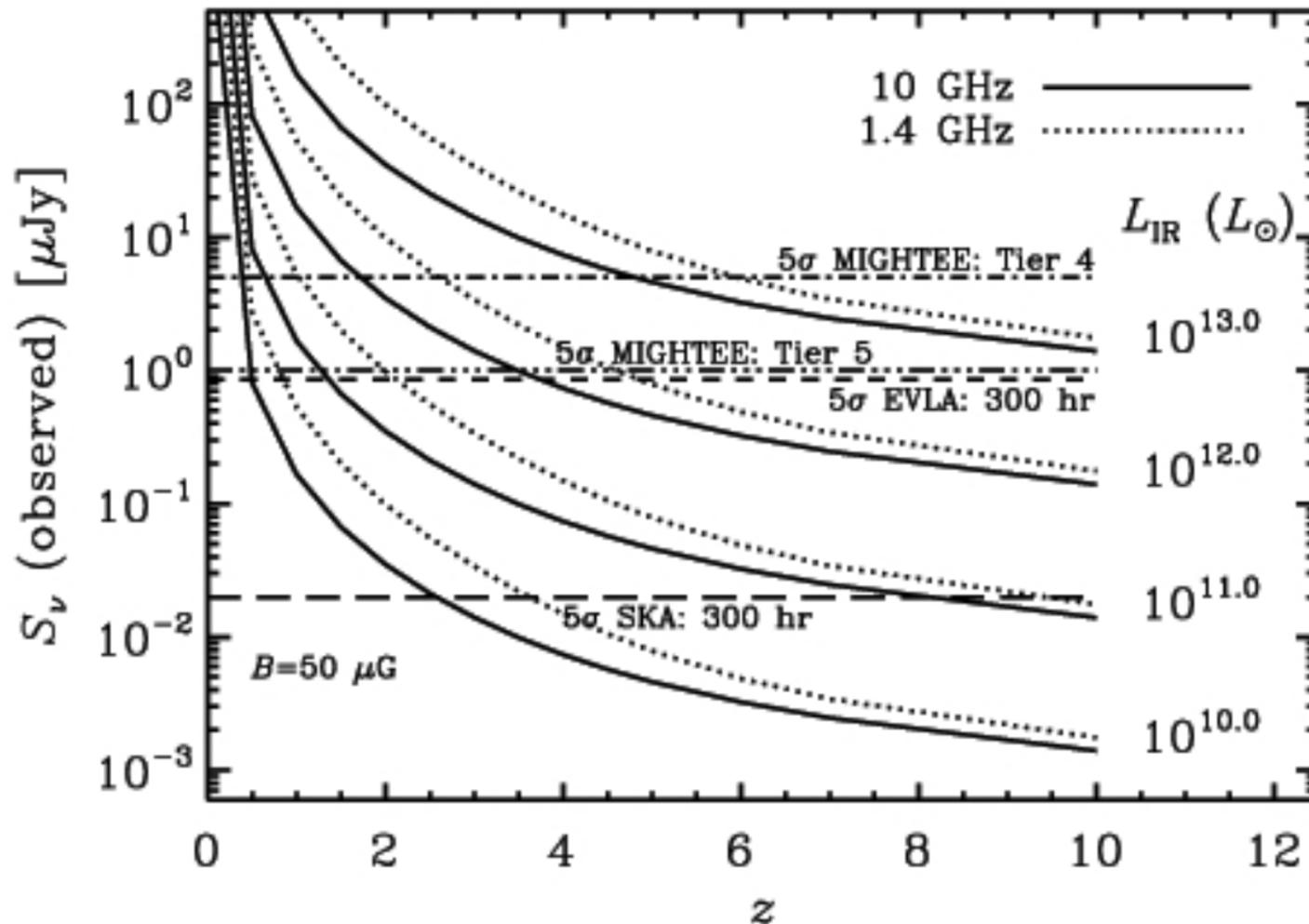
Number of galaxies vs. their intrinsic luminosity



# Number counts vs. redshift

- Distant sources are fainter
- Source populations evolve with redshift
- Luminosity depends on frequency (redshifted!)

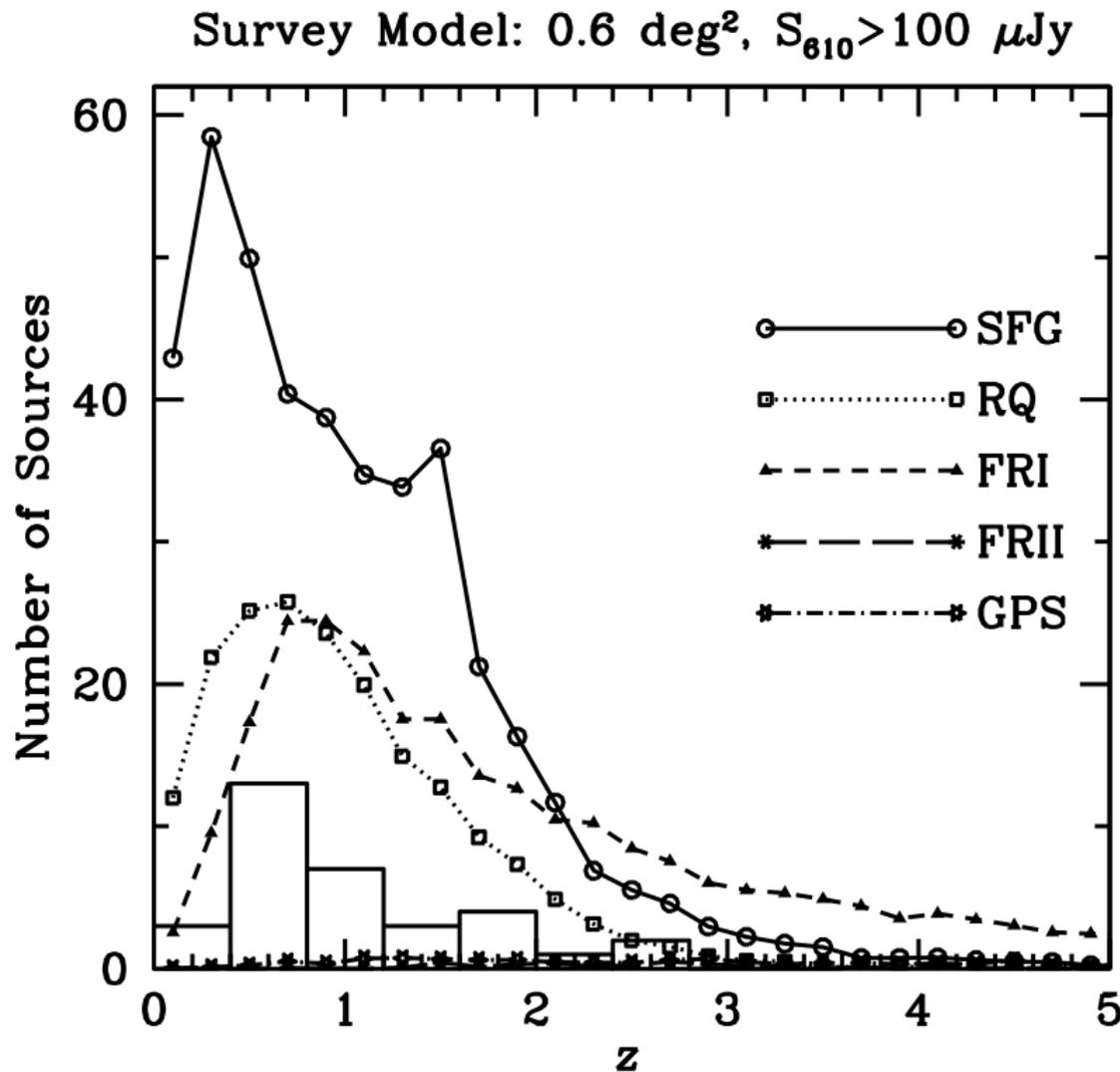
$$S = \frac{L}{4\pi d_L^2}$$



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# Cosmology with continuum galaxies

## **No redshift information**

- Continuum spectra are smooth → no lines or features
- Can only measure the 2D (angular) coordinates

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- Can only measure the 2D (angular) coordinates

## 2D clustering

- Much less information than 3D, but still useful
- High number densities: valuable for **lensing**
- Look for **preferred directions** and anisotropies

## Classification

- Galaxies can be *classified* by spectra and morphology
- Different types of galaxy live in dark matter halos of different masses

# “Value-added” weak lensing

## **Intrinsic galaxy properties**

- Some *intrinsic* properties (i.e. before lensing) can be inferred and compared with (lensed) observations
- Use these to separate lensing from *intrinsic alignments*

# “Value-added” weak lensing

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## Examples

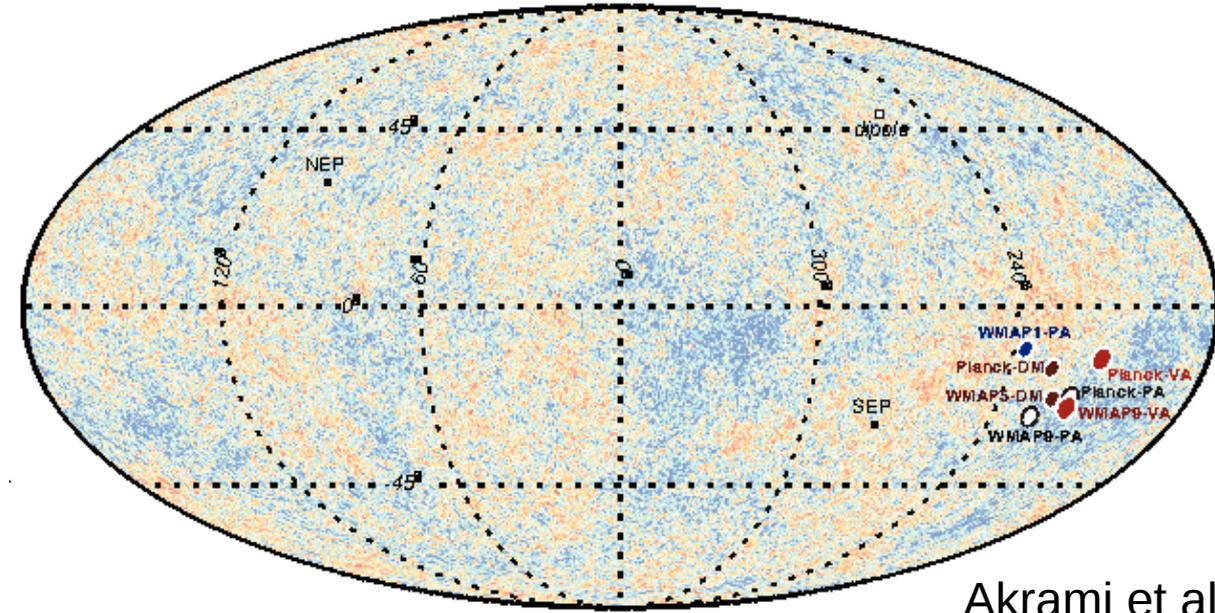
- Rotation velocities (Blain 2002; Morales 2006)
- Polarisation (Brown & Battye 2011)

## Problems

- Deconvolution can affect shape measurements...
- Measure ellipticity directly in visibility (Fourier) space?
- See [arXiv:1507.06639](https://arxiv.org/abs/1507.06639) for SKA lensing requirements

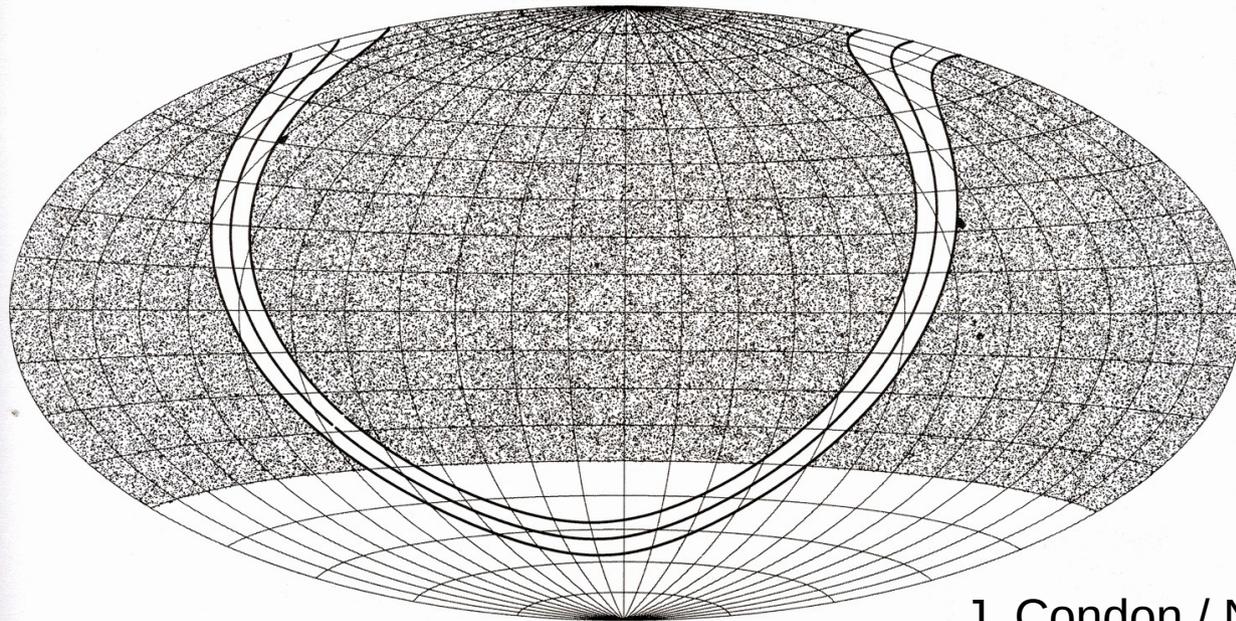
# Cosmology with continuum galaxies

## Anisotropy / preferred directions?



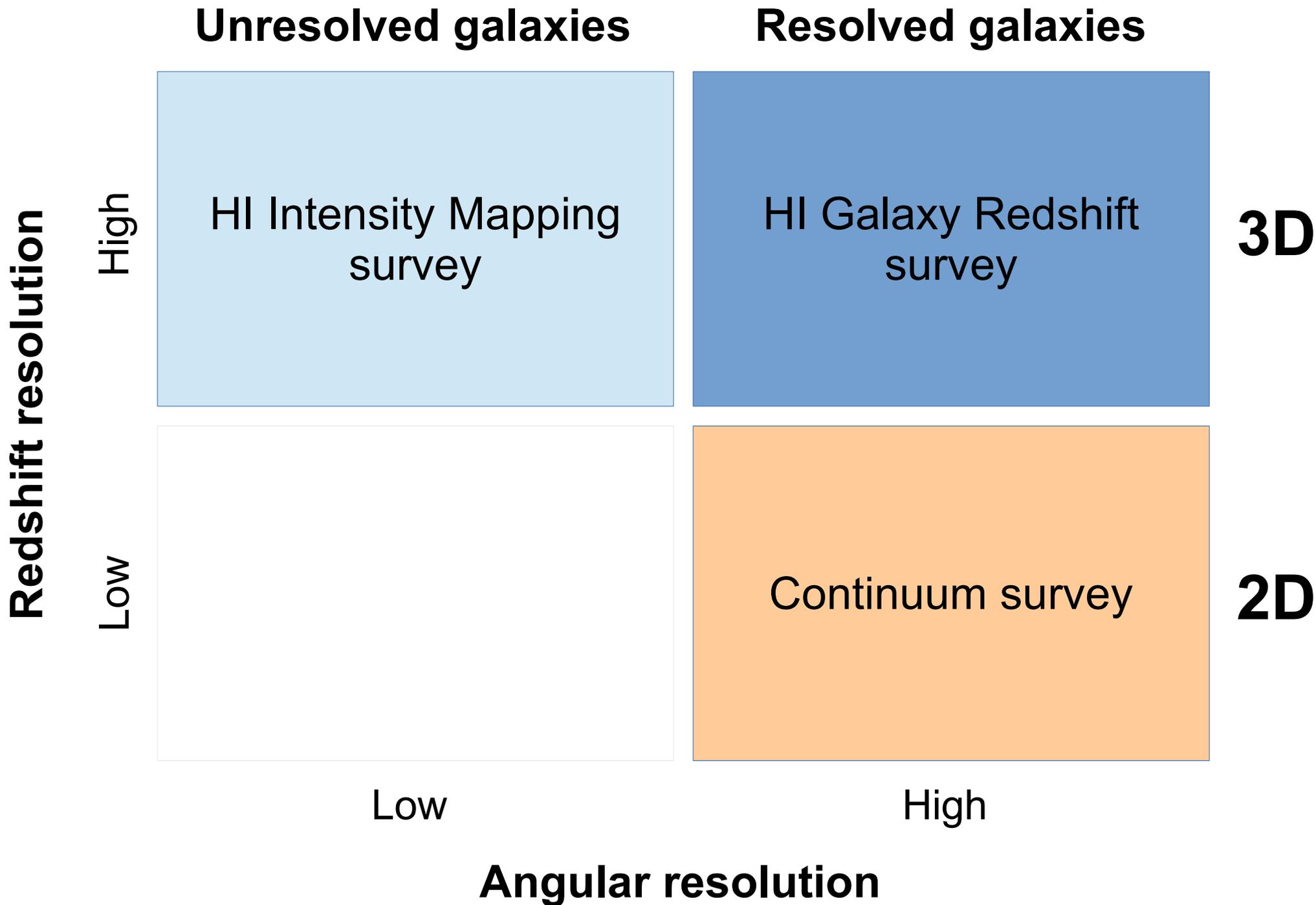
Akrami et al. 2014

Small ( $\sim 7\%$ ) power asymmetry seen in the CMB



J. Condon / NVSS

Is it real? Need to cross-check with galaxy distribution



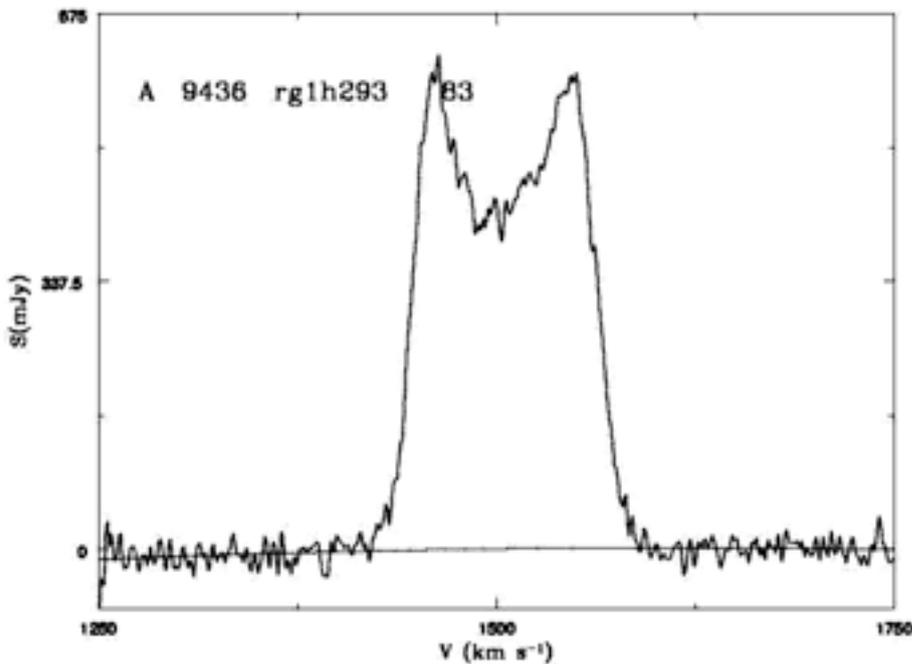
# HI galaxy surveys

# Neutral Hydrogen

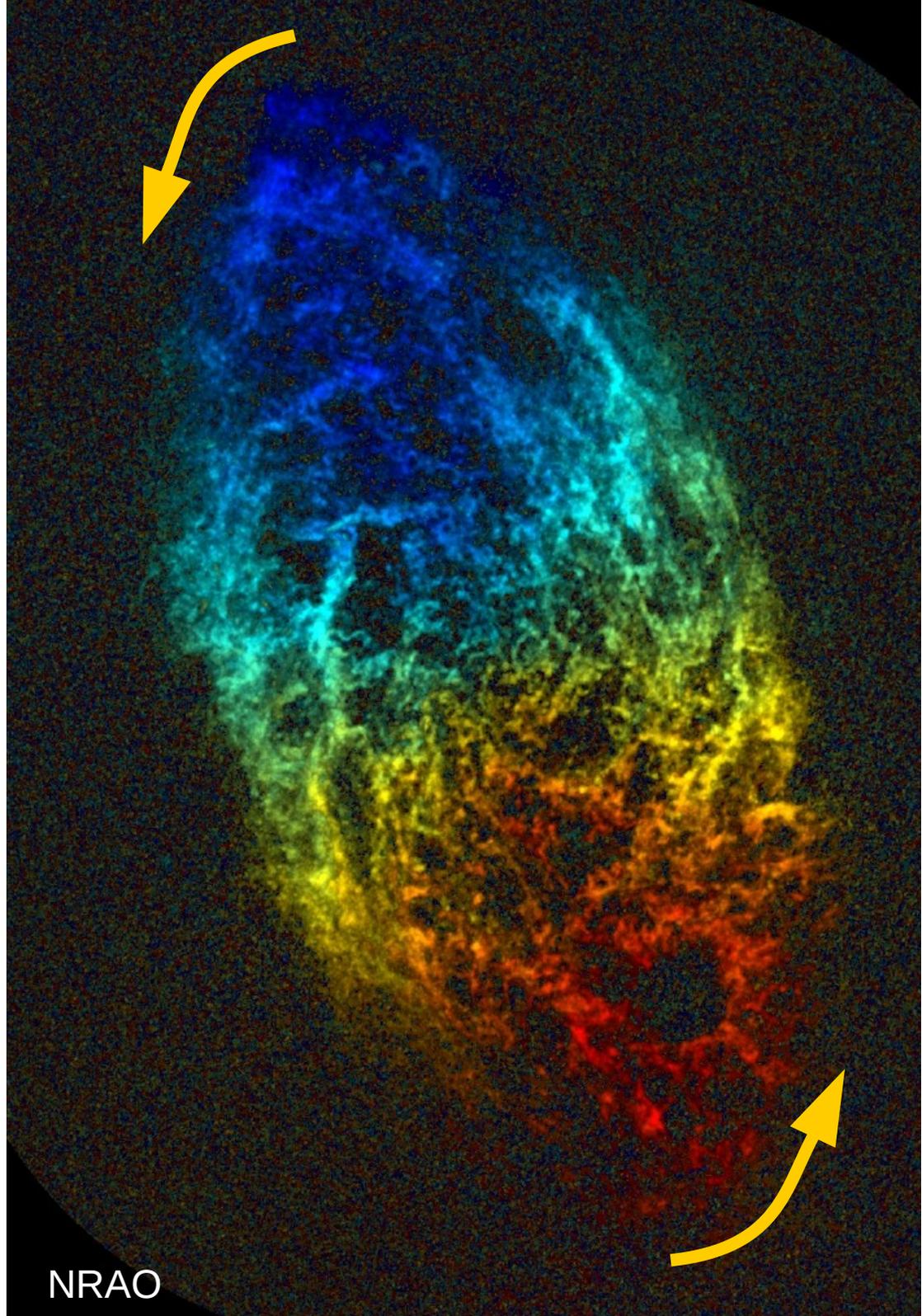
21cm line is Doppler shifted by galaxy rotation

Traces motion of gas in galaxies: “rotation curve”

“Double-peaked” line profile



ALFALFA



NRAO

# Detecting HI galaxies

Need sensitivity in **narrow band** to detect 21cm line

$$\sigma_S \approx \frac{2k_B T_{\text{sys}}}{A_{\text{eff}} \sqrt{\delta\nu t_{\text{obs}}}} \quad \sim \text{few kHz}$$

## Source detection algorithm

- Need to reject “lines” that are just RFI and noise peaks

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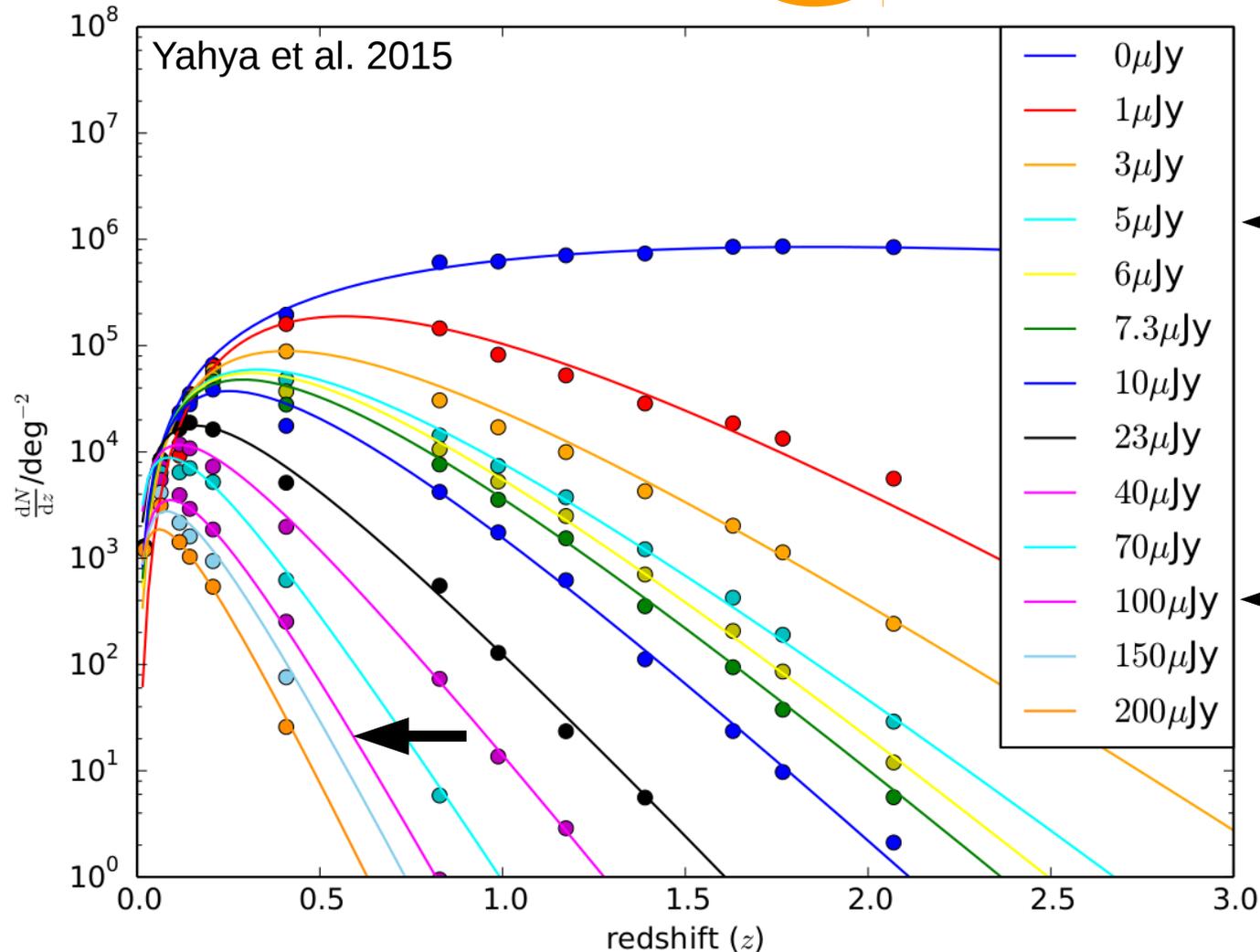
- Need to reject “lines” that are just RFI and noise peaks
  - If we see a double-peaked line, it’s not noise/RFI...  
but *face-on* galaxies don’t have a double peak
  - If we choose a larger  $\delta\nu$ , the noise is smaller... but then we won’t see a double peak for *almost* face-on galaxies
- Smart algorithms can be designed, but quickly get complicated...

# Detecting HI galaxies

Need sensitivity in **narrow band** to detect 21cm line

$$\sigma_S \approx \frac{2k_B T_{\text{sys}}}{A_{\text{eff}} \sqrt{\delta\nu t_{\text{obs}}}}$$

Depends on the survey area + total survey time



SKA2  
~30k deg<sup>2</sup>

SKA1-MID  
~5,000 deg<sup>2</sup>

# Detecting HI galaxies

**SKA1-MID:** ~few million HI galaxies at  $z < 0.4$

**SKA2:** ~1 billion HI galaxies at  $z < 1.5$

All with high-precision **3D positions** (angle + redshift):

→ Measure the *3D galaxy power spectrum*

- Baryon acoustic oscillations → expansion rate
  - Redshift-space distortions → growth of structure
  - Cross-correlation/tomography → improve lensing etc.
- (See lectures by others)*

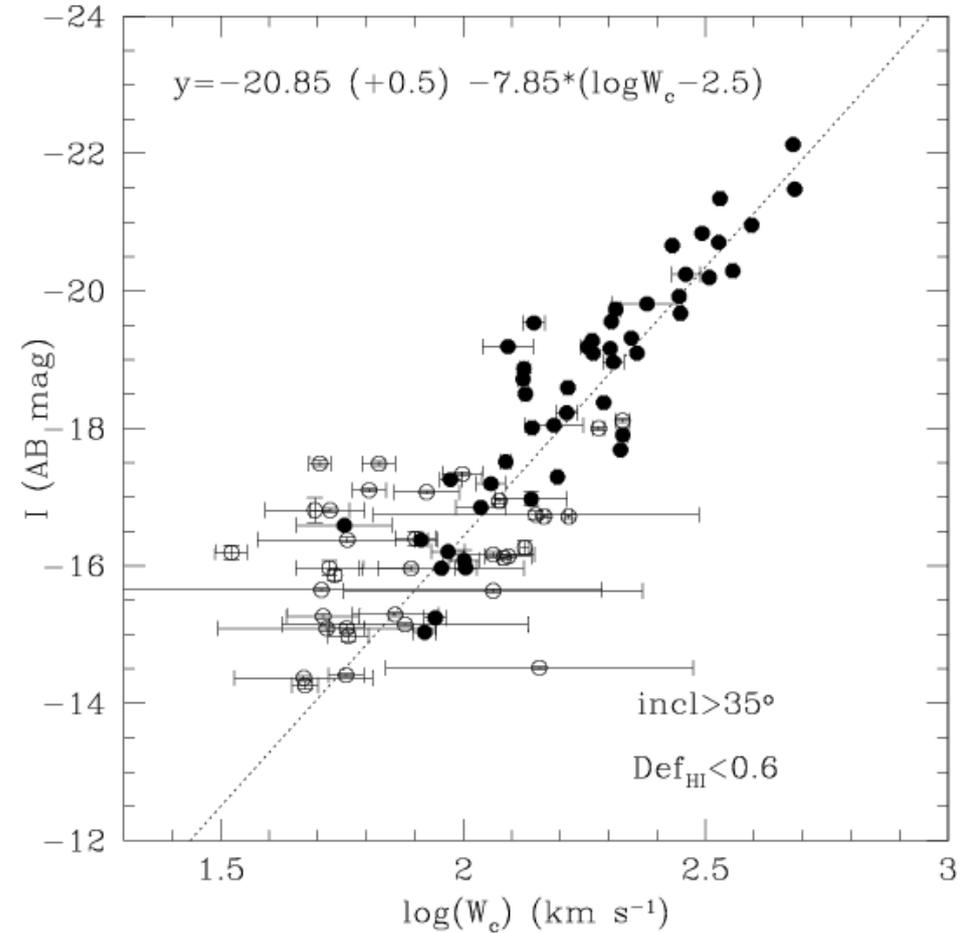
**Unique with HI:** direct galaxy velocity measurements

# Peculiar velocities

**Tully-Fisher:** Relation between max. *rotation* velocity and

luminosity:  $L \propto v_{\max}^{\alpha}$

Gavazzi et al. 2008



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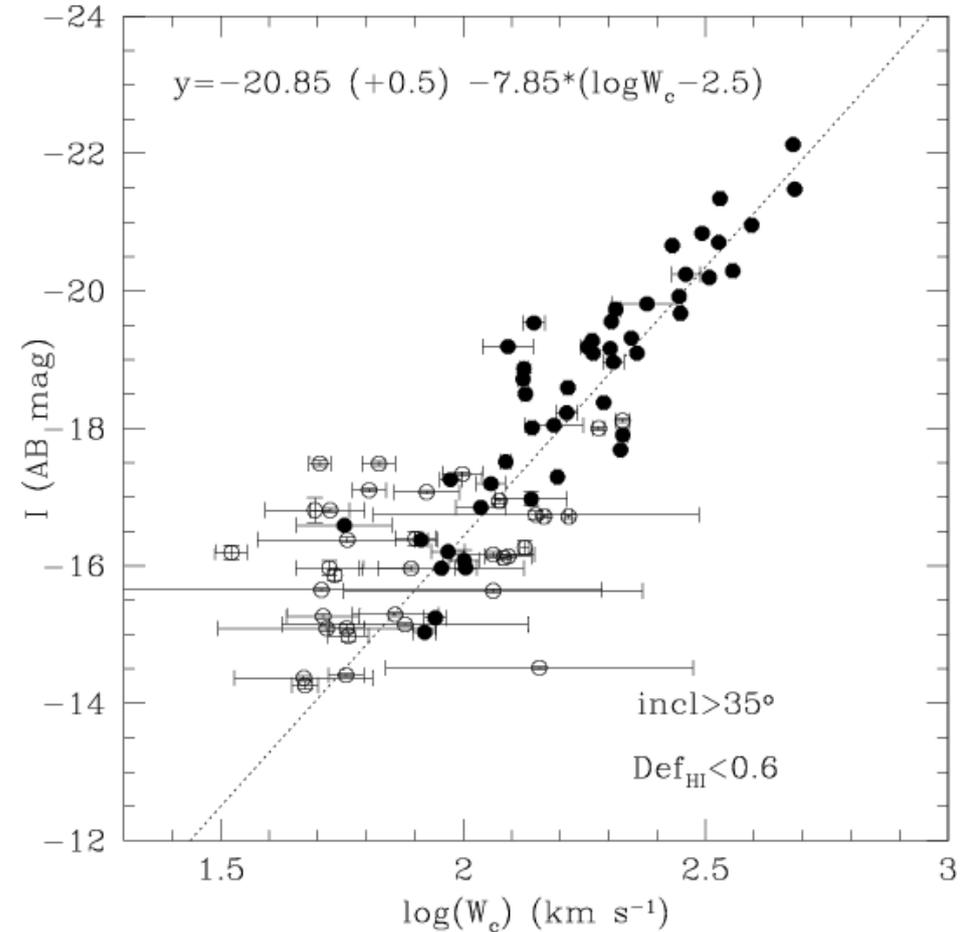
luminosity:  $L \propto v_{\max}^{\alpha}$

Gavazzi et al. 2008

21cm line width related to  $v_{\max}$

→ Use measured flux and width as “standard candle”:

$$L = \kappa w_{21}^{\alpha} \quad S = \frac{L}{4\pi d_L^2}$$



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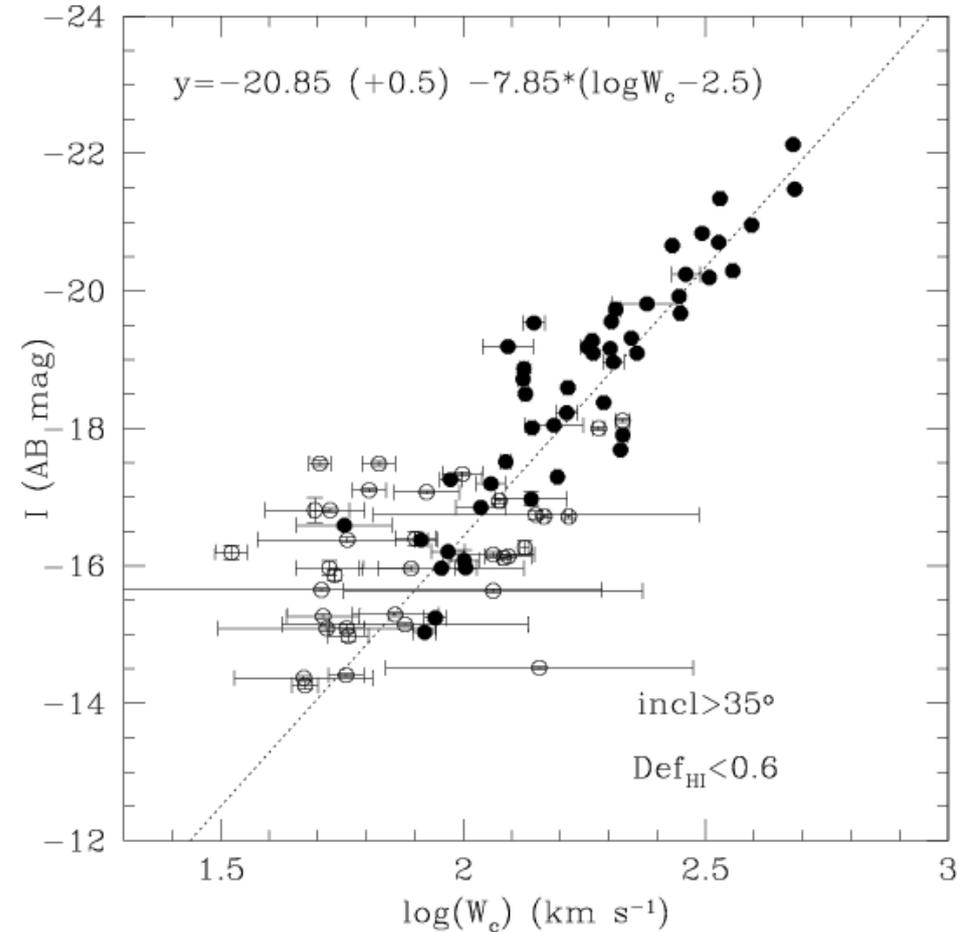
→ Use measured flux and width as “standard candle”:

$$L = \kappa w_{21}^\alpha \quad S = \frac{L}{4\pi d_L^2}$$

Measured luminosity distance:

$$d_L(z_{\text{true}}) = \sqrt{\frac{\kappa w_{21}^\alpha}{4\pi S}}$$

Invert to get true redshift and compare to *observed* redshift:

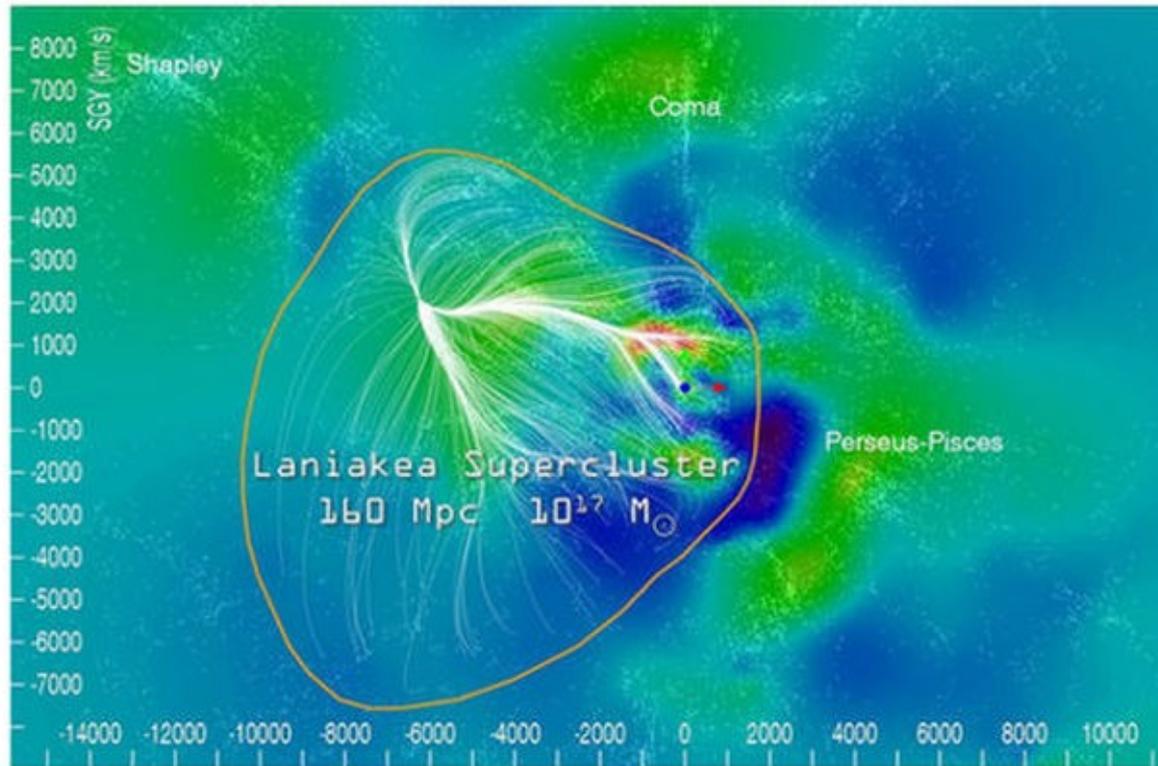


$$z_{\text{obs}} = z_{\text{true}} + (\mathbf{v} \cdot \hat{\mathbf{n}}/c)$$

# Peculiar velocities

What can we learn from peculiar velocities?

- Galaxy motions identify objects that are gravitationally **bound**:



DPvision/CEA

- Measures **growth**,  $f(z)$ , and **expansion rate**,  $H(z)$ :

$$\mathbf{v}(t, \mathbf{k}) = \frac{H f}{a} \frac{i\mathbf{k}}{k^2} \delta(t, \mathbf{k})$$

# Intensity mapping

# Intensity mapping

## Why detect individual galaxies?

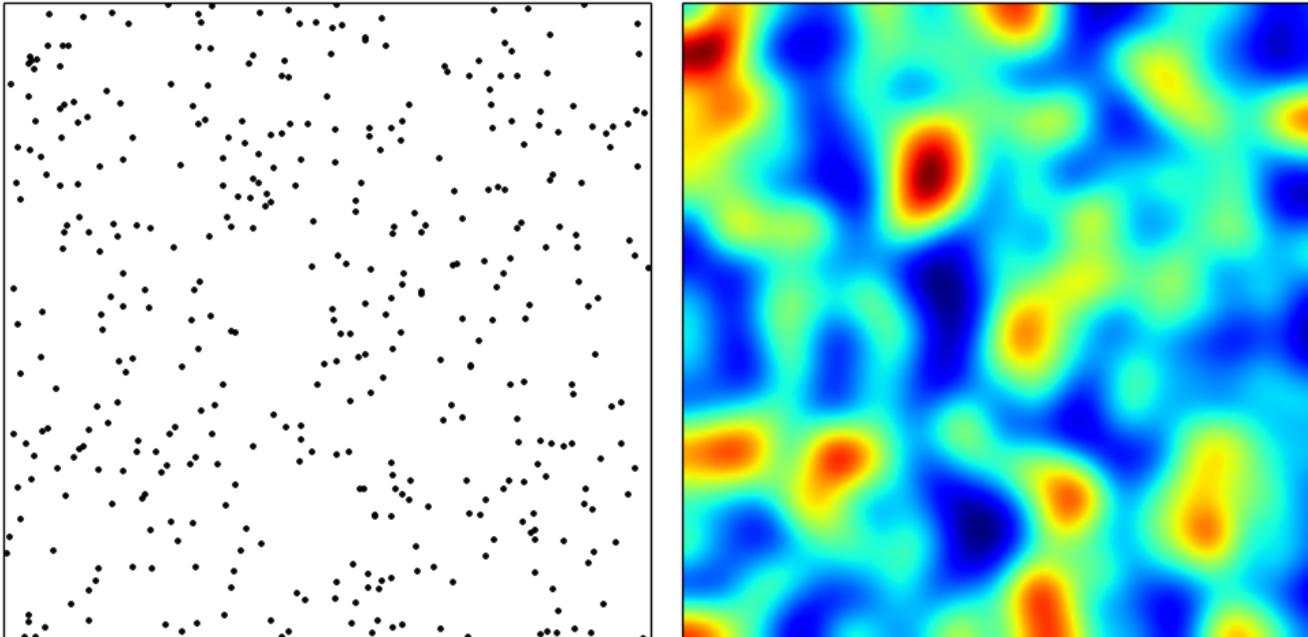
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- High SNR detection of galaxy 'wastes' photons
- Spectroscopic redshifts take a long time

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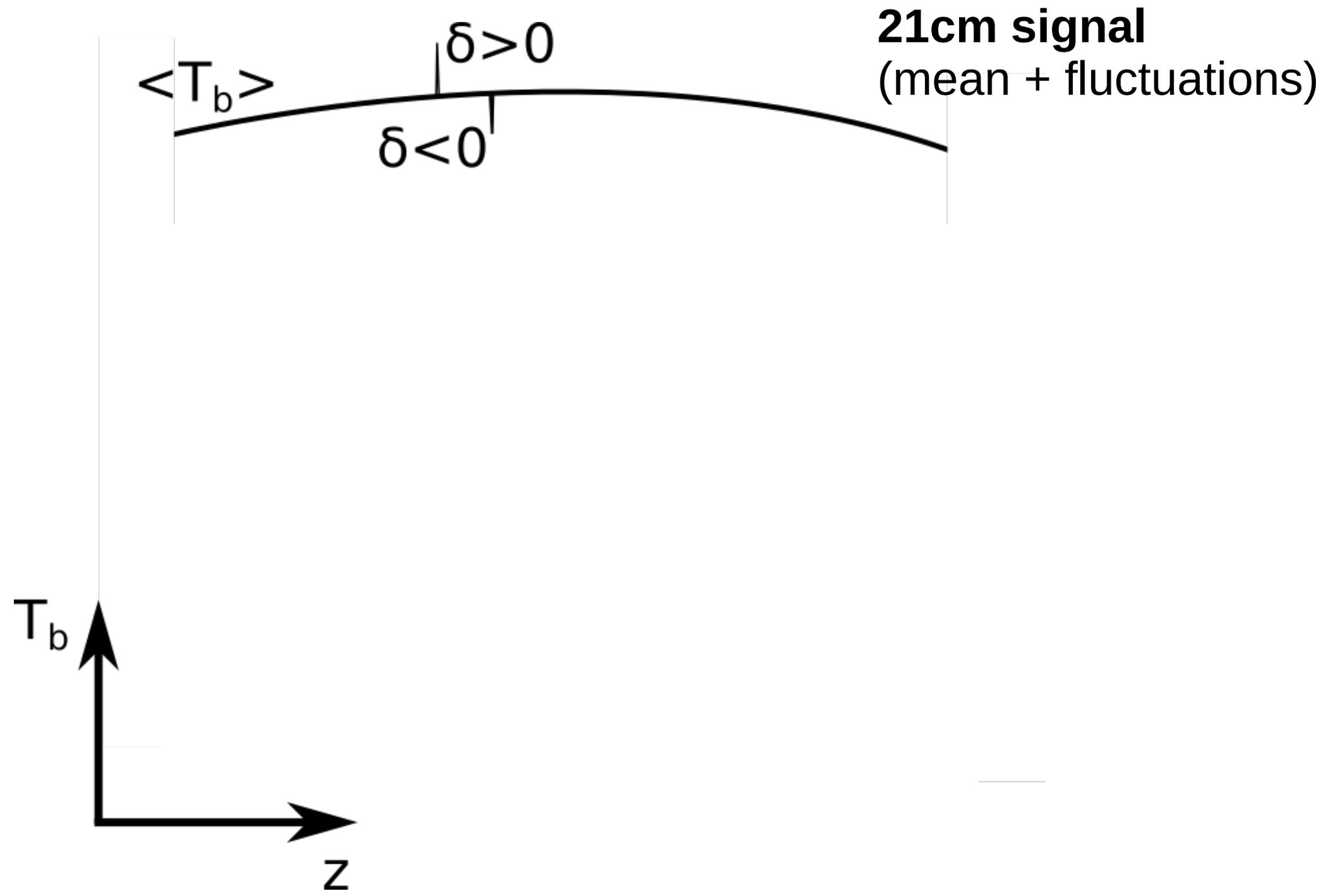
→ **Map out emission integrated over many galaxies**

## 21cm intensity maps

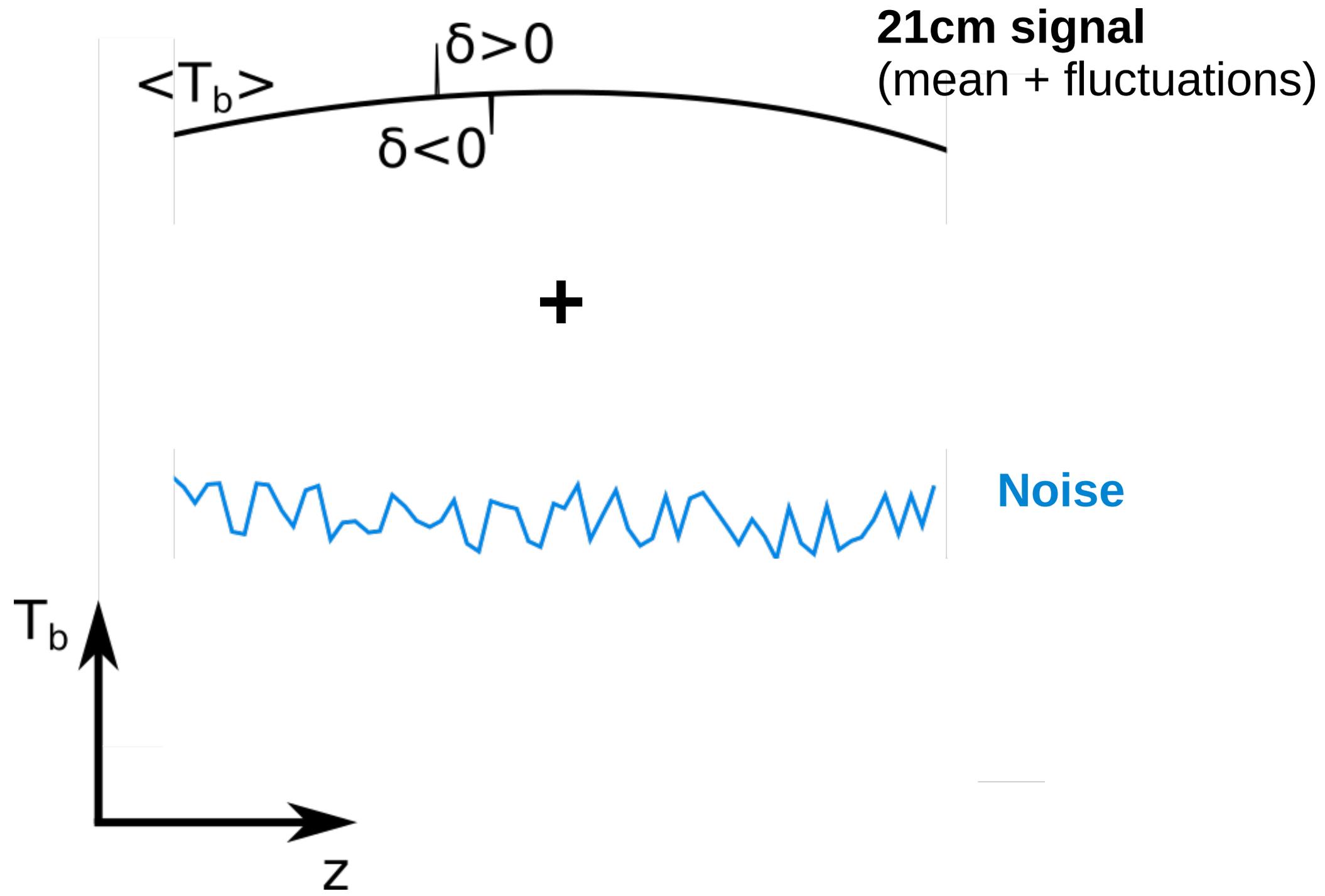
- Low-resolution still preserves large-scales (c.f. CMB)
- Integrated emission is easier to detect / no thresholding
- Detecting an emission line → get redshifts for free

See **Bull** et al. (1405.1452) for a primer

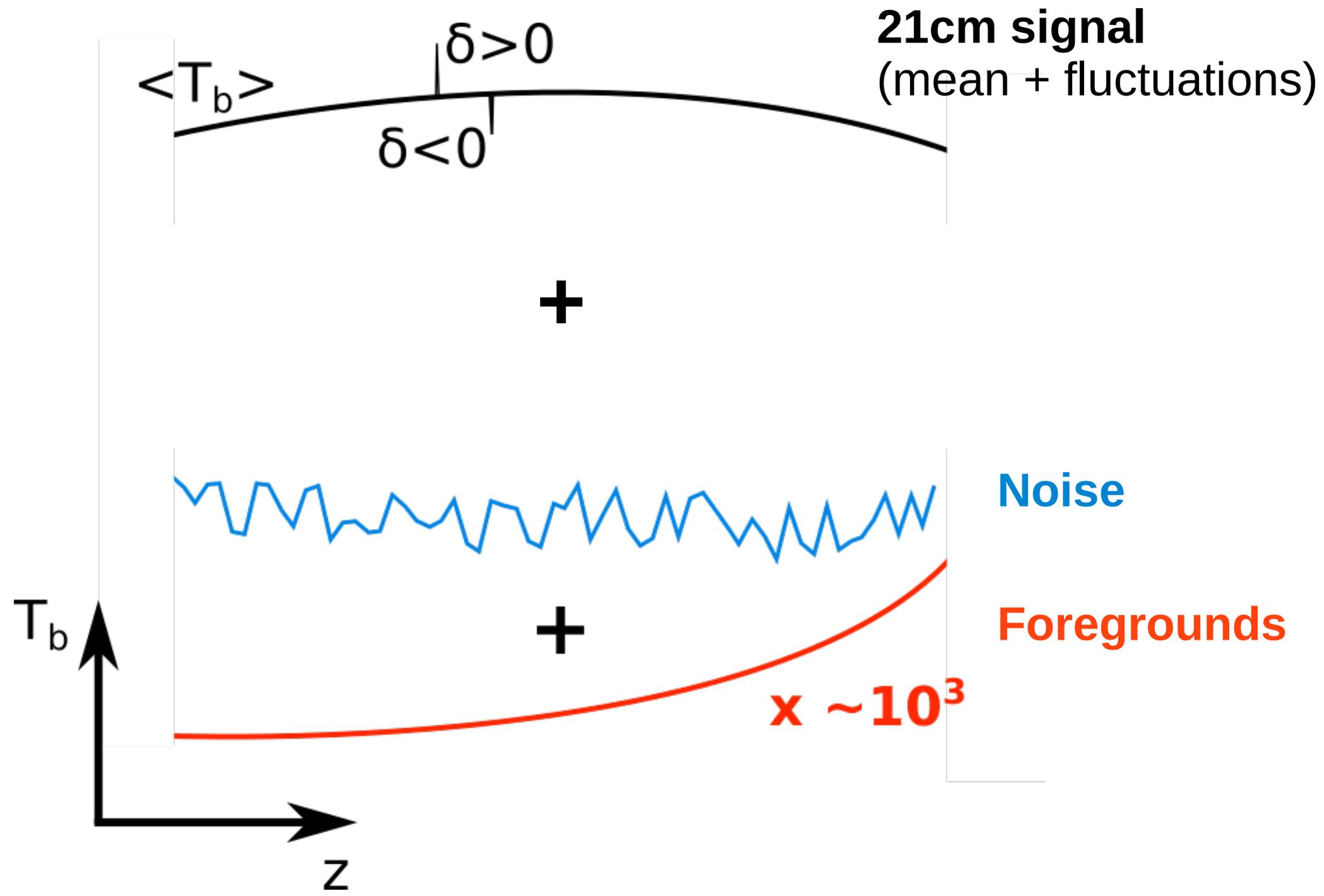
# Frequency spectrum



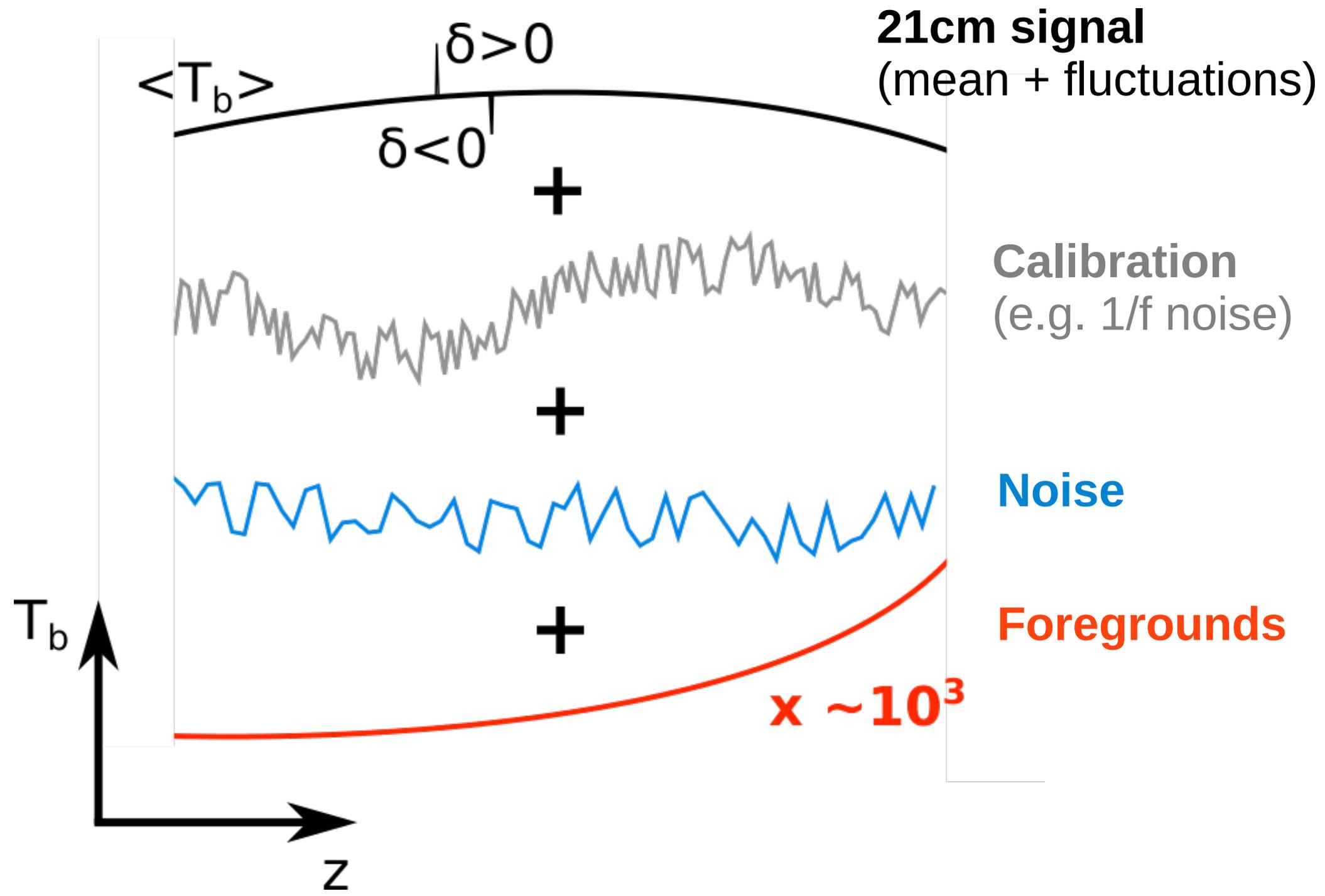
# Frequency spectrum



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# Frequency spectrum



# 21cm brightness temperature

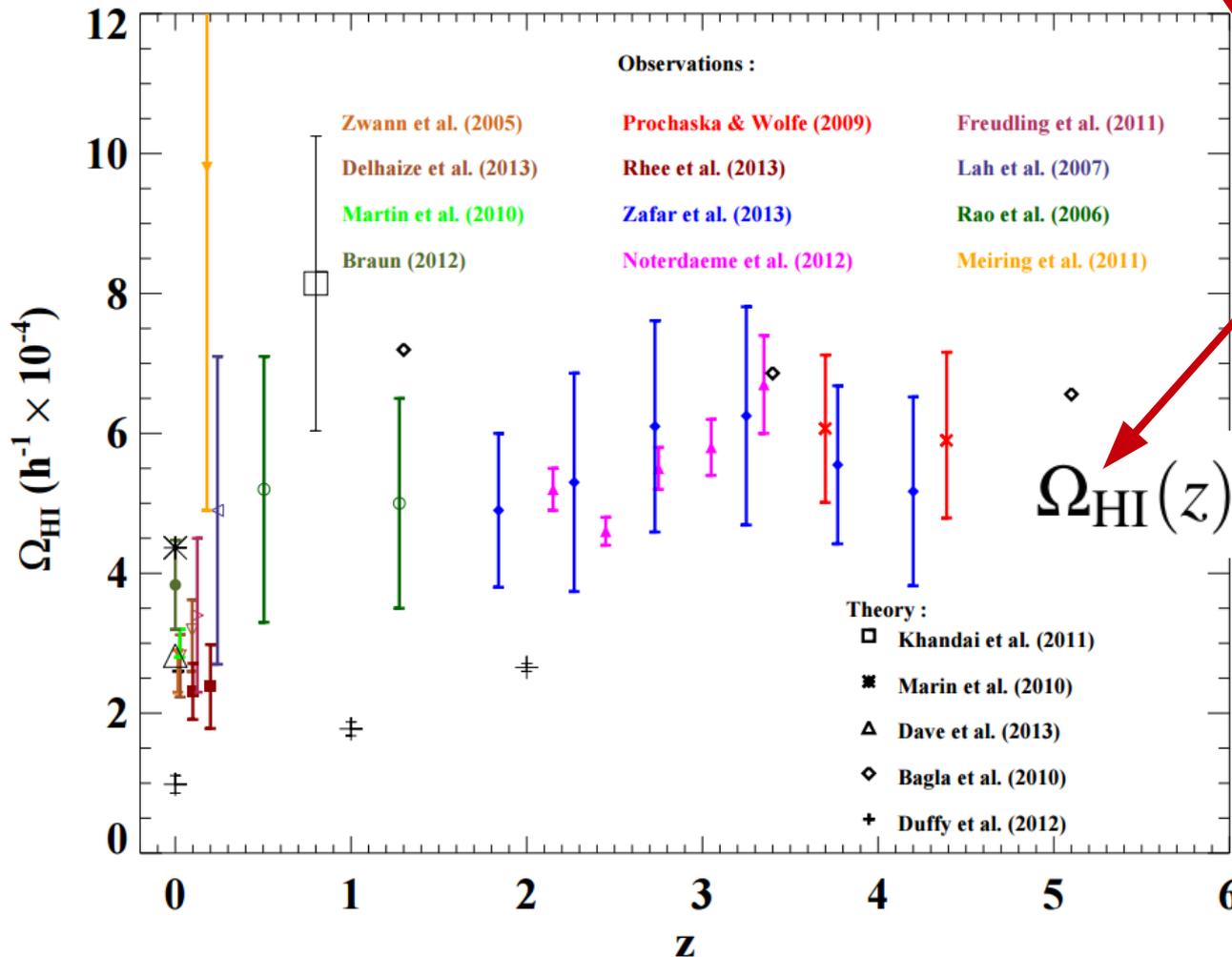
Mean temperature of **all the HI** at a given redshift:

$$\bar{T}_b(z) \approx 566h \left( \frac{H_0}{H(z)} \right) \left( \frac{\Omega_{\text{HI}}(z)}{0.003} \right) (1+z)^2 \mu\text{K}$$

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What fraction of the cosmic energy density is in neutral hydrogen?

$$\Omega_{\text{HI}}(z) \equiv (1+z)^{-3} \rho_{\text{HI}}(z) / \rho_{c,0}$$

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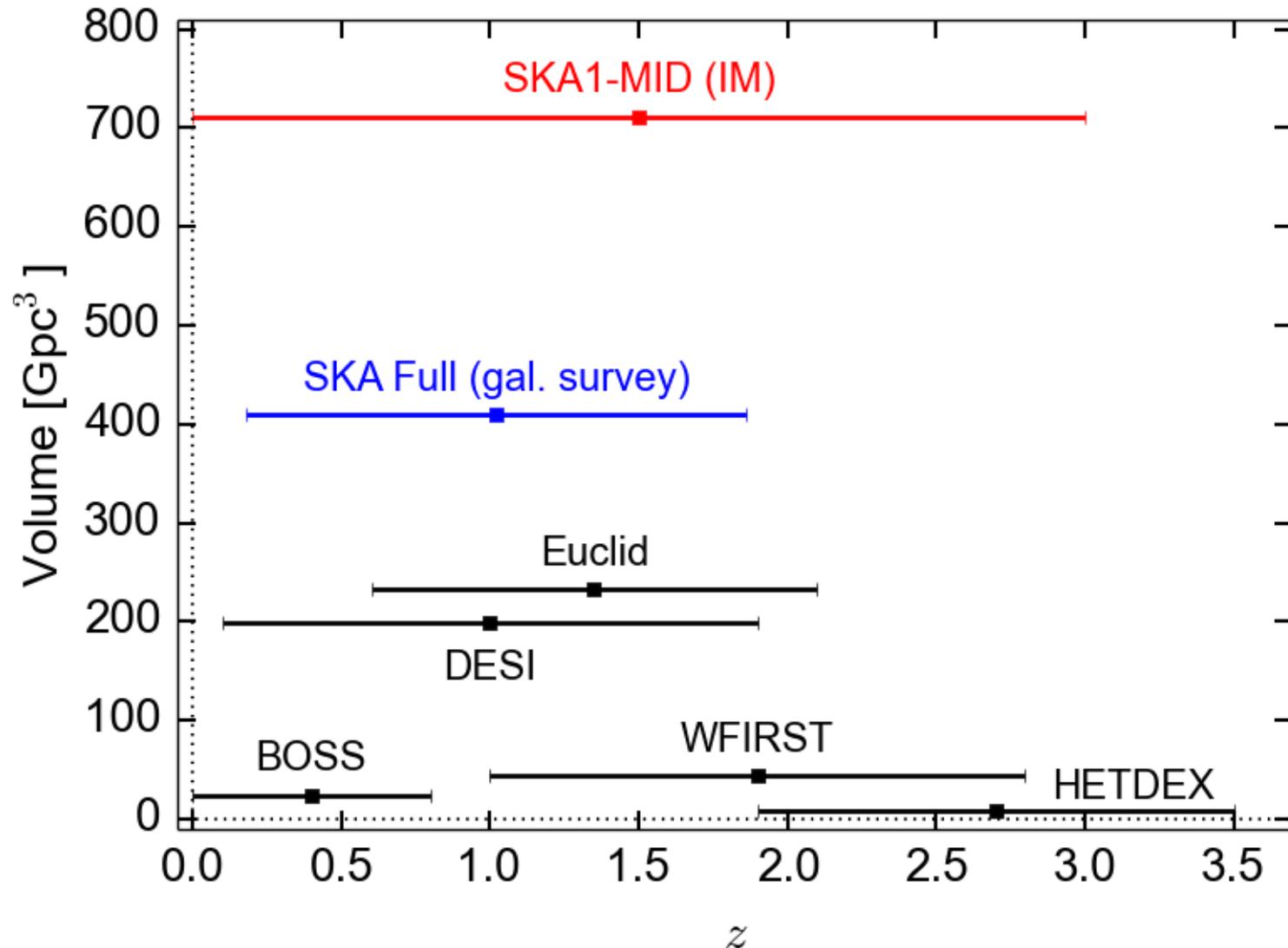
Temperature in a **volume element** at a given frequency/angle:

$$T_b(\nu, \Omega) \approx \bar{T}_b(z) \left[ 1 + b_{\text{HI}} \delta_m(z) - \frac{1}{H(z)} \frac{d\nu}{ds} \right]$$

# Volume

Intensity mapping is very fast → uses all the photons

Can survey much bigger volumes in the same time

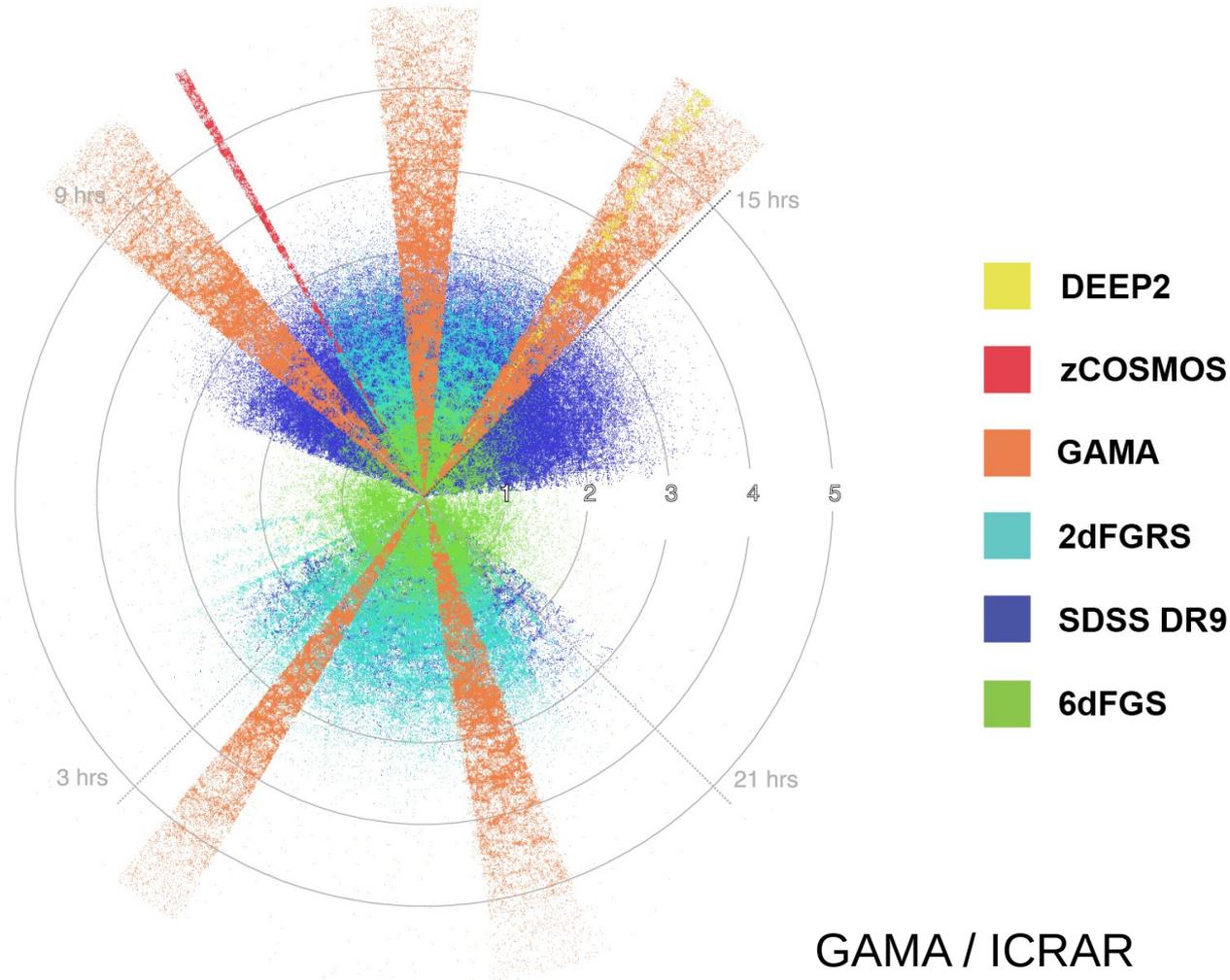


# Designing an intensity mapping experiment

# Designing an IM experiment

## Sensitivity; depth vs. width

- Signal is faint; need high sensitivity to detect it
- Small survey area = greater depth; more time per pointing
- Large survey area = shallower, but can cover larger volume



# Designing an IM experiment

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- Small survey area = greater depth; more time per pointing
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## **Resolution**

- Match the resolution to the scales you care about!
- Big dishes = small field of view. More sensitive but slower surveys
- Interferometers: which Fourier modes? Sparse or dense?

# Designing an IM experiment

## Frequency range

- Frequency range maps directly to redshift range
- Which redshifts matter for the physics you are targeting?
- Wide bandwidths are possible with radio, but receivers get worse if it's too wide (need *multi-mode* receivers)

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## Systematic effects!

- Foregrounds are much bigger than the signal
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- Need a very stable receiver, or one that's easy to calibrate!

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## \$\$\$

- Radio receivers are (relatively) cheap, but people and electricity are not
- Can you justify spending €1 billion? €100m? €10m?

# Single dish or interferometer?

We can use the SKA in single-dish *or* interferometer mode  
→ depends on which **angular scales** we care about!

**Single-dish** (also called autocorrelation)

$$\delta\theta \gtrsim \frac{\lambda}{D_{\text{dish}}}$$

(Can see angular scales  
larger than this size)

**Interferometer**

$$\frac{\lambda}{D_{\text{min}}} \gtrsim \delta\theta \gtrsim \frac{\lambda}{D_{\text{max}}}$$

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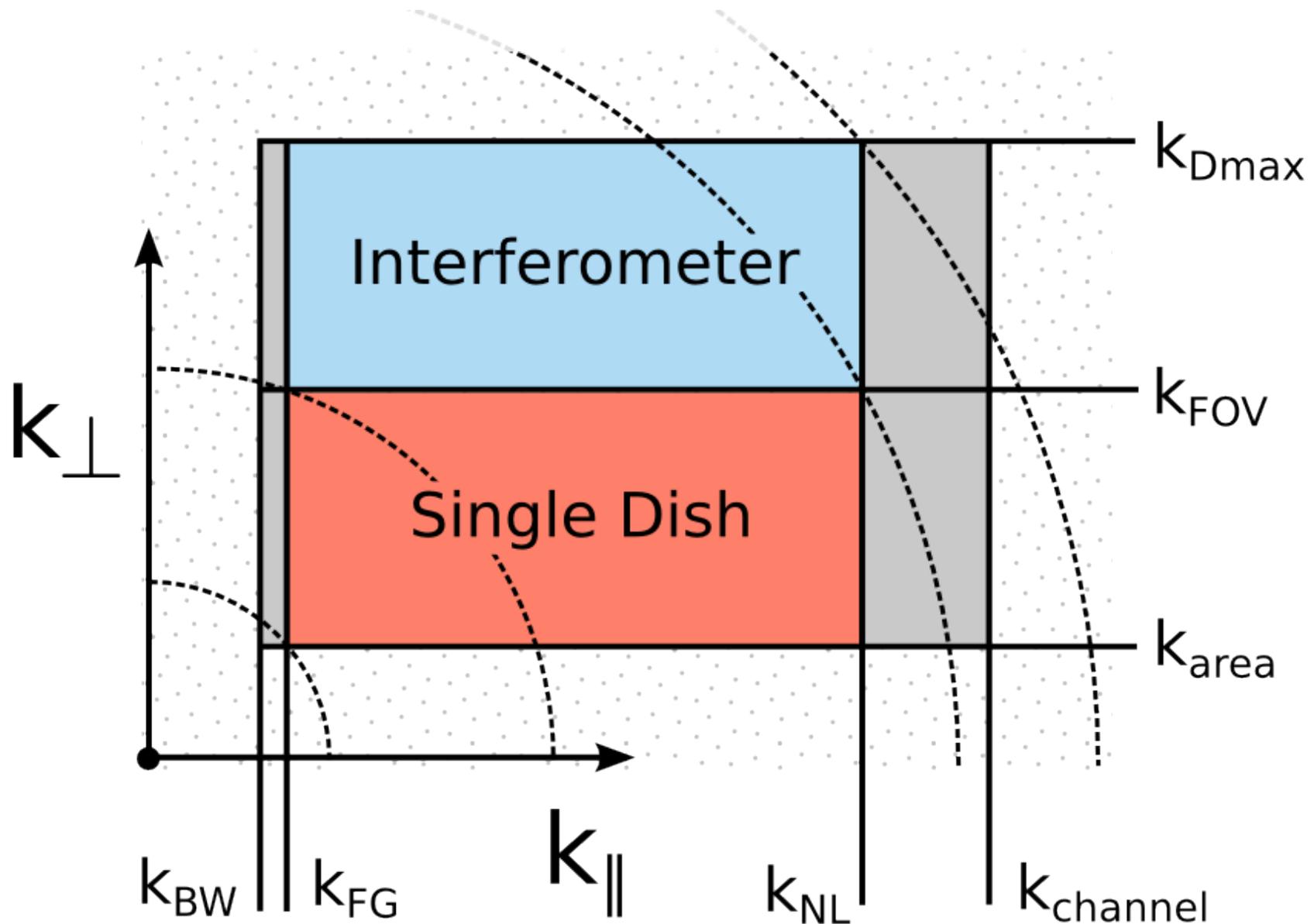
(Can see angular scales  
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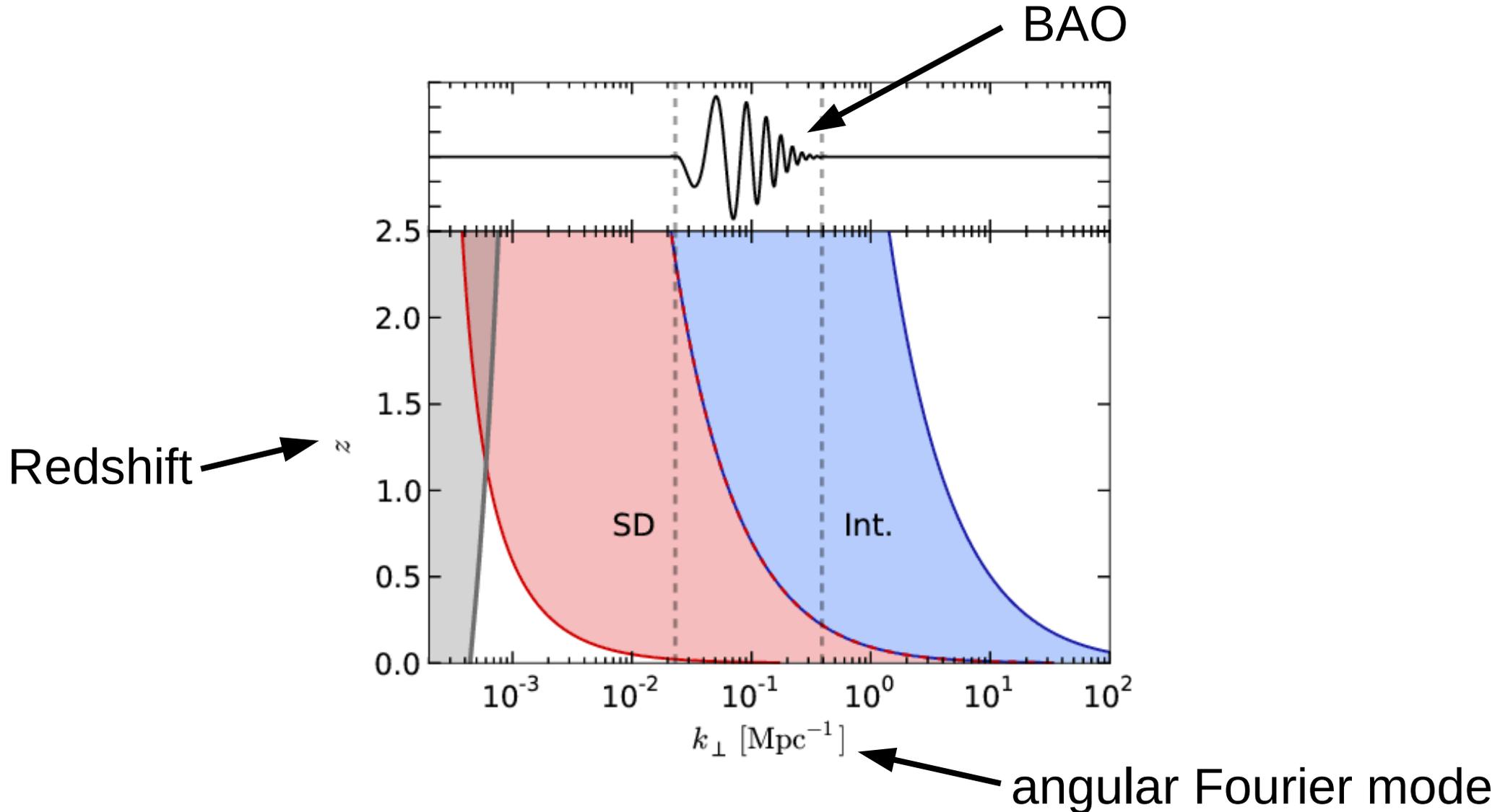
# Single dish or interferometer?

We can use the SKA in single-dish *or* interferometer mode



# Baryon acoustic oscillations

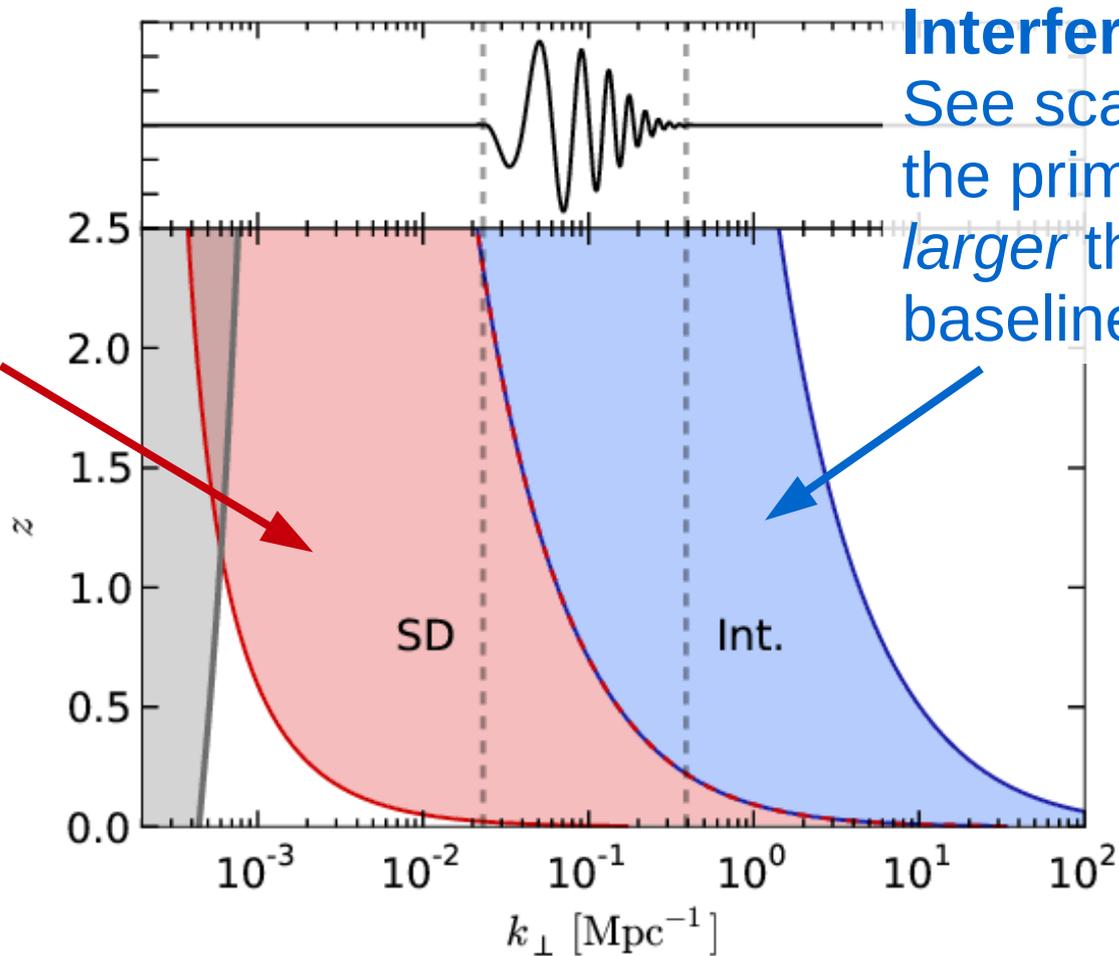
If we want to measure the BAO with the SKA, which mode is better?



# Baryon acoustic oscillations

If we want to measure the BAO with the SKA, which mode is better?

**Single-dish**  
See all scales  
larger than the  
beam

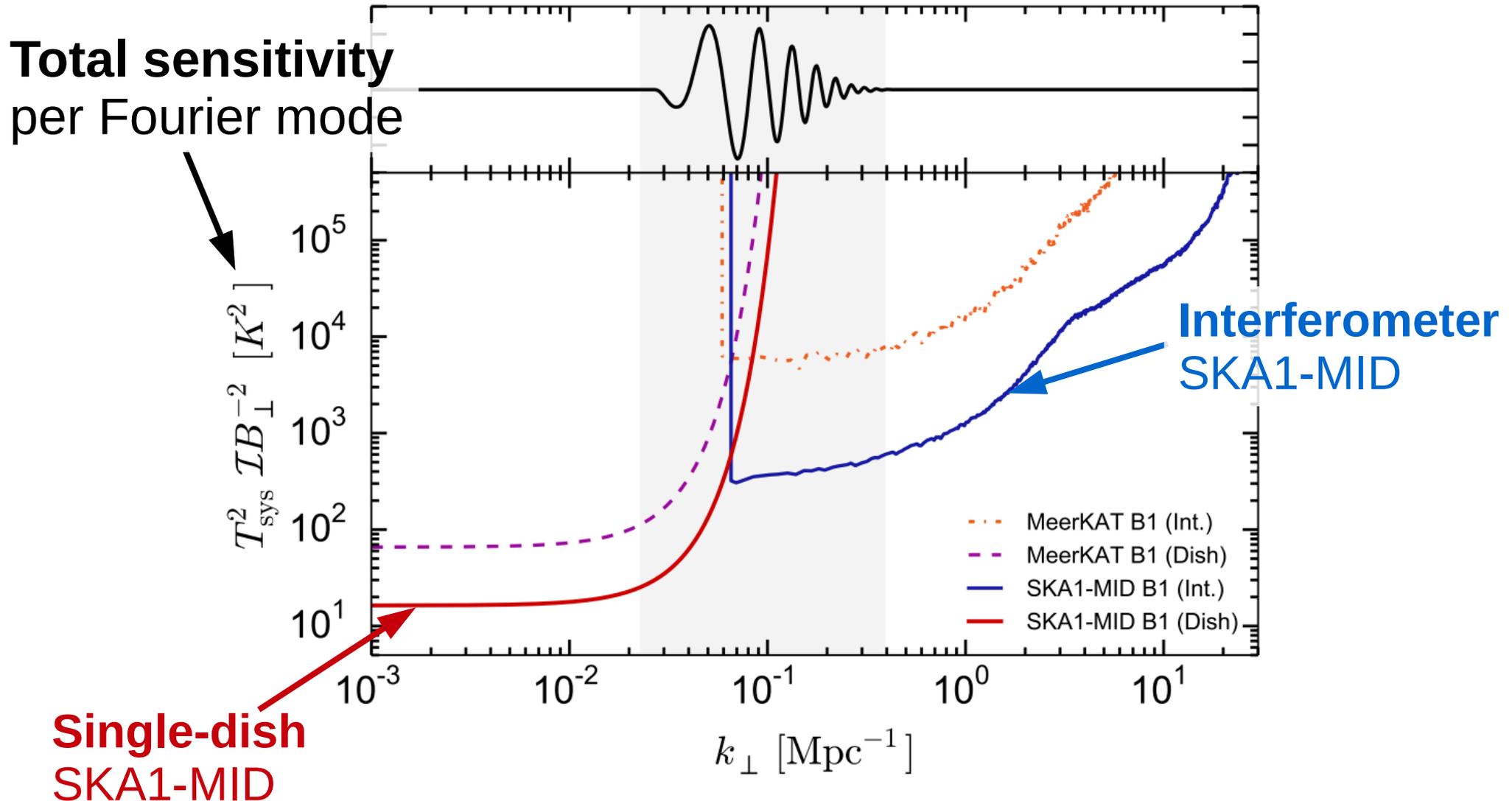


**Interferometer**

See scales *smaller* than  
the primary beam, but  
*larger* than the max.  
baseline

# Relative sensitivity

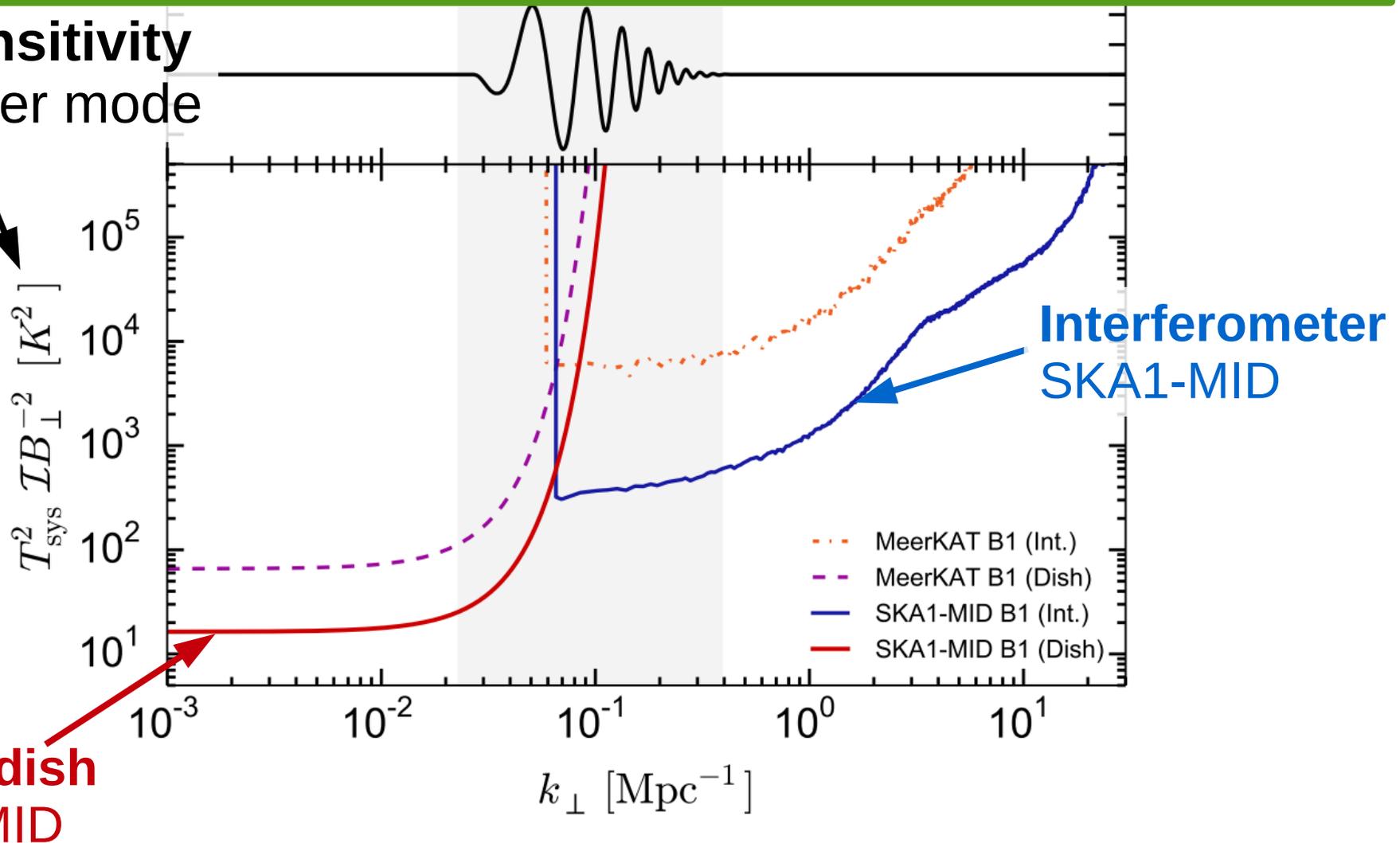
Interferometers are typically less sensitive than single-dish



# Relative sensitivity

SKA is too sparse for intensity mapping  
In interferometer mode

Total sensitivity  
per Fourier mode



Single-dish mode is harder to calibrate ( $1/f$  noise)  
Better to use a **dense interferometer array**



HIRAX /  
J. Sievers



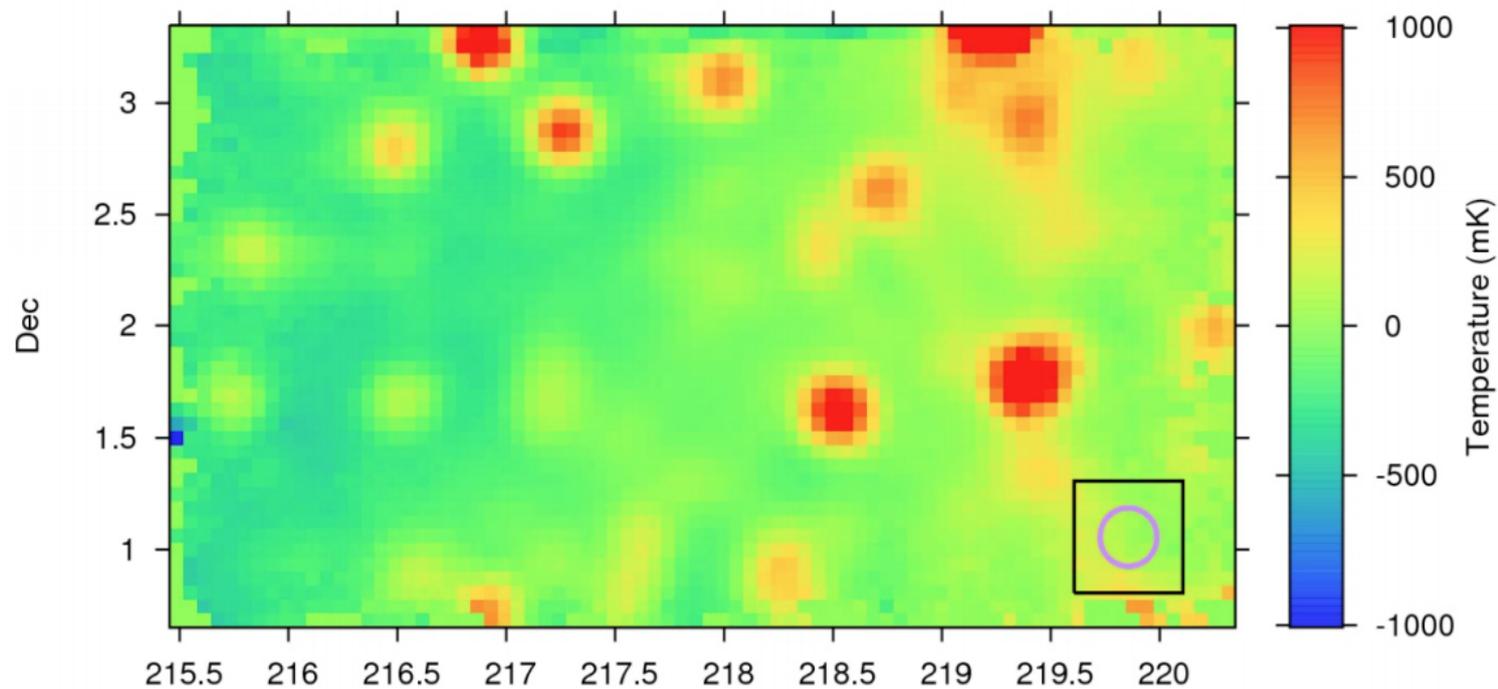
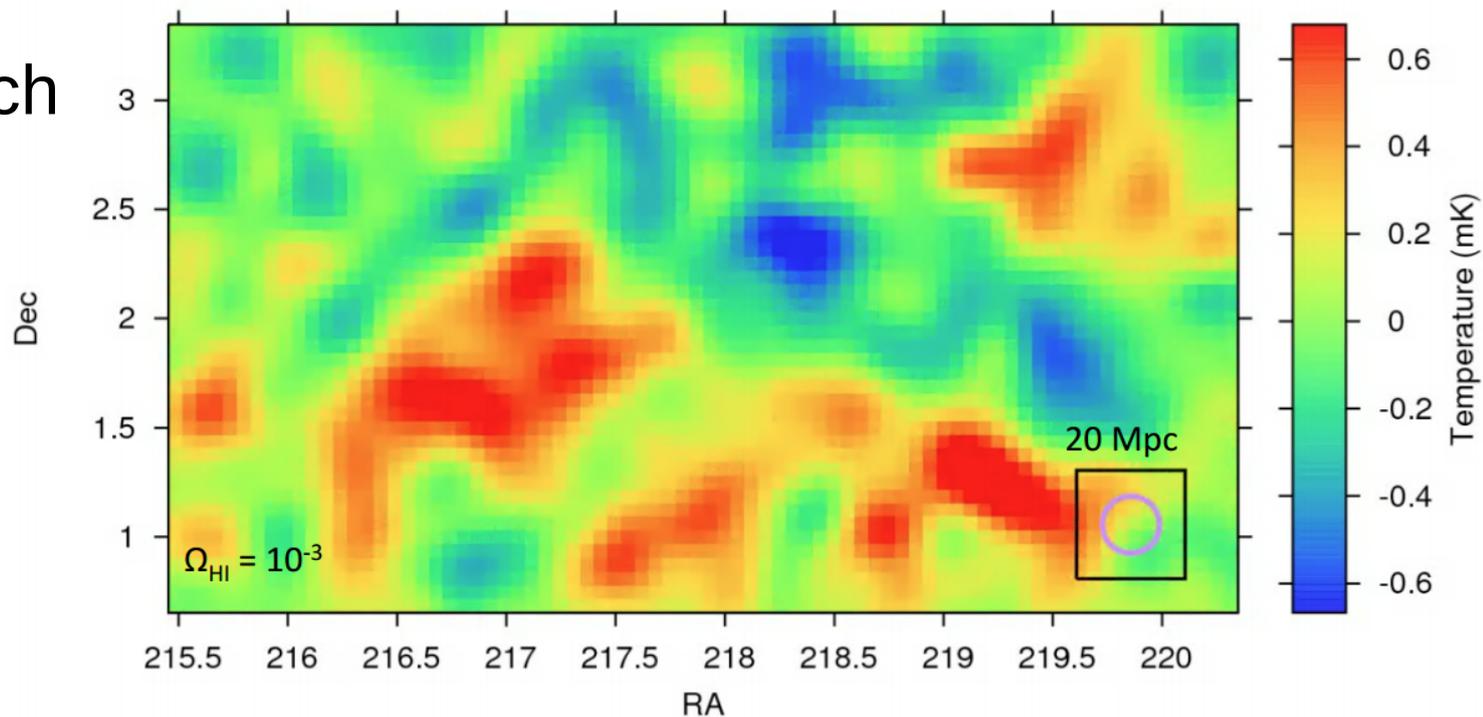
CHIME

# Foreground contamination

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E. Switzer / GBT

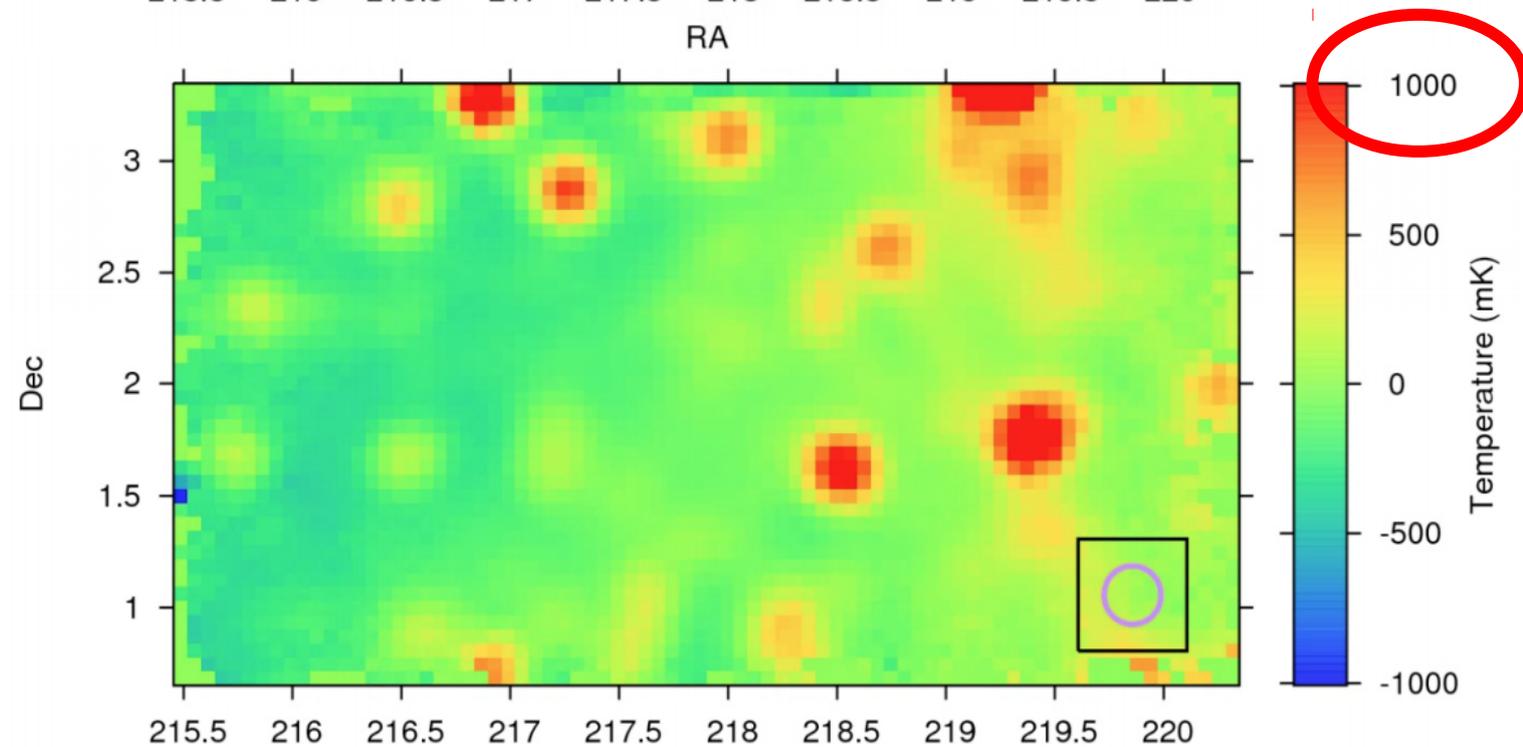
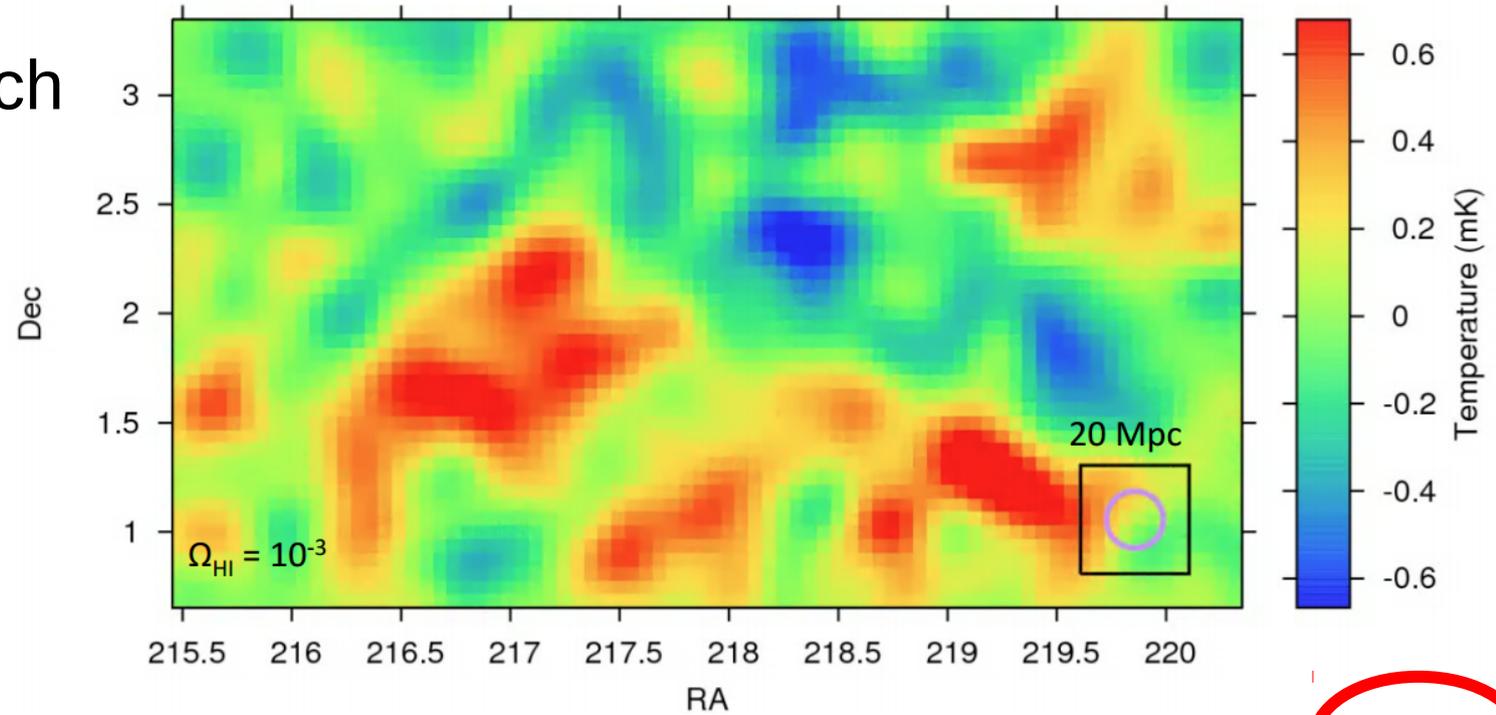
Our galaxy is much brighter than the 21cm signal



# Foreground contamination

E. Switzer / GBT

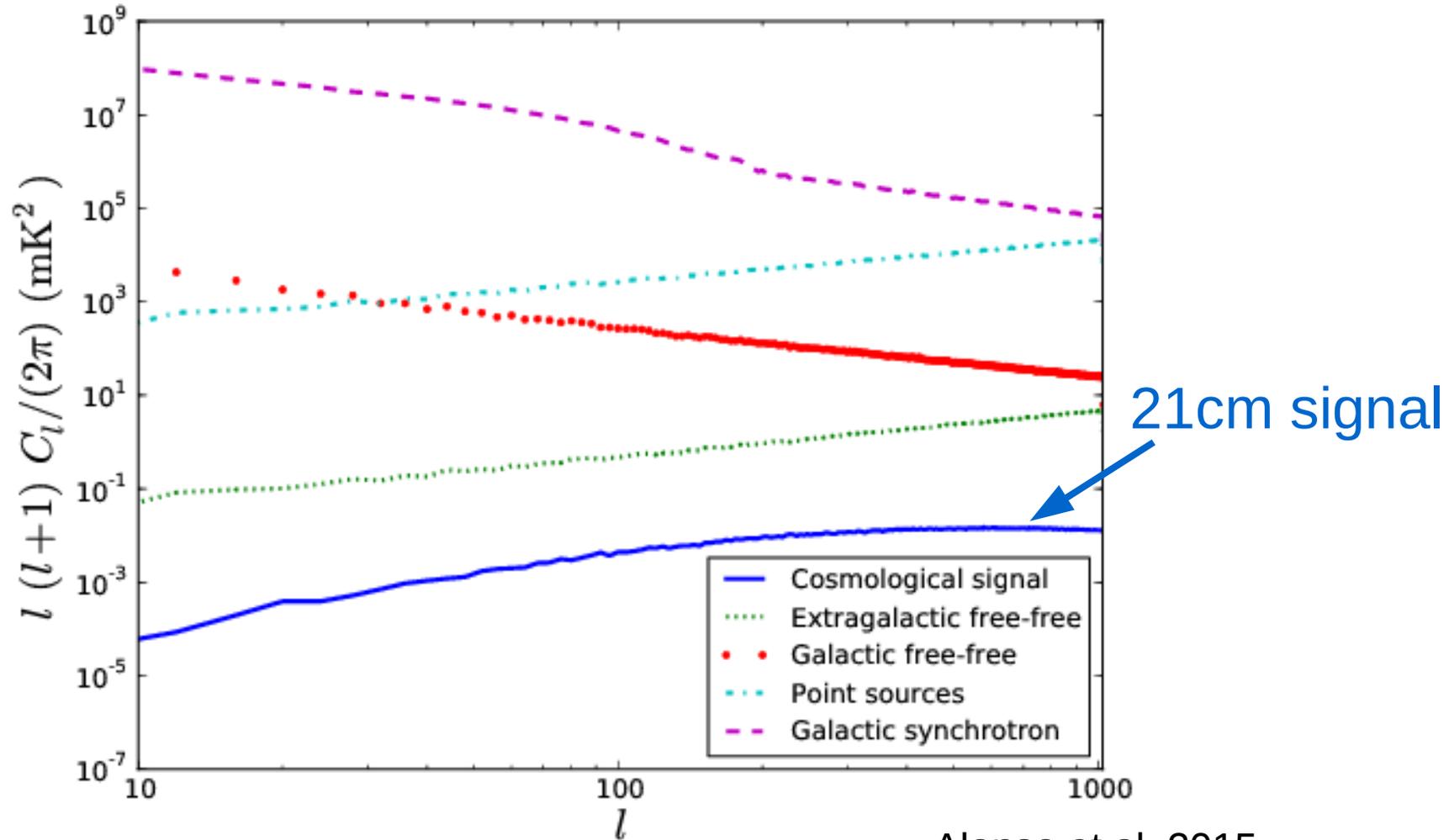
Our galaxy is much brighter than the 21cm signal



# Foreground contamination

Foregrounds dominate, but are **smooth** in frequency/angle?

Example foreground angular power spectra from simulations:

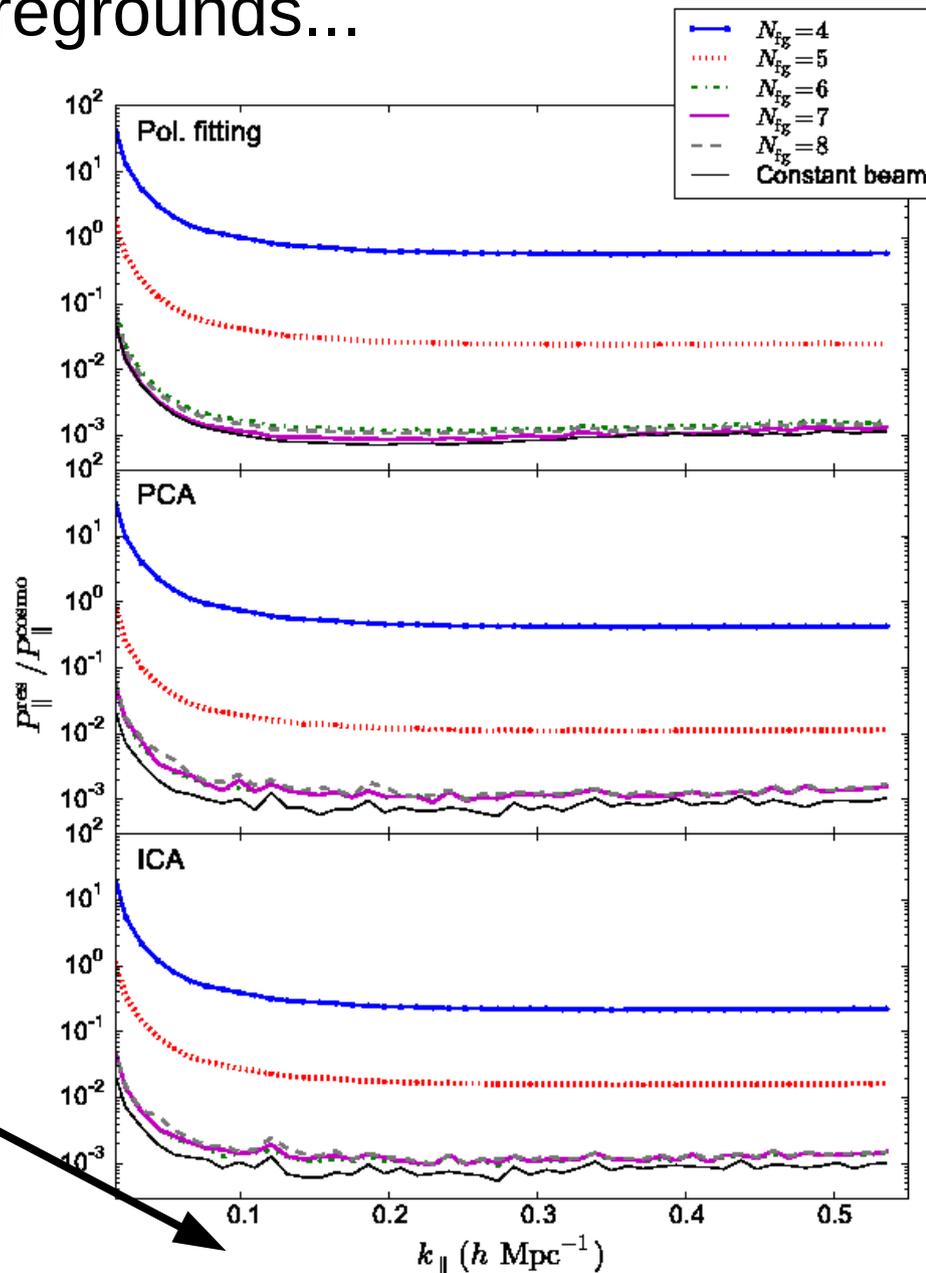


# Foreground contamination

Subtracting a few smooth (long-wavelength Fourier) modes should subtract most of the foregrounds...

Left-over foregrounds  
as a fraction of the  
21cm signal

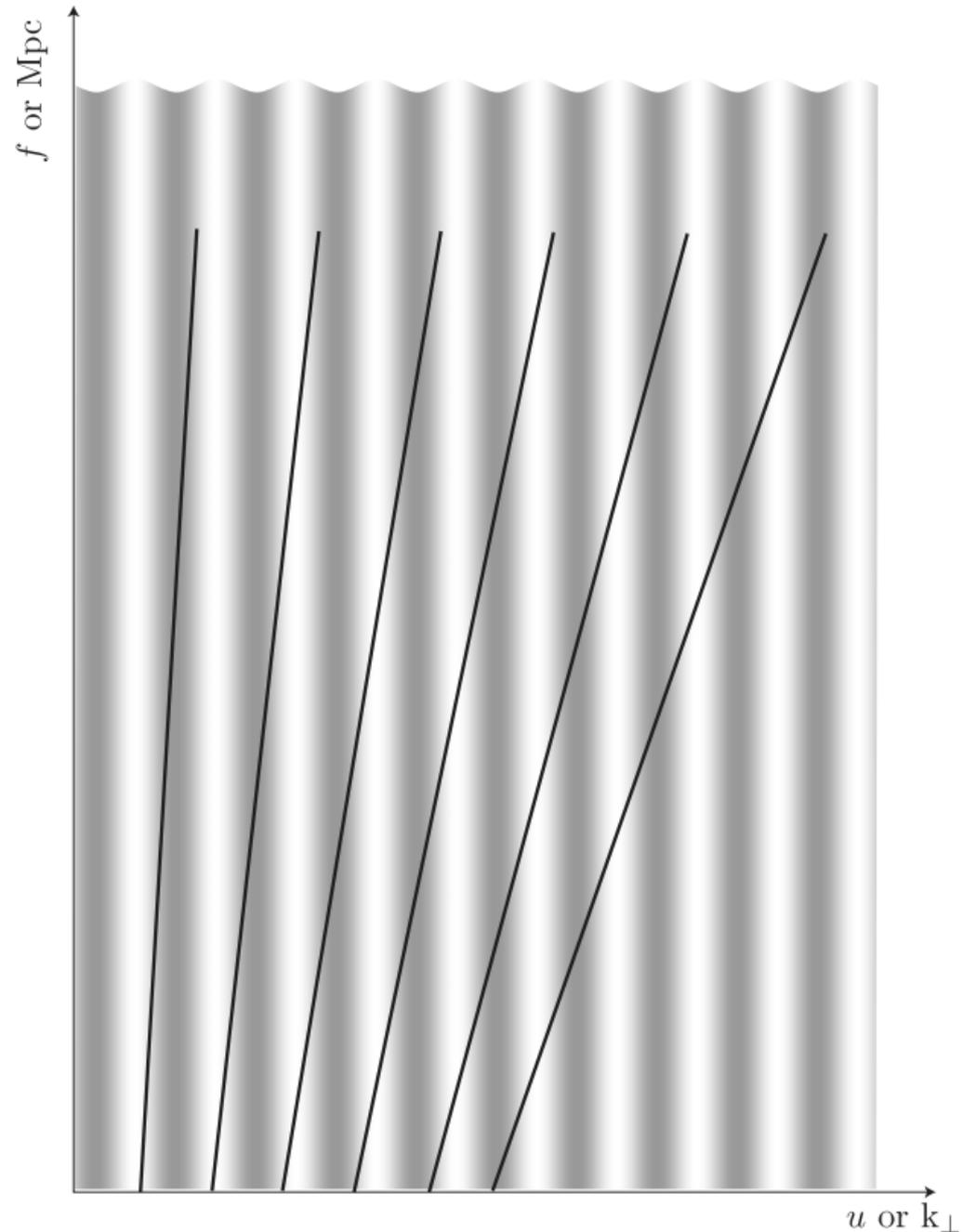
Fourier wavenumber  
in parallel (frequency)  
direction



# Foreground wedge

Interferometers are intrinsically chromatic  $\rightarrow$  sample different Fourier modes at different frequencies

We **pixelise** the Fourier plane (necessary for analysis)



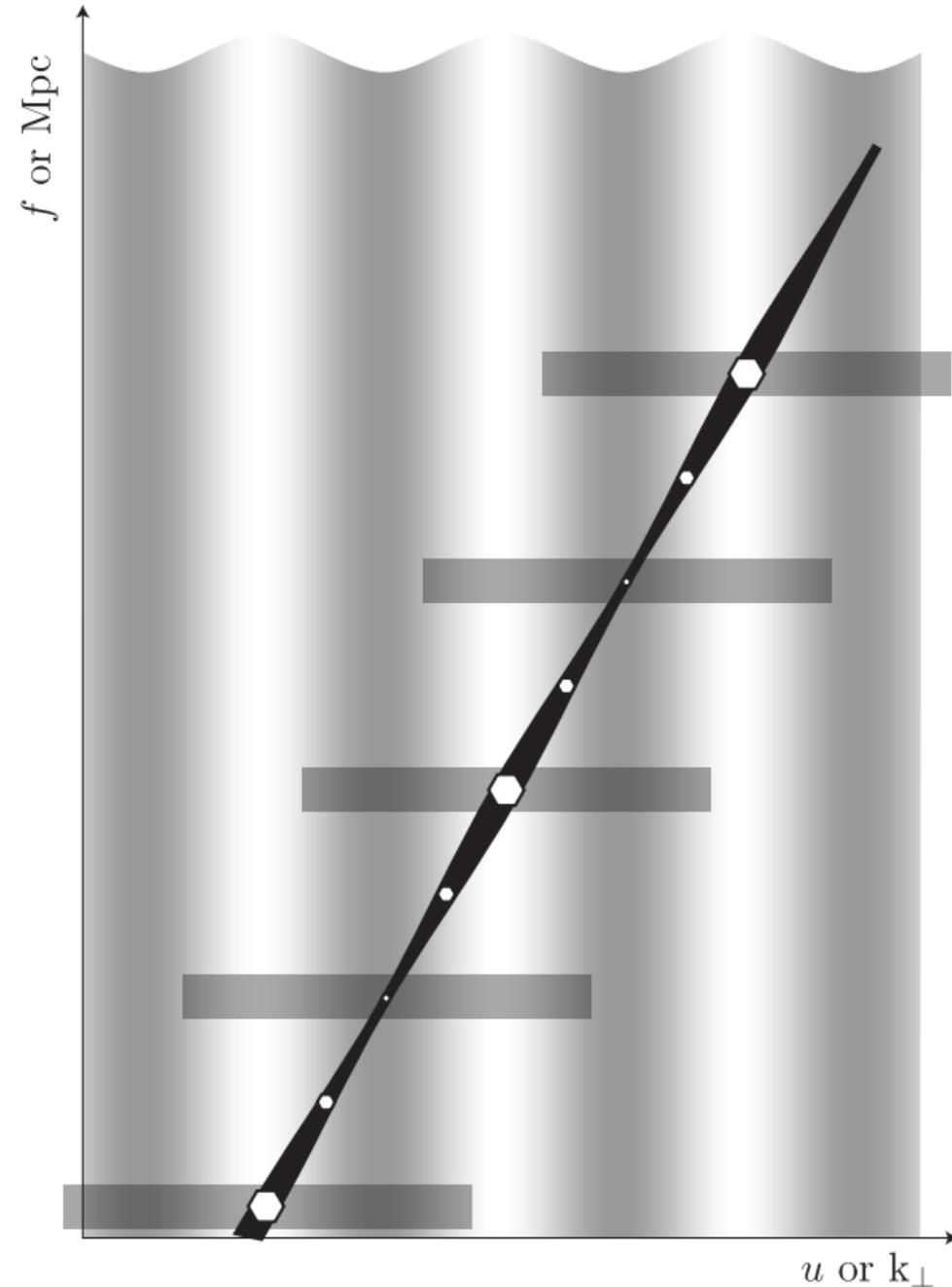
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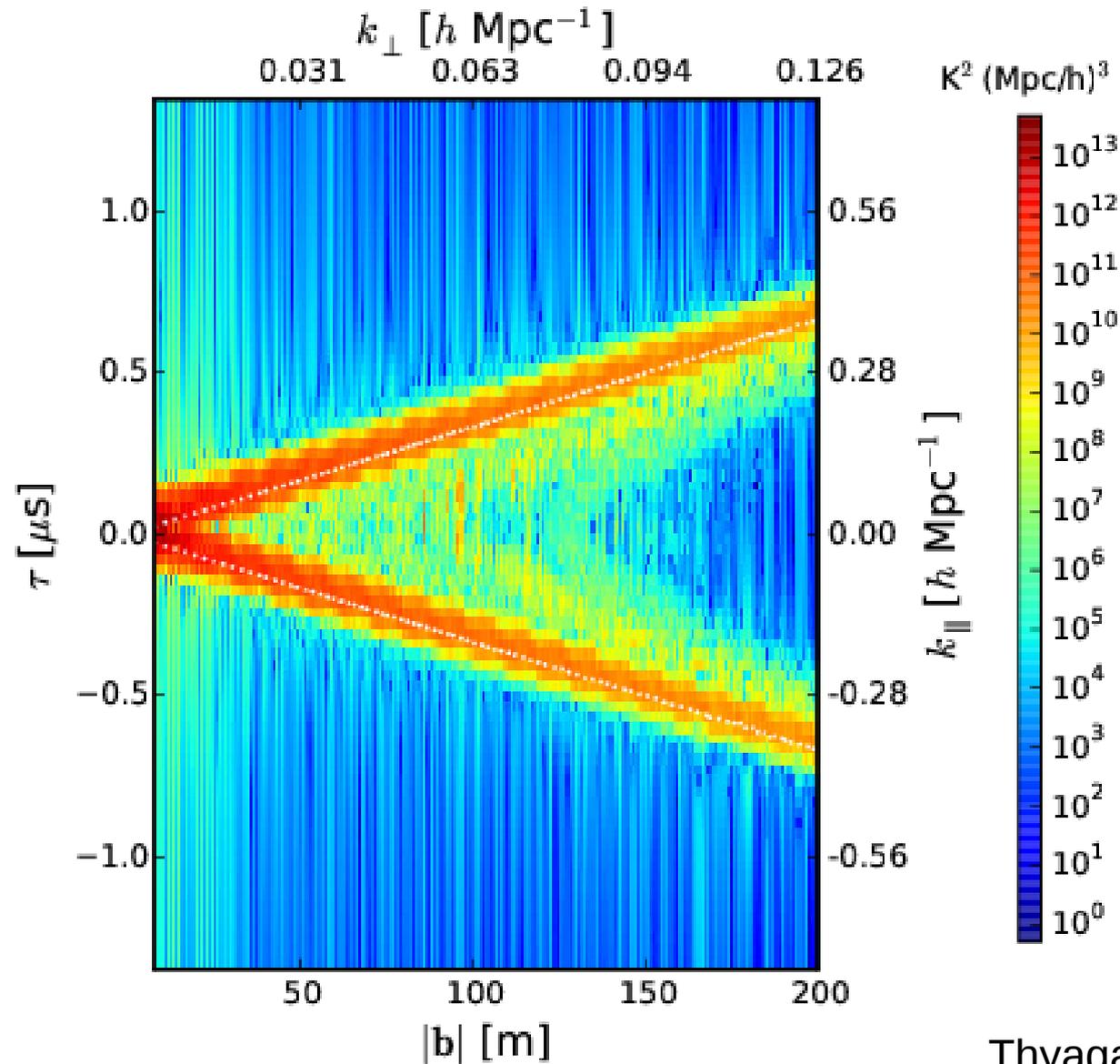
This loses some information  $\rightarrow$  leads to coupling between angular & frequency modes

Frequency structure of foregrounds is connected to small-scale angular modes!



# Foreground wedge

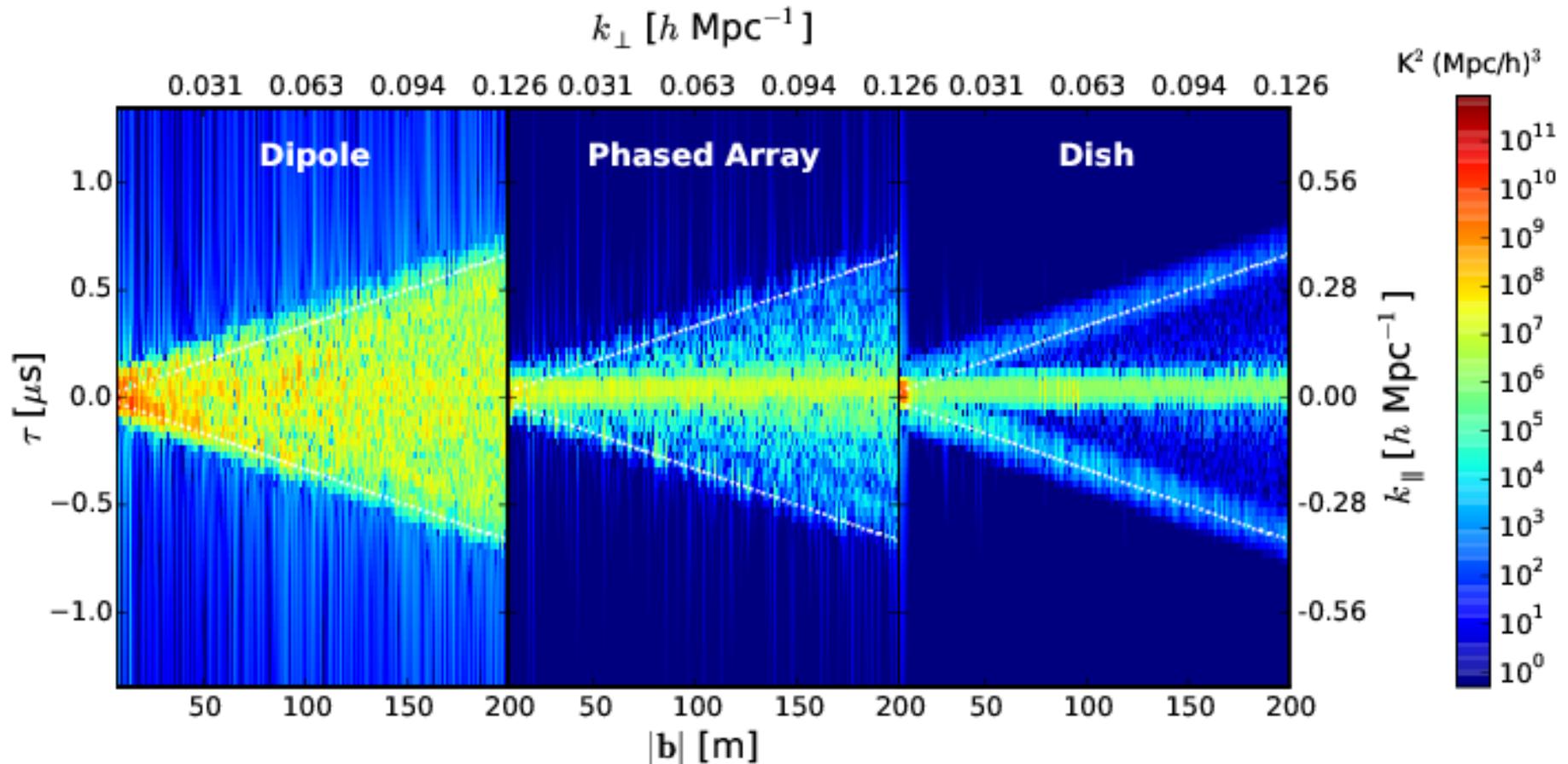
Some Fourier modes are completely spoiled by the bright foregrounds



# Foreground wedge

Some Fourier modes are completely spoiled by the bright foregrounds

Information lost in pixelisation depends in part on the primary beam



# Polarisation leakage

Polarised emission: angle of polarisation rotates as it passes through ionised gas → **Faraday rotation** effect

$$\alpha = \alpha_0 + \lambda^2 \psi(\mathbf{r}) \quad \psi(\mathbf{r}) = \frac{e^3}{2\pi(m_e c^2)^2} \int_0^r dr' n_e(\mathbf{r}') B_{\parallel}(\mathbf{r}')$$

# Polarisation leakage

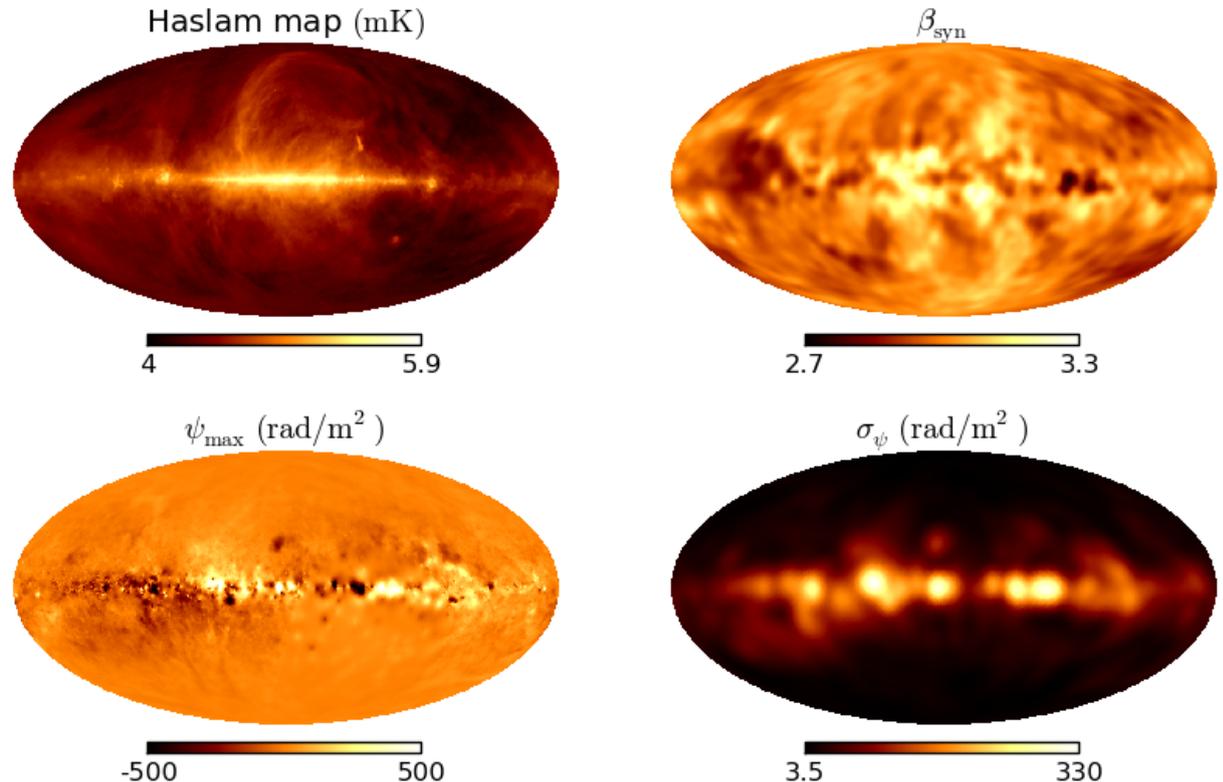
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Frequency-dependent:  
**smooth** spectra gain  
extra **structure**

Rotation happens faster  
at longer wavelengths  
→ worse at low freq.

More rotation near the  
galactic plane



# Polarisation leakage

Radio telescopes can't perfectly separate different polarisations

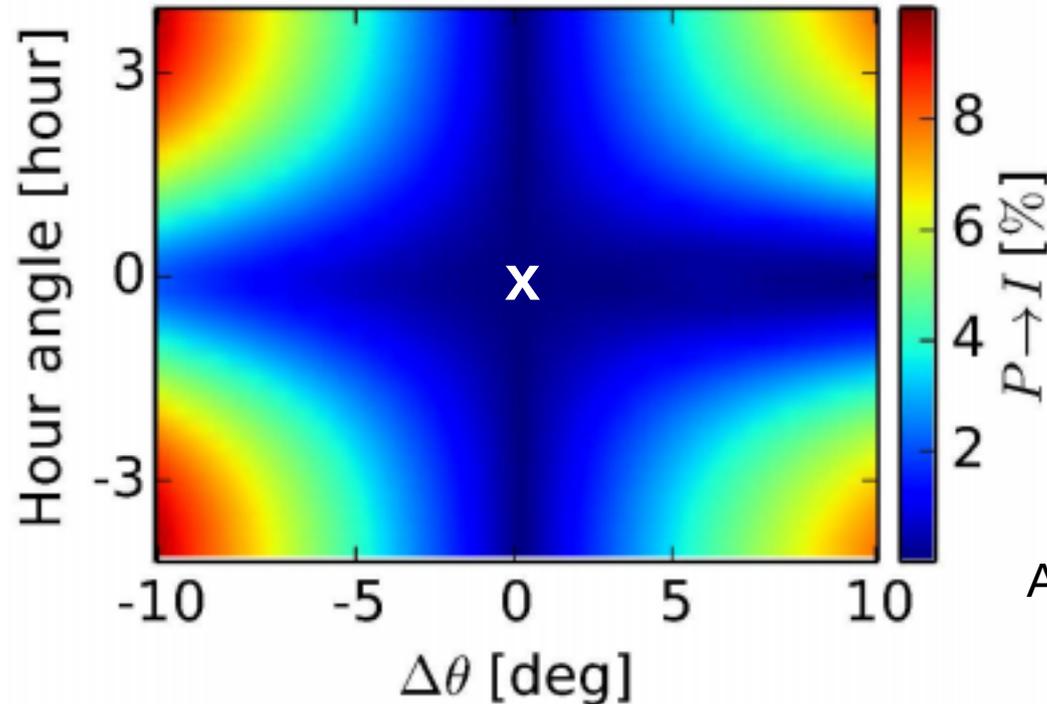
→ Polarised emission **leaks** into observed total intensity signal

# Polarisation leakage

Radio telescopes can't perfectly separate different polarisations

→ Polarised emission **leaks** into observed total intensity signal

Leakage is worse around the edges of the beam



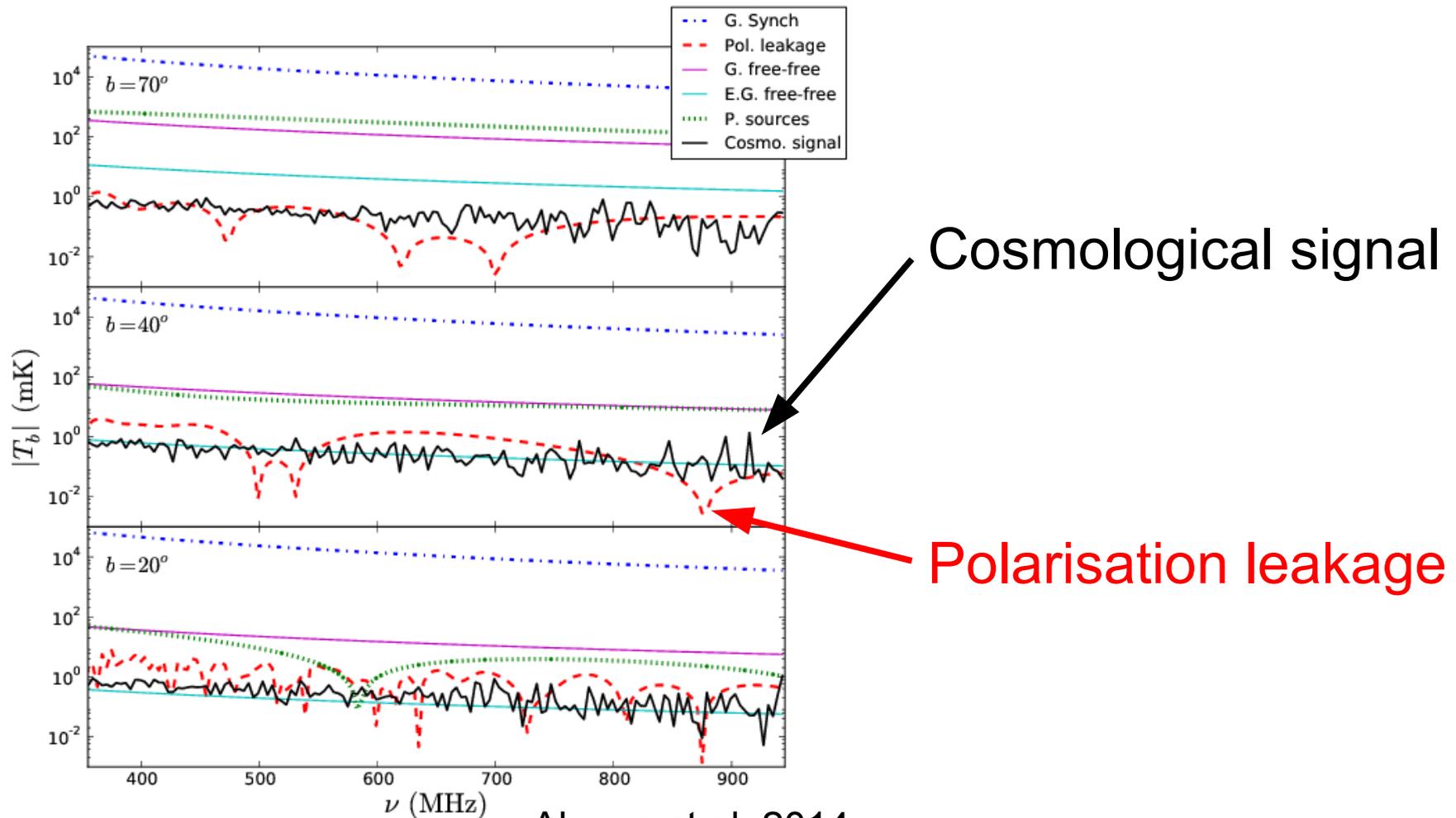
Asad et al. 2015

Complicated signal: Depends on frequency, polarisation angle of source, position on the sky, orientation of the radio receiver...

# Polarisation leakage

Polarised foregrounds are fainter than total intensity ones **but** have extra spectral structure due to **Faraday rotation**

Much harder to separate from the cosmological signal!



# Open questions and the future of radio cosmology

## **Open questions**

- Can radio + optical/IR surveys work better together?  
(intrinsic alignment, deblending, multi-tracer)

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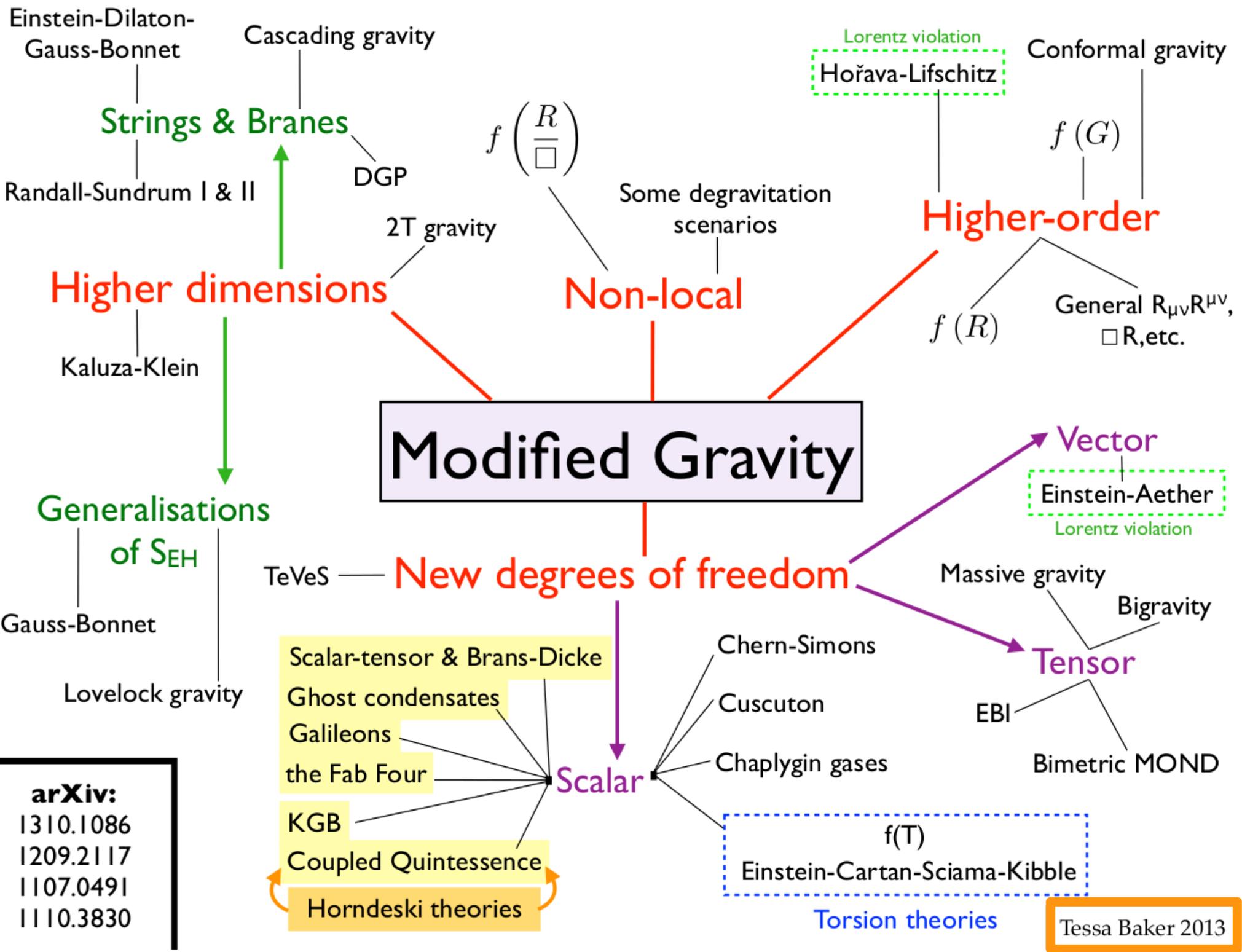
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(intrinsic alignment, deblending, multi-tracer)
- Can we handle IM foregrounds well enough?
- What are FRBs?
- Can we trust intensity maps? (cross-correlation)
- What is the most useful thing we can do to solve dark energy / gravity / etc. problems?

# The future of radio cosmology

- Epoch of Reionisation / dark ages → go to the Moon!
- Dense aperture arrays (MFAA/SKA2)
- The Cosmic Atlas (21cm map of the entire Universe!)
- Second-order effects (polarised 21cm, IM lensing)

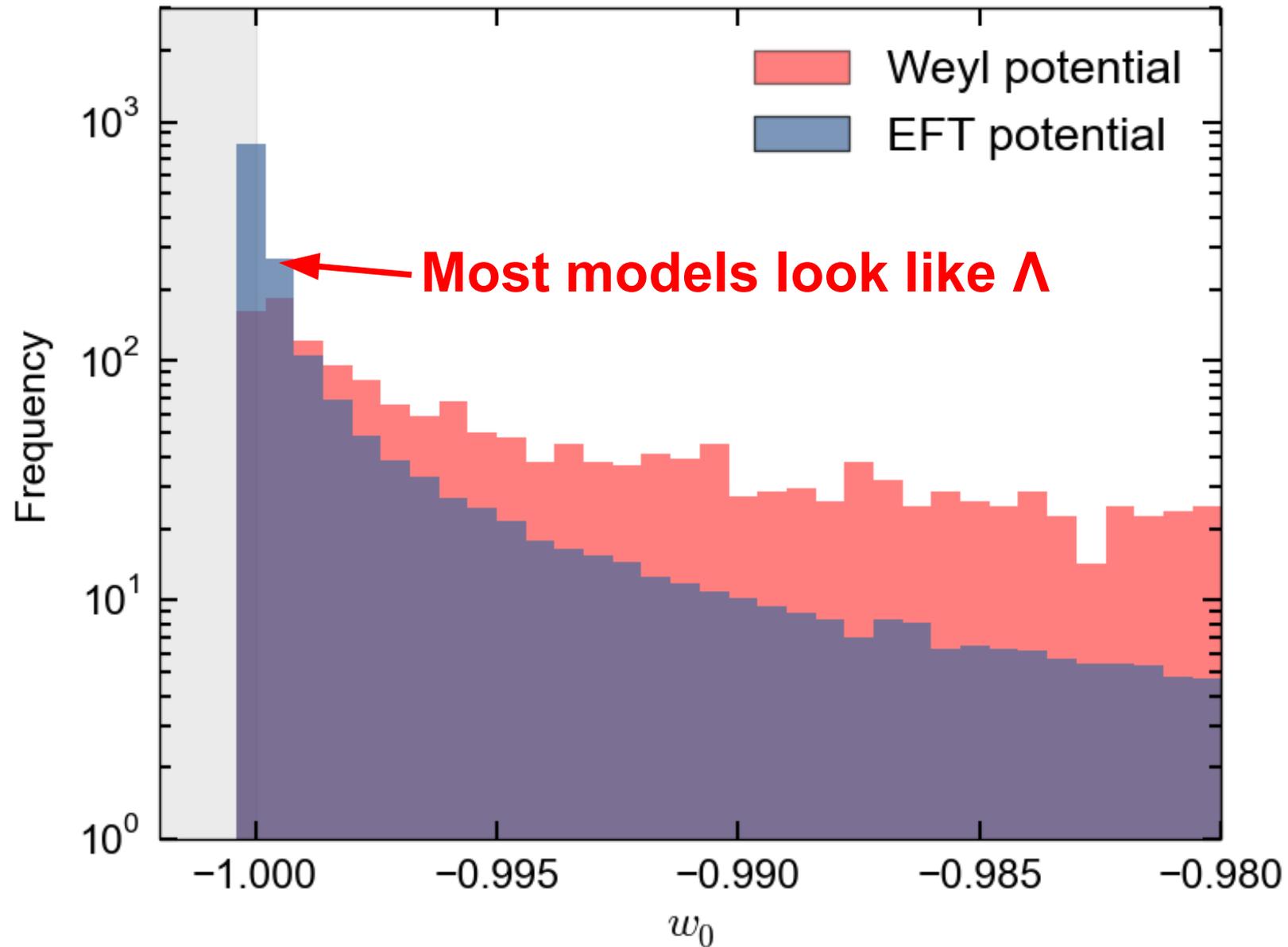




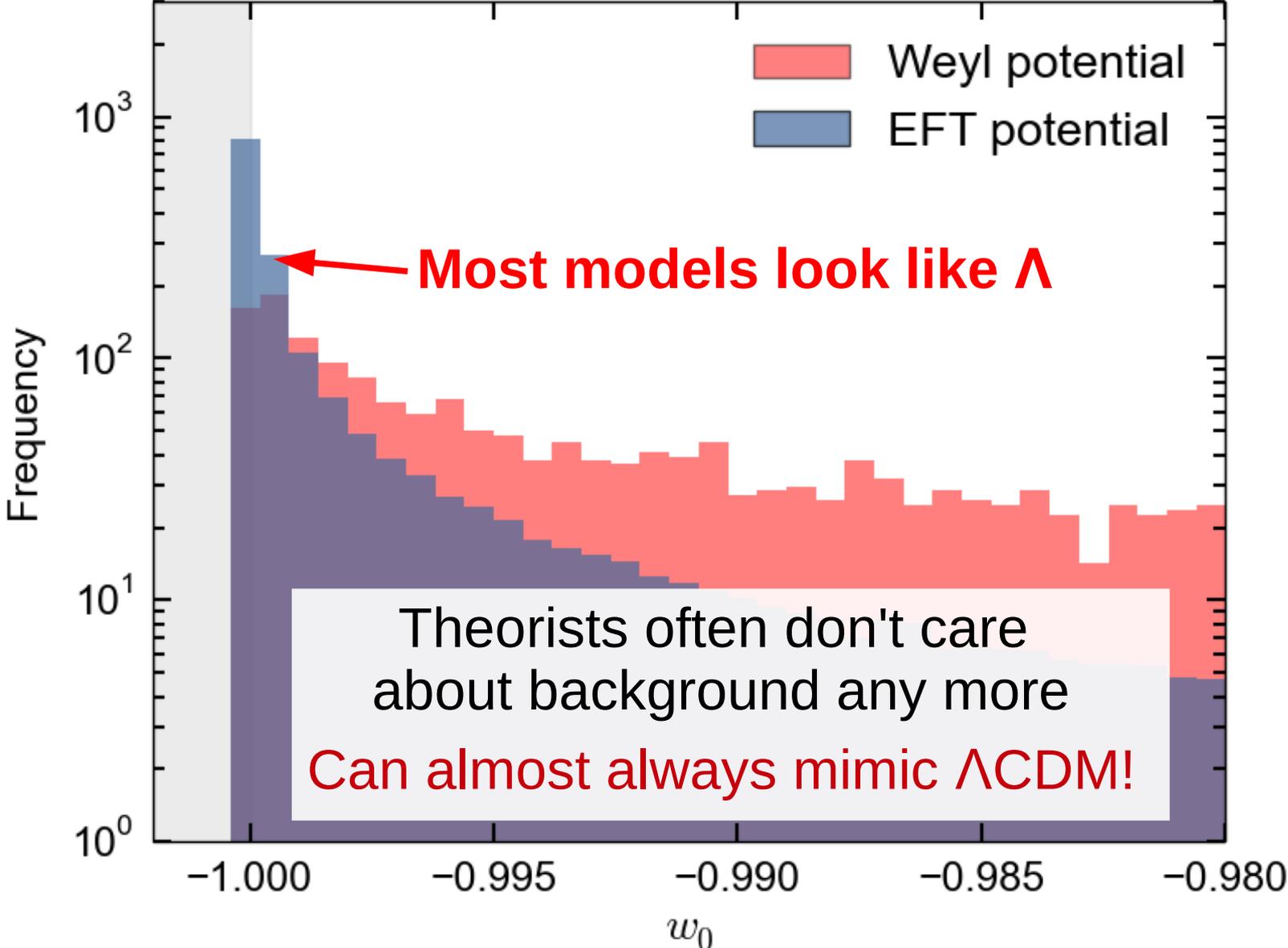
**arXiv:**  
 1310.1086  
 1209.2117  
 1107.0491  
 1110.3830

Tessa Baker 2013

*A priori* predictions for  $w$  from a specific class of theories  
(Here: quintessence)



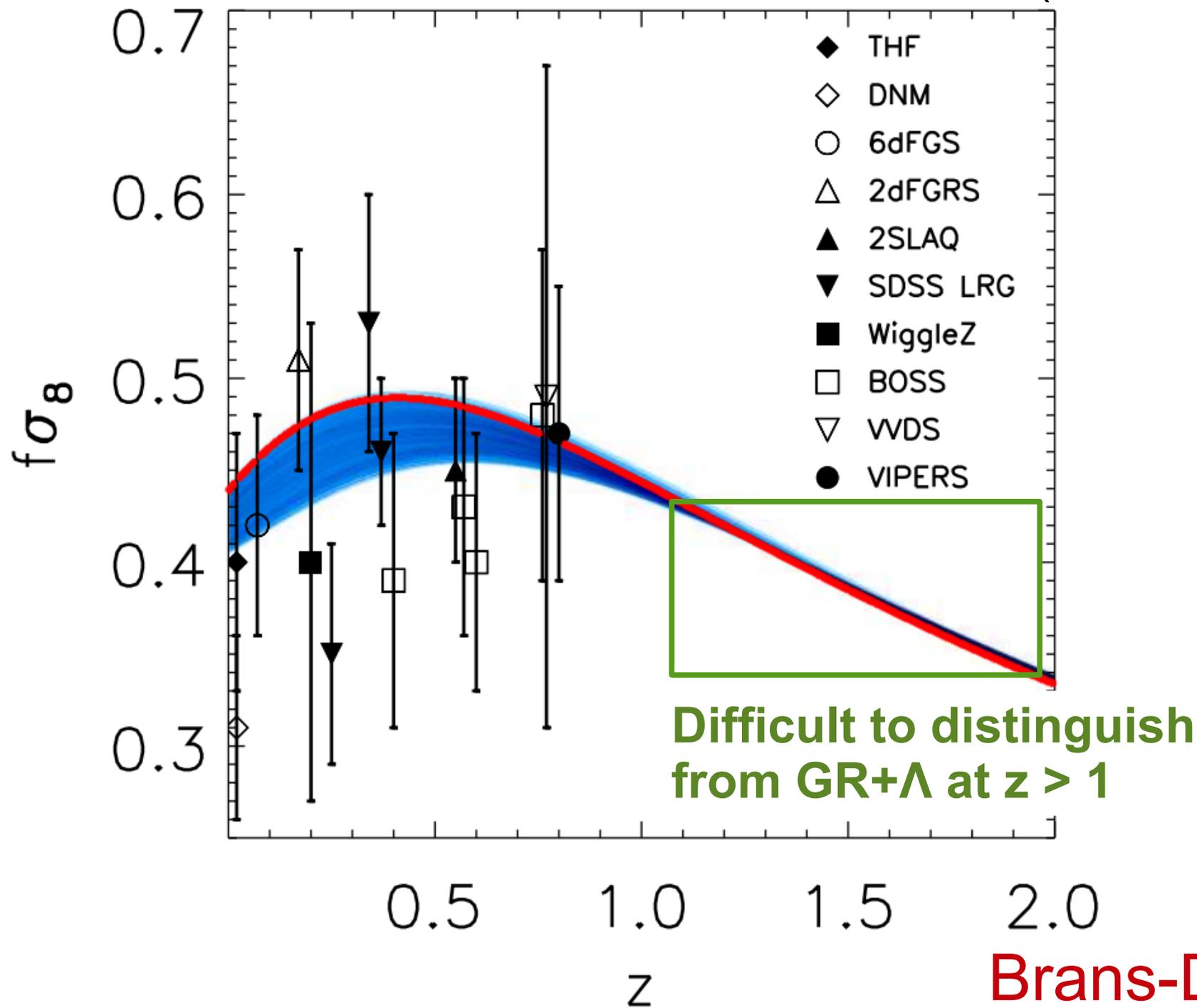
*A priori* predictions for  $w$  from a specific class of theories  
(Here: quintessence)



# Theory priors

BD

Perenon et al.  
(1506.03047)



# The End

Thanks!

*Email:* [philbull@gmail.com](mailto:philbull@gmail.com)